

Model-based Optimal Control of a Building HVAC System

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July 11 -14, 2016



Outline



- Background
- Methodology
- Case Study
- Results and Discussions
- Conclusions and Future work



Background



- The energy demand from the simulation case with the optimized control strategy is 19.5% less than that from the actual building with the non-optimized control strategy in the HVAC system. (Nassif, N., Kajl, S., & Sabourin, R. (2004, June). Evolutionary algorithms for multi-objective optimization in HVAC system control strategy. In *Fuzzy Information, 2004. Processing NAFIPS'04. IEEE Annual Meeting of the* (Vol. 1, pp. 51-56). IEEE.)



Background



- Modeling effort and required computation resource are bottlenecks for on-line implementations of MPC at a large scale.
- Other optimization based control methods utilized customized physics-based models that are complex and not scalable.



Methodology



Modeling

- AHU model

$$Q_{AHU} = \dot{m}_{s,AHU} c_p (T_{s,AHU} - T_{mix})$$

$$T_{mix} = rT_{oat} + (1-r)T_{ra}$$

$$\dot{m}_{s,AHU} = \sum_{i=1}^{N_{vav}} \dot{m}_{vav}^i$$

$$T_{ra} = \frac{\sum_{i=1}^{N_{vav}} (\dot{m}_{vav}^i \cdot T_r^i)}{\sum_{i=1}^{N_{vav}} \dot{m}_{vav}^i}$$



Methodology



Modeling

- Fan model

$$P_{fan} = a_1 \dot{m}_{s,AHU}^3 + a_2 \dot{m}_{s,AHU}^2 + a_3 \dot{m}_{s,AHU} + a_4$$

- VAV box model

$$Q_{reheat}^i = \dot{m}_{vav}^i c_p (T_{s,vav}^i - T_{s,AHU})$$

- Room air thermal response model

$$T_r = a_0 + a_1 \cdot T_{oat} + a_2 \cdot T_{s,vav} \cdot m_{vav}$$



Methodology



Optimization formulation

- Objective

$$\text{Minimize: } Q_{total} = \frac{Q_{AHU}}{\eta} + P_{fan} + \frac{\sum_{i=1}^{N_{vav}} Q_{reheat}^i}{\eta}$$

- Subject to

$$T_r^{\min} \leq T_r^i(t) \leq T_r^{\max}$$

$$T_{s,AHU}^{\min} \leq T_{s,AHU} \leq T_{s,AHU}^{\max}$$

$$\dot{m}_{s,AHU} c_p (T_{s,AHU} - T_{mix}) \leq Q_{capa,AHU}$$

$$\dot{m}_{vav}^i c_p (T_{s,vav}^i - T_{s,AHU}) \leq Q_{capa,reheat}^i$$



Methodology



Modeling Platform and Optimization Solver

- AMPL

A Mathematical Programming Language (AMPL) is an algebraic modeling language to describe and solve high-complexity problems for large-scale mathematical computing (i.e., large-scale optimization and scheduling-type problems).

- IPOPT

IPOPT, short for "Interior Point OPTimizer", is a software library for large scale nonlinear optimization of continuous systems



