

EQUIVALENT LINKAGES OF COMPRESSOR MECHANISMS

Numerical variant of an old graphical method

Although the equivalent linkage of a reciprocating piston compressor is well known, the equivalent linkages of other types of compressors are not.

The method will be illustrated on two compressor mechanisms

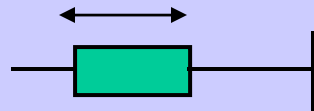
1. Reciprocating piston compressor
2. Rotary vane compressor with eccentric vanes

EQUIVALENT KINEMATIC PAIRS

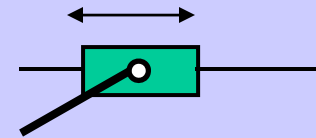
Joint



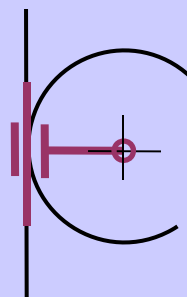
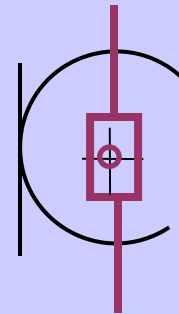
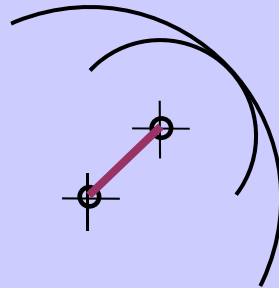
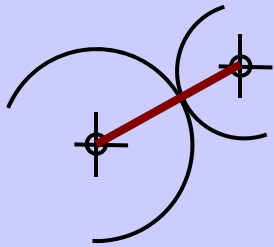
Slider



Slider and joint

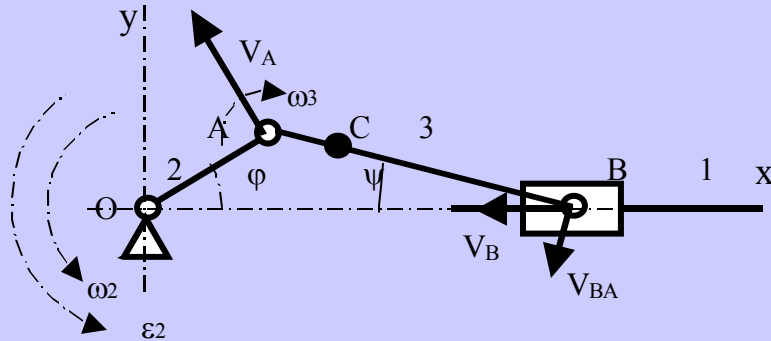


Contacting surfaces



RECIPROCATING PISTON COMPRESSOR

VELOCITY

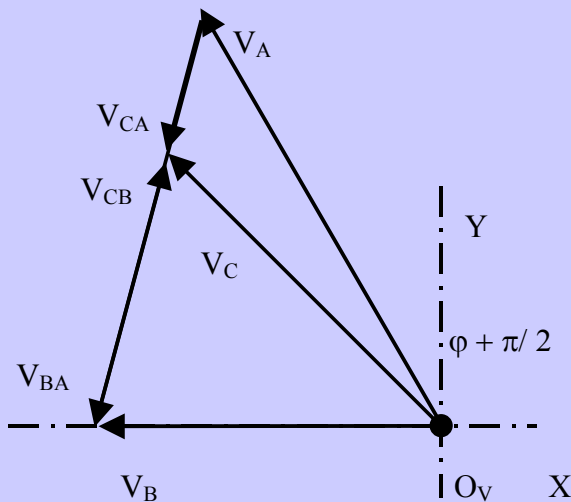


$$\mathbf{V}_B = \mathbf{V}_A + \mathbf{V}_{BA}$$

$$V_A = r \cdot \omega_2$$

$$\omega_3 = \frac{V_{BA}}{L_3}$$

$$\sin \psi = \frac{r_2}{L_3} \cdot \sin \phi$$



RECIPROCATING PISTON COMPRESSOR

Velocity

Projected into x axis

$$V_B \cdot \cos \pi = V_A \cdot \cos \left(\varphi + \frac{\pi}{2} \right) + V_{BA} \cdot \cos \left(\frac{3\pi}{2} - \psi \right)$$

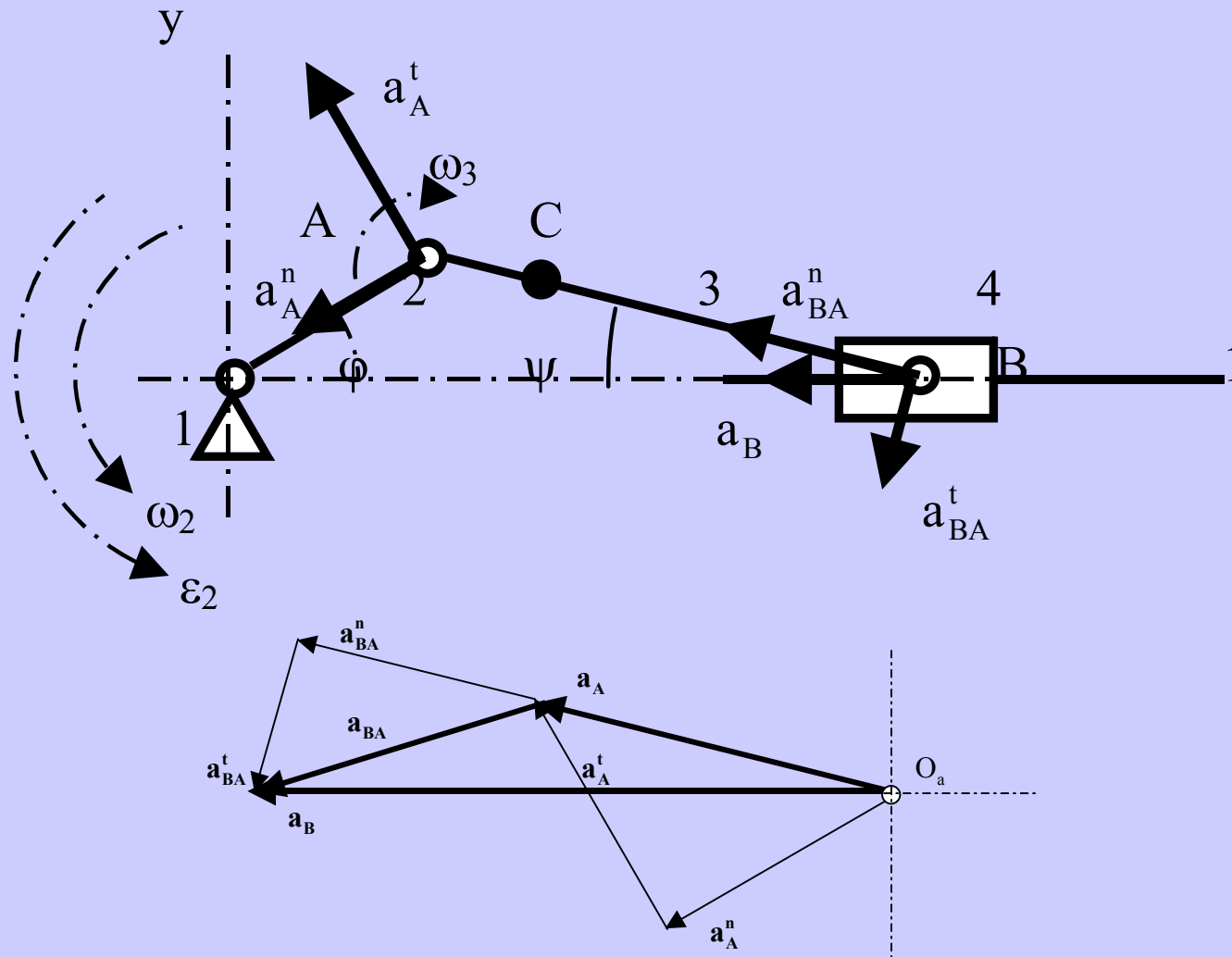
Projected into y axis

$$V_B \cdot \sin \pi = V_A \cdot \sin \left(\varphi + \frac{\pi}{2} \right) + V_{BA} \cdot \sin \left(\frac{3\pi}{2} - \psi \right)$$

Unknown magnitudes of V_B and V_{BA} can be calculated

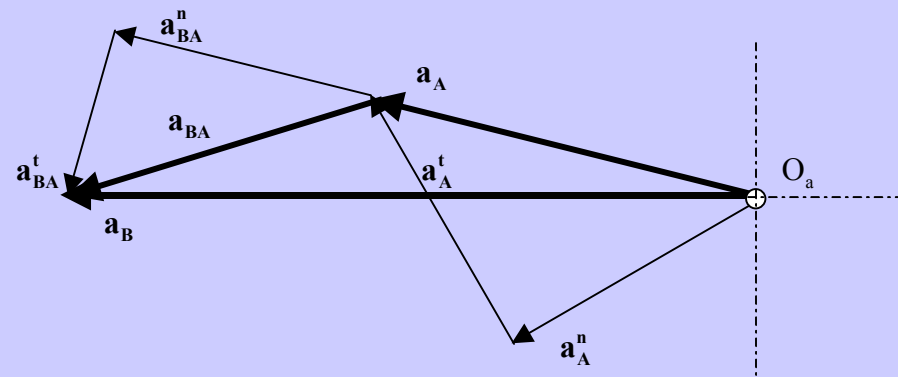
RECIPROCATING PISTON COMPRESSOR

ACCELERATION



RECIPROCATING PISTON COMPRESSOR

ACCELERATION



$$\mathbf{a}_B = \mathbf{a}_A + \mathbf{a}_{BA}$$

$$\omega_3 = \frac{V_{BA}}{L_3}; \quad \mathbf{a}_{BA}^n = L_3 \cdot \omega_3^2 = \frac{V_{BA}^2}{L_3}$$

$$\mathbf{a}_B = \mathbf{a}_A^n + \mathbf{a}_A^t + \mathbf{a}_{BA}^n + \mathbf{a}_{BA}^t$$

$$\mathbf{a}_A^n = r_2 \cdot \omega_2^2; \quad \mathbf{a}_A^t = \varepsilon \cdot r_2$$

\mathbf{a}_{BA}^t has the direction of \mathbf{v}_{BA}

RECIPROCATING PISTON COMPRESSOR

ACCELERATION

$$a_B \cdot \cos \pi = a_A^n \cdot \cos(\varphi + \pi) + a_A^t \cdot \cos\left(\varphi + \frac{\pi}{2}\right) + a_{BA}^n \cdot \cos(\pi - \psi) + a_{BA}^t \cdot \cos\left(\frac{3\pi}{2} - \psi\right)$$