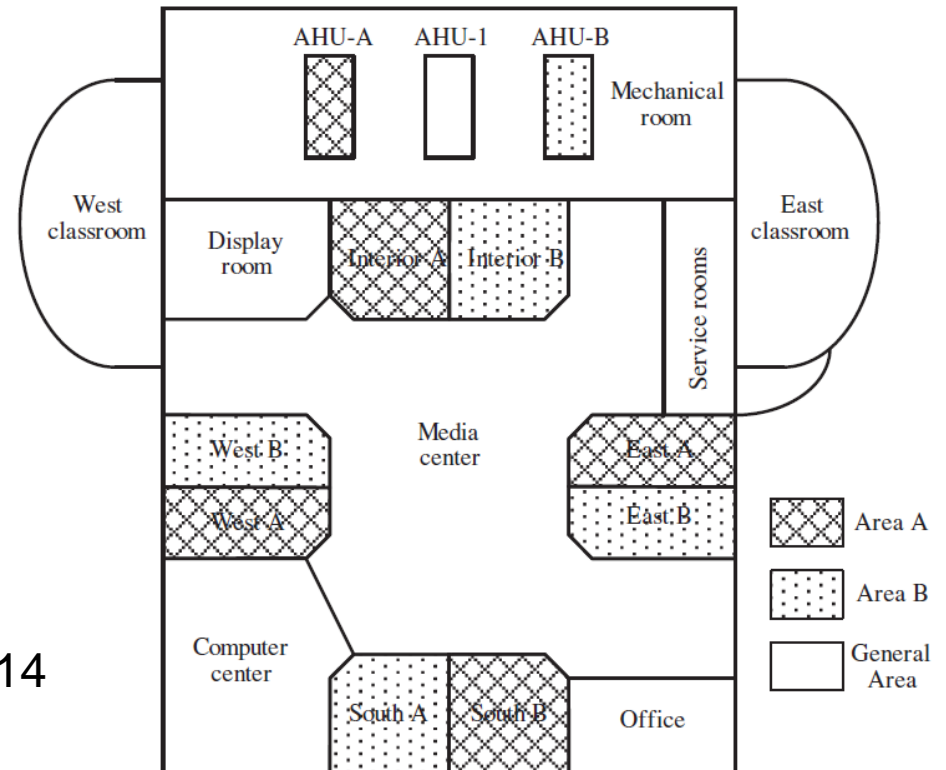
Case Study



HVAC system-Iowa Energy Center

- The HVAC system B is comprised of a central AHU and an overhead ducted air distribution that terminates with four room-level VAV terminal boxes. Each test room is equipped with a pressure-independent, single-duct VAV box. Each VAV box has both a hydronic and an electric reheat coil

Data from Oct 30th 2013 to Jan 30th 2014

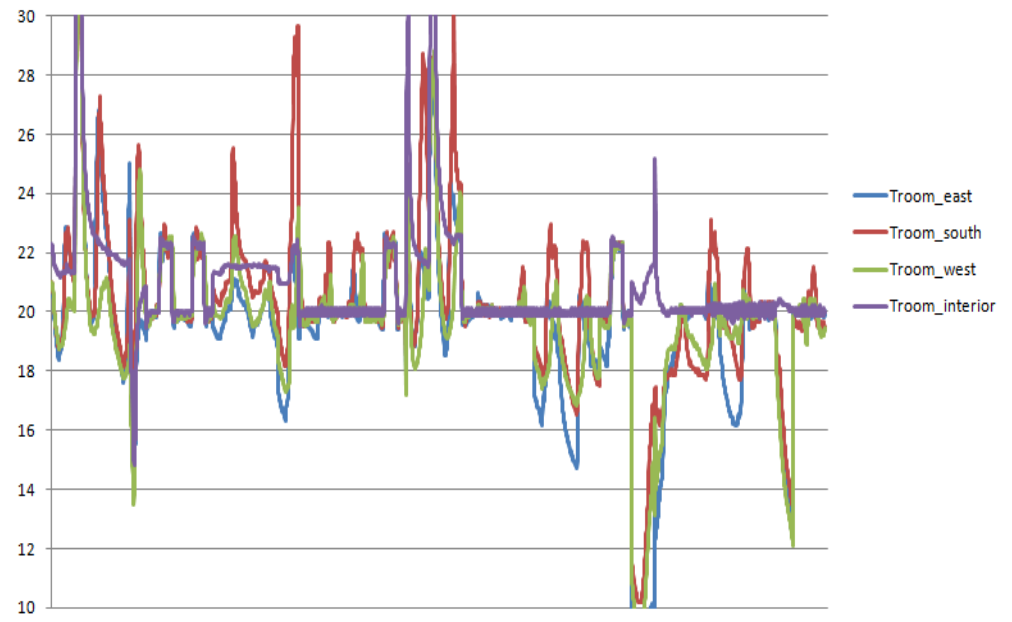
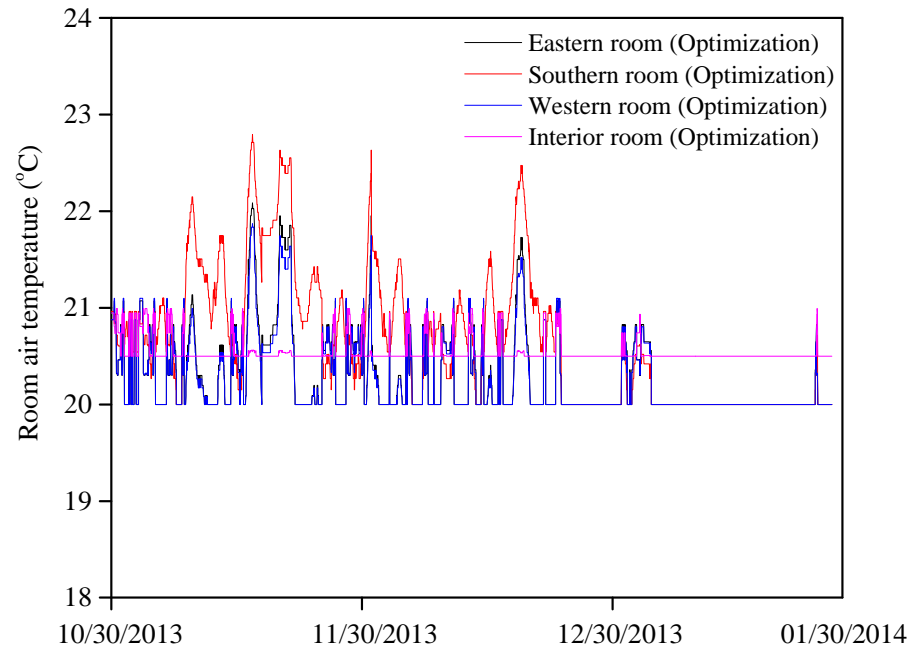