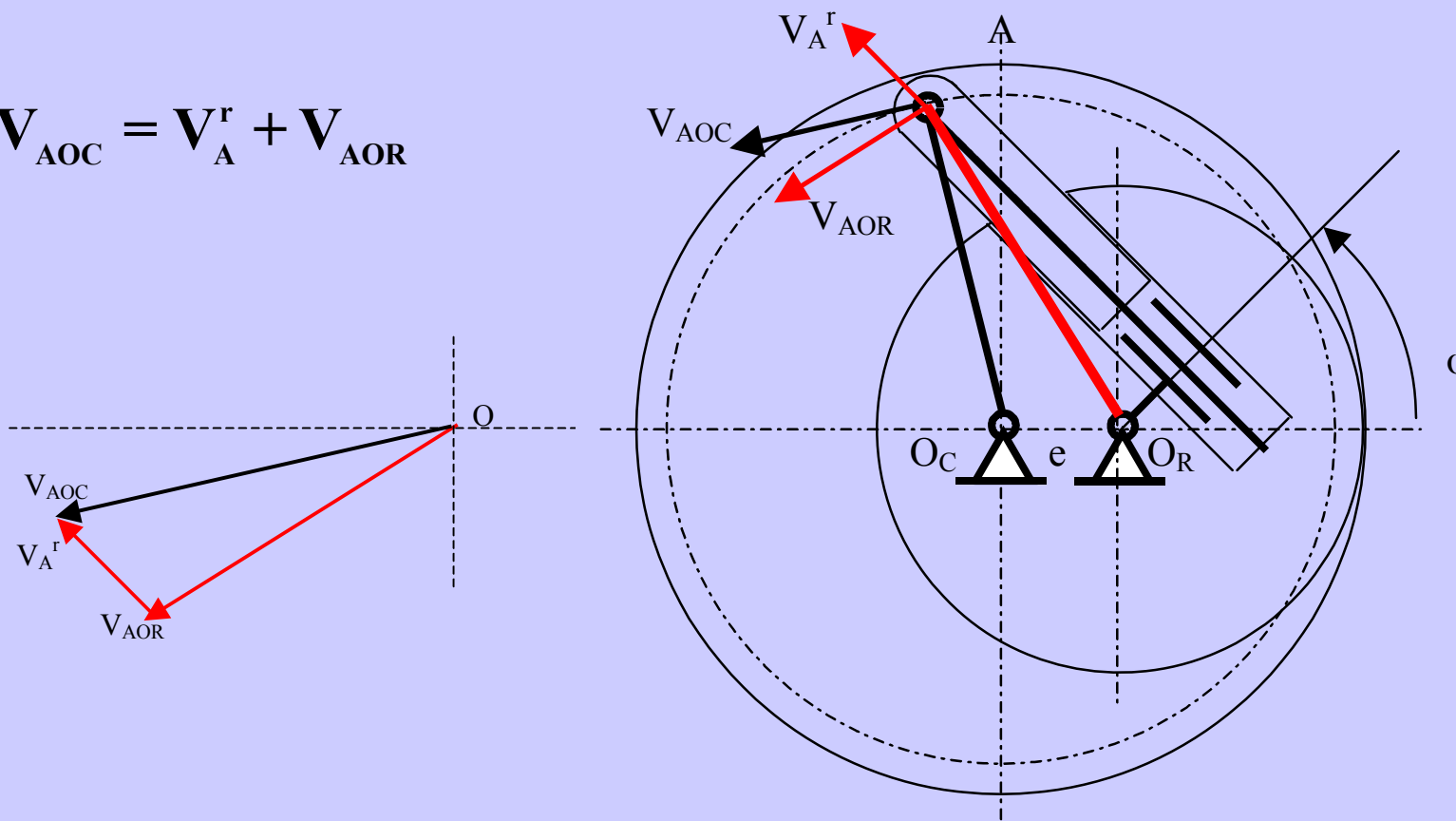
$$a_B \cdot \cos \pi = a_A^n \cdot \cos(\varphi + \pi) + a_A^t \cdot \cos\left(\varphi + \frac{\pi}{2}\right) + a_{BA}^n \cdot \cos(\pi - \psi) + a_{BA}^t \cdot \cos\left(\frac{3\pi}{2} - \psi\right)$$