Results and Discussions



Room air temperature

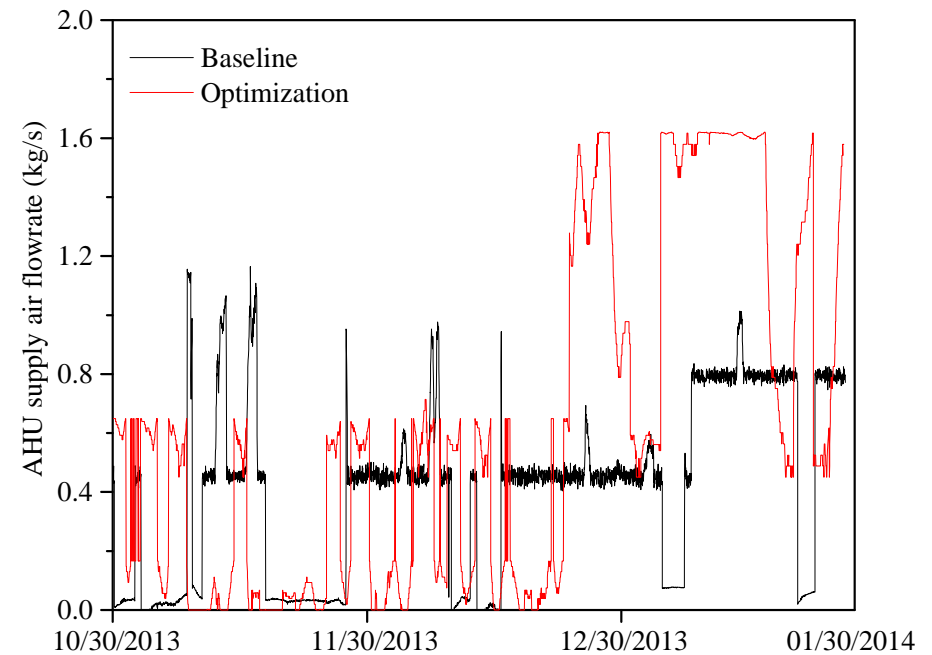
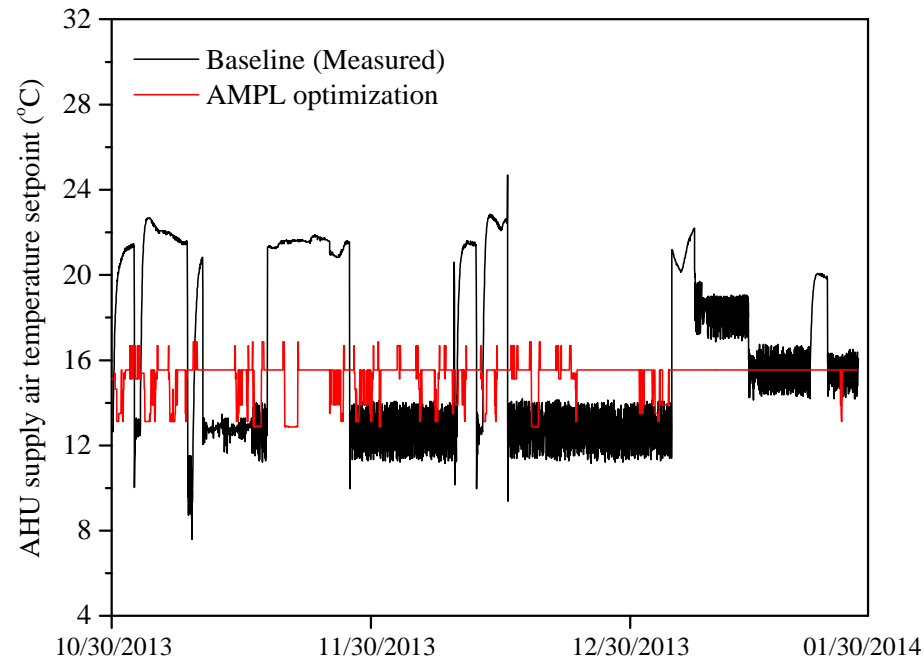




Results and Discussions



AHU supply air temperature and flow rate

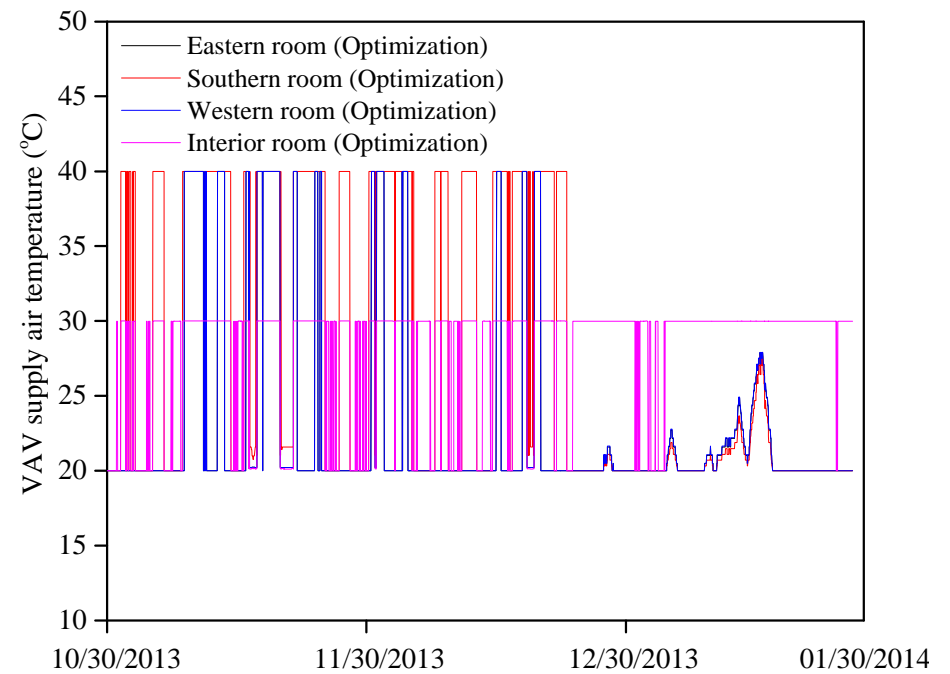
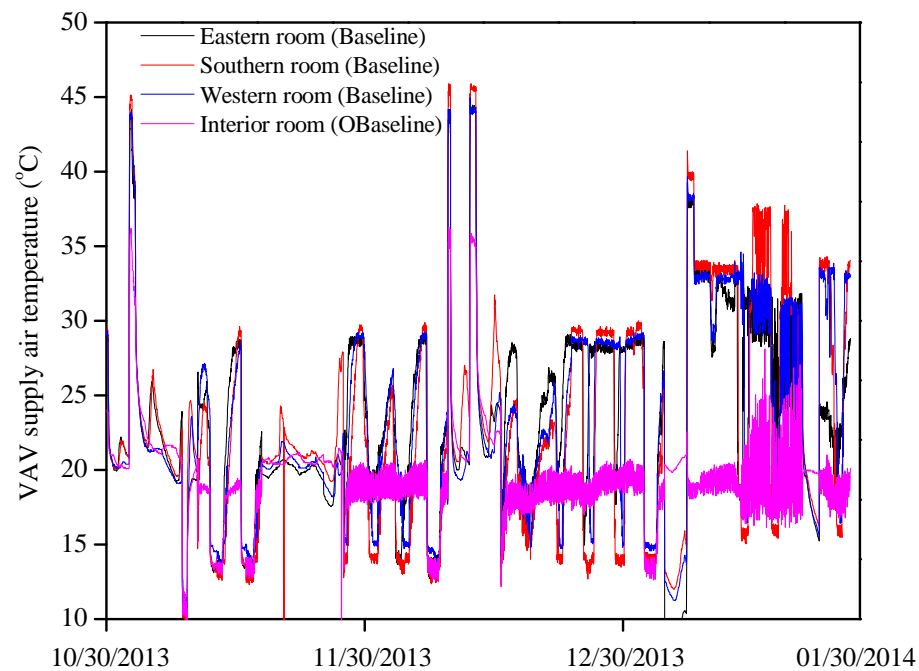