Unknown magnitudes of a_B and a_{BA}^t can be calculated

ROTARY VANE COMPRESSOR WITH ECCENTRIC VANES

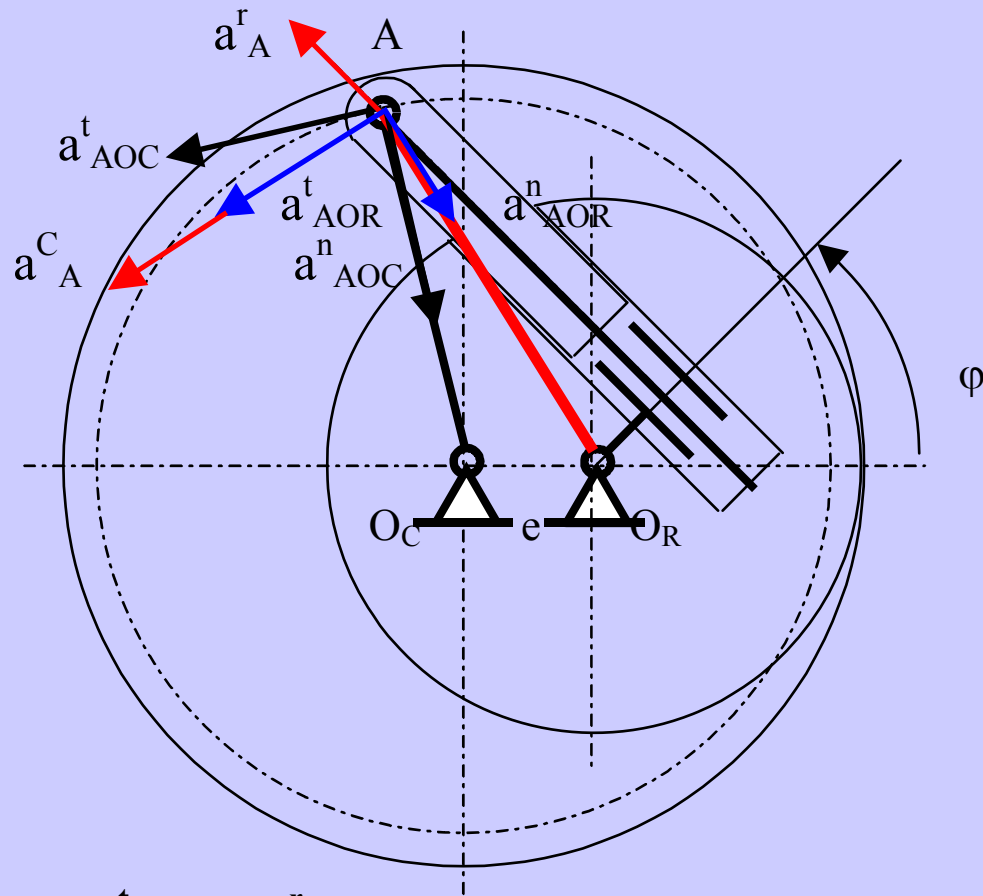
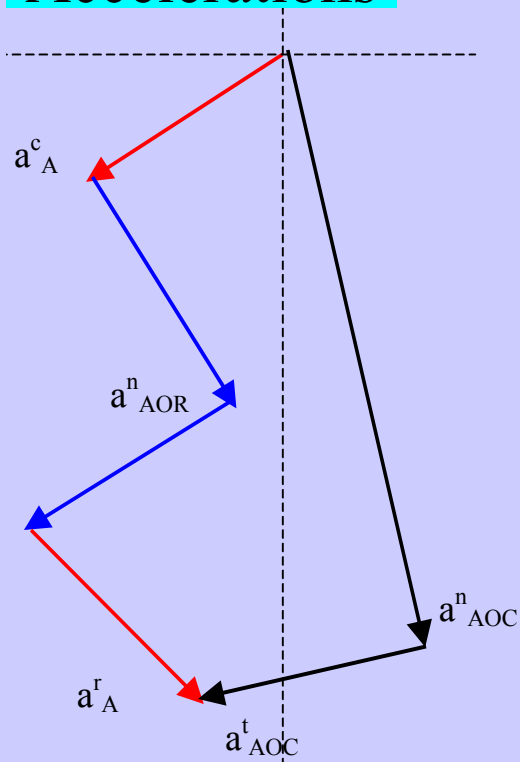
Velocity