Results and Discussions



VAV supply air temperature

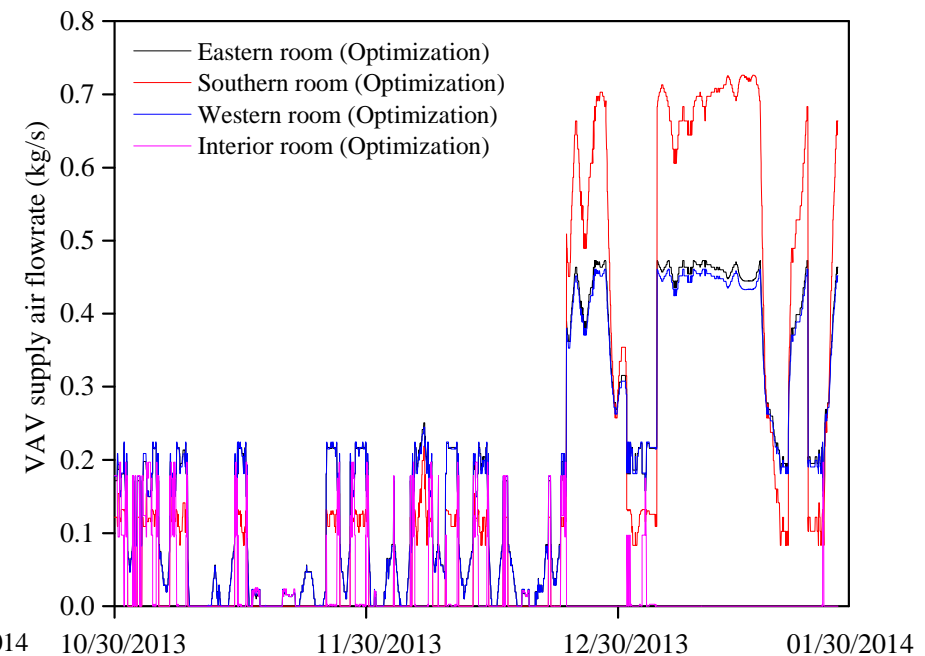
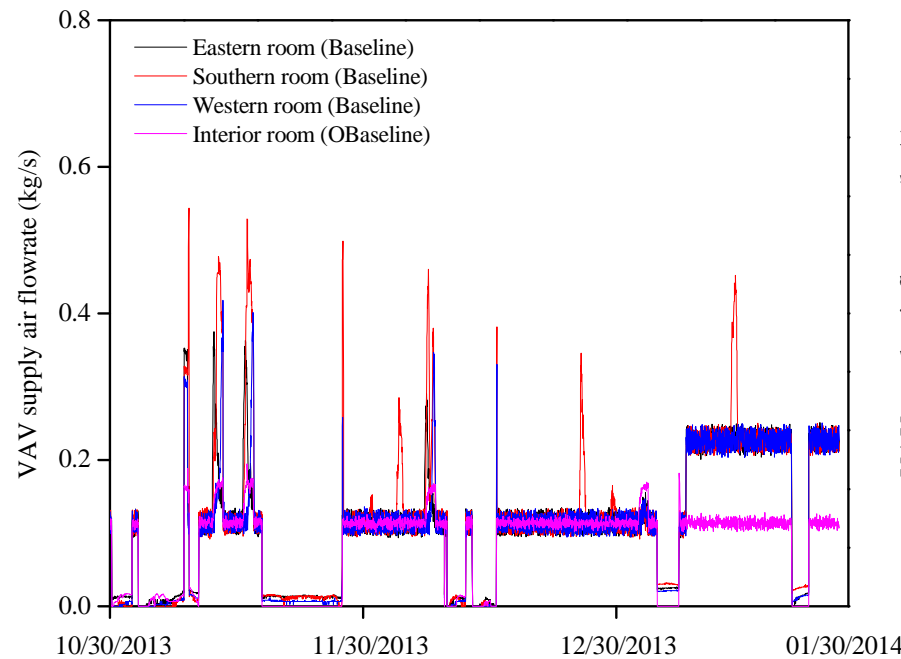