$$\mathbf{V}_{AOC} = \mathbf{V}_A^r + \mathbf{V}_{AOR}$$



ROTARY VANE COMPRESSOR WITH ECCENTRIC VANES

Accelerations

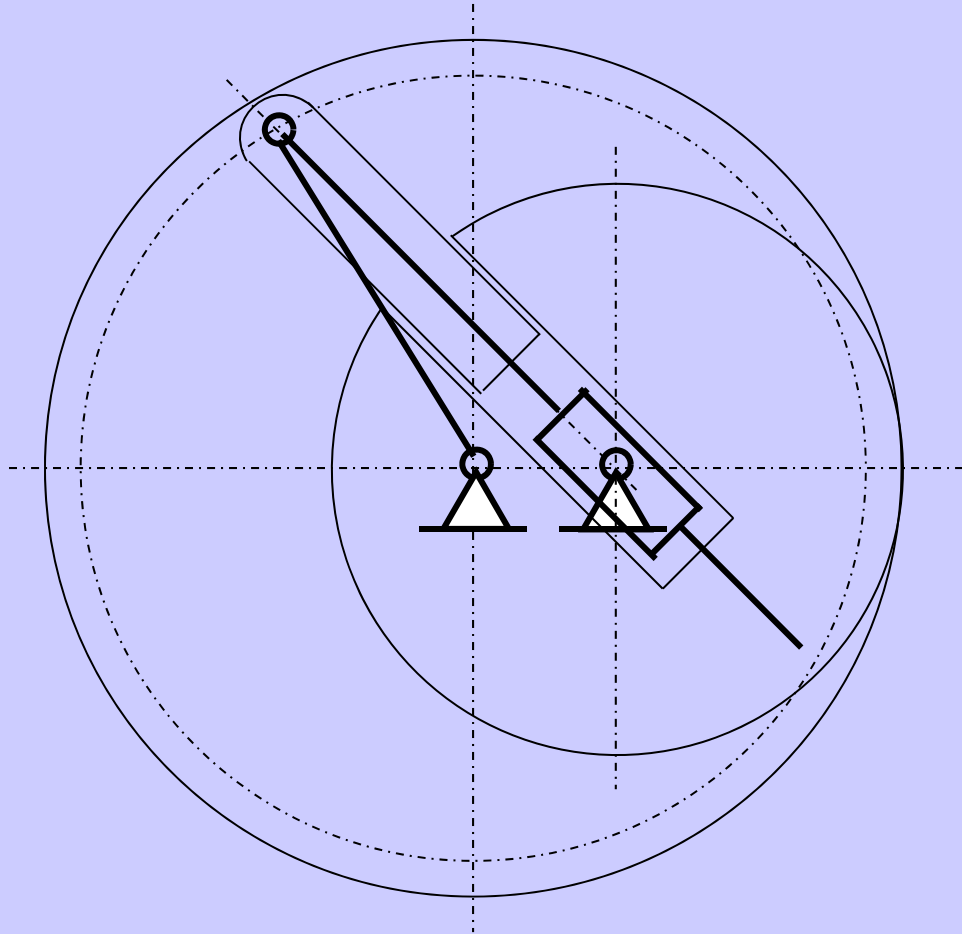


$$\mathbf{a}_A = \mathbf{a}_A^c + \mathbf{a}_{AOR} + \mathbf{a}_A^r$$

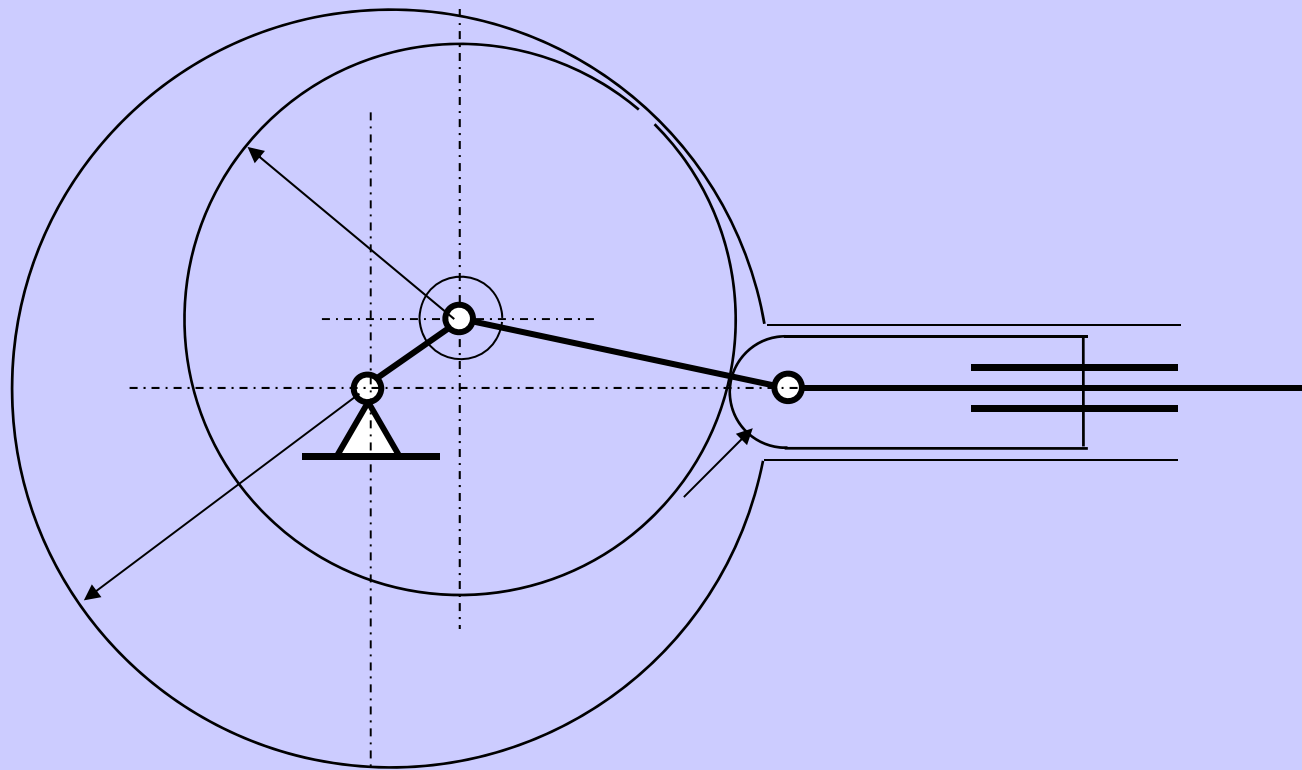
$$\mathbf{a}_{AOC}^n + \mathbf{a}_{AOC}^t = \mathbf{a}_A^c + \mathbf{a}_{AOR}^n + \mathbf{a}_{AOR}^t + \mathbf{a}_A^r$$

$$\mathbf{a}_A^C = 2 \cdot \boldsymbol{\omega} \times \mathbf{v}_A^r; \quad |\mathbf{a}_A^C| = 2 \cdot \omega \cdot v_A^r \cdot \sin(\omega, v_A^r) = 2 \cdot \omega \cdot v_A^r$$

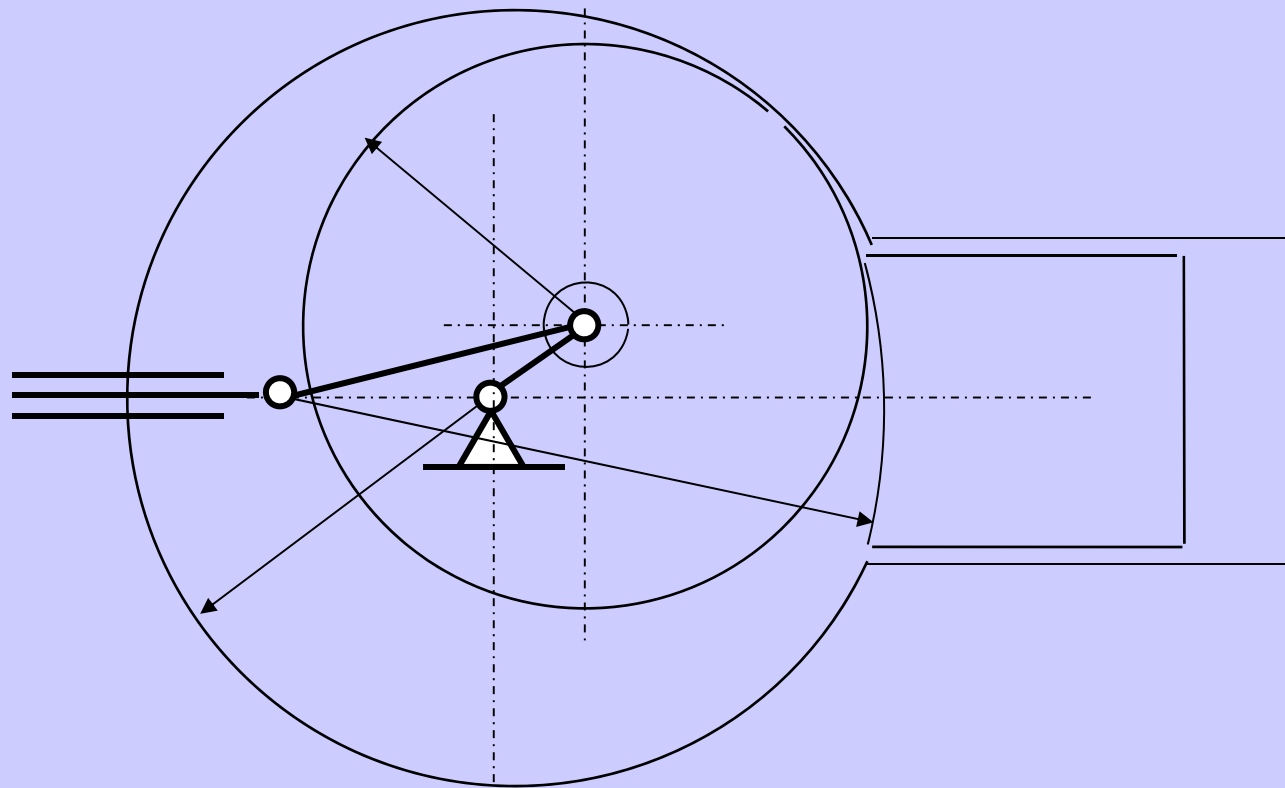
ROTARY VANE COMPRESSOR WITH CONCENTRIC VANES