Results and Discussions



VAV supply air flow rate

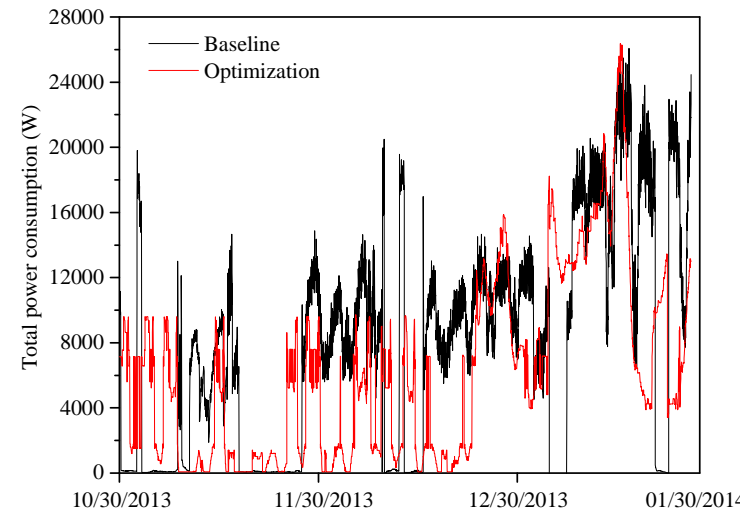
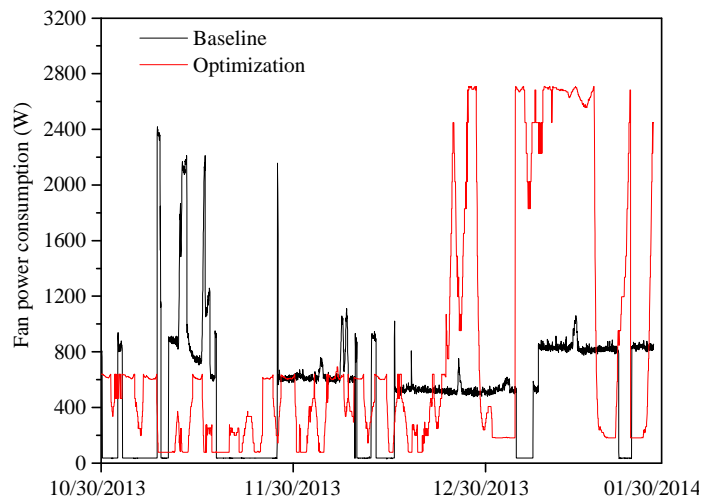