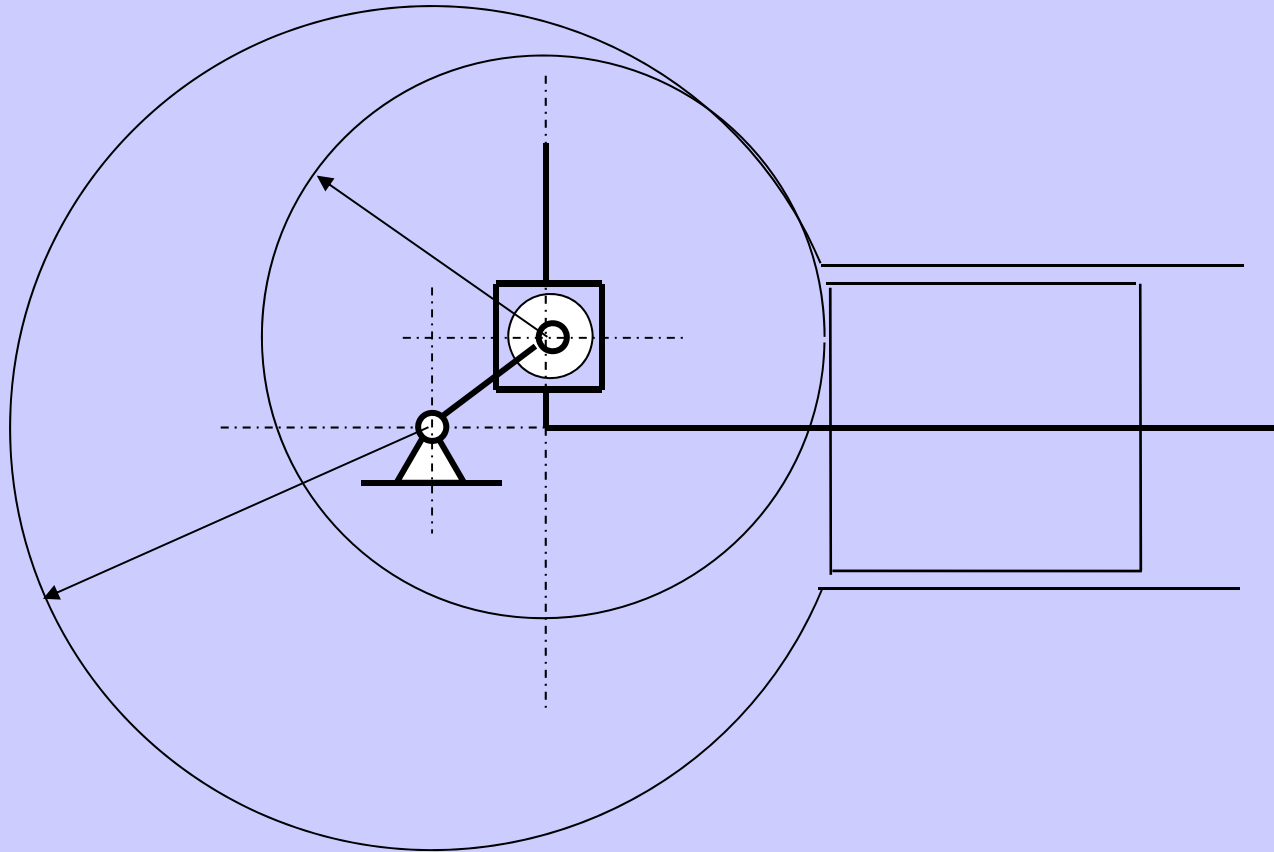
ROLLING PISTON COMPRESSOR



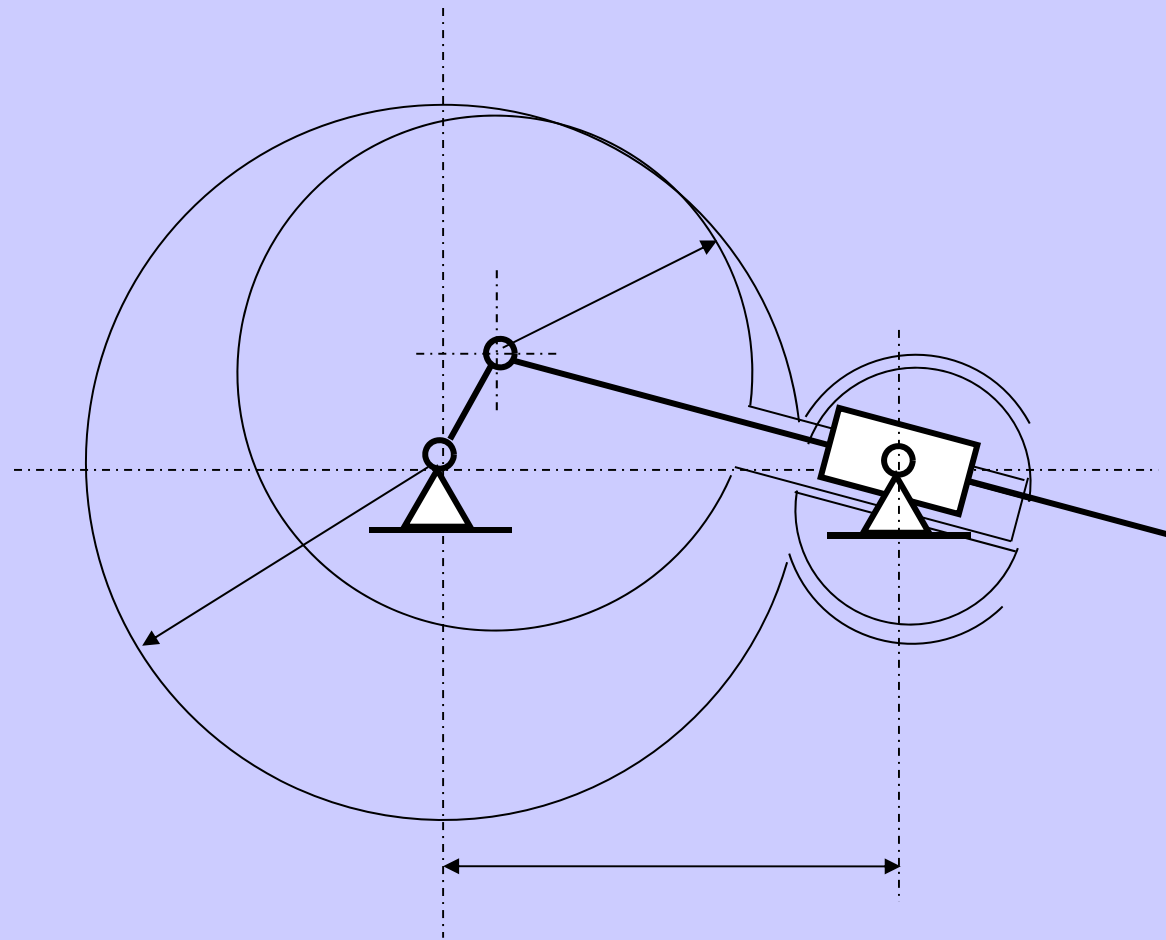
ROLLING PISTON COMPRESSOR



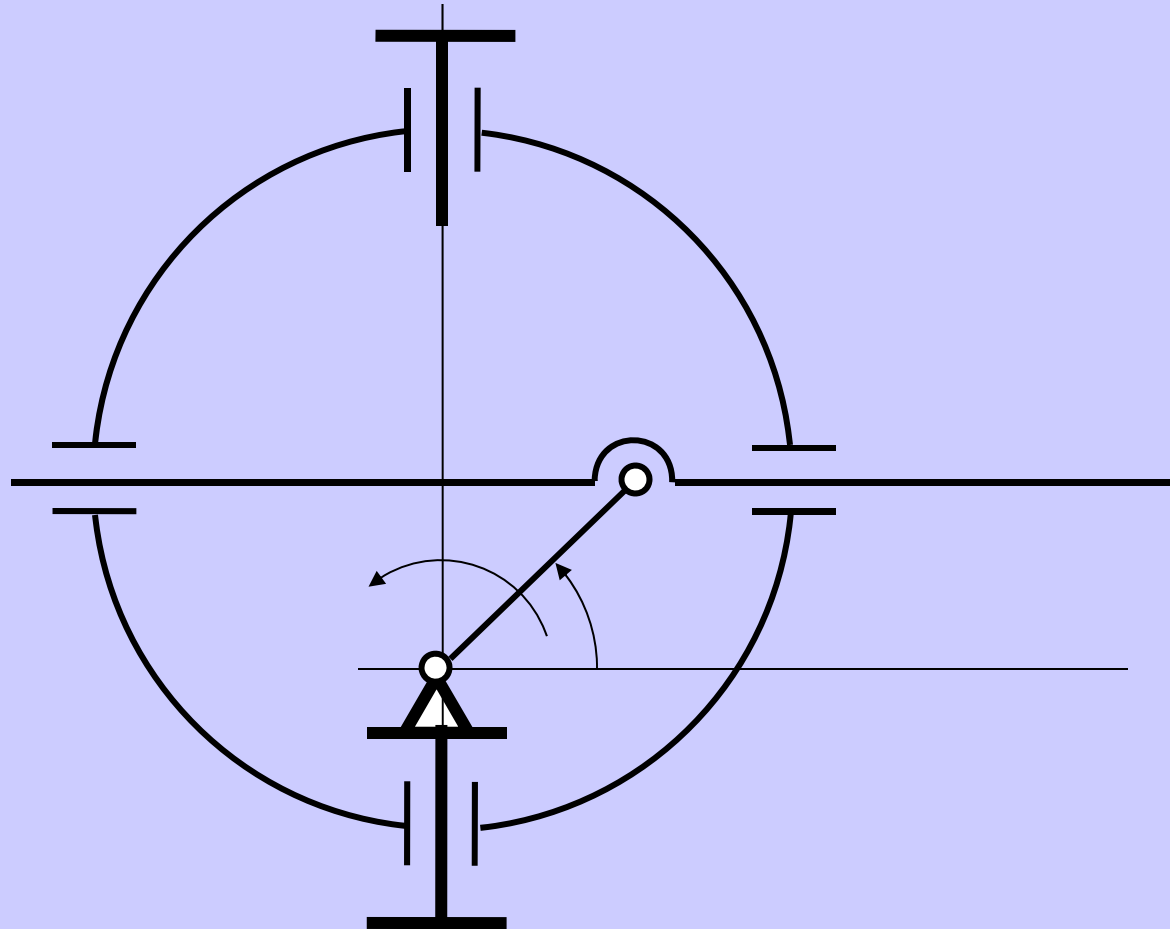
ROLLING PISTON COMPRESSOR



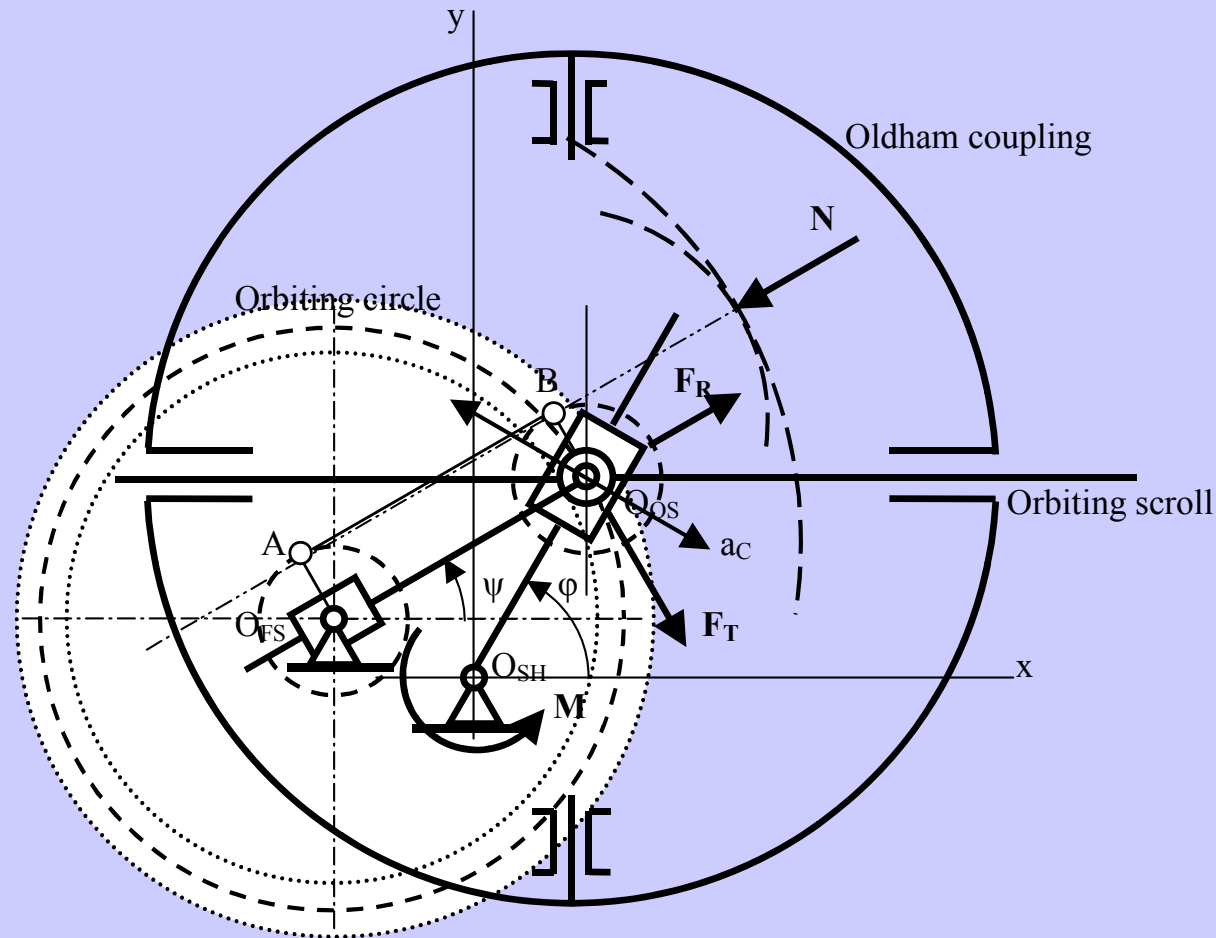
SWING PISTON COMPRESSOR



SCROLL COMPRESSOR WITH FIXED ORBITING RADIUS



RADIALLY COMPLIANT SCROLL COMPRESSOR



22nd International Compressor Engineering Conference at Purdue, July 14-17, 2014

**THANK YOU
FOR YOUR ATENTION**

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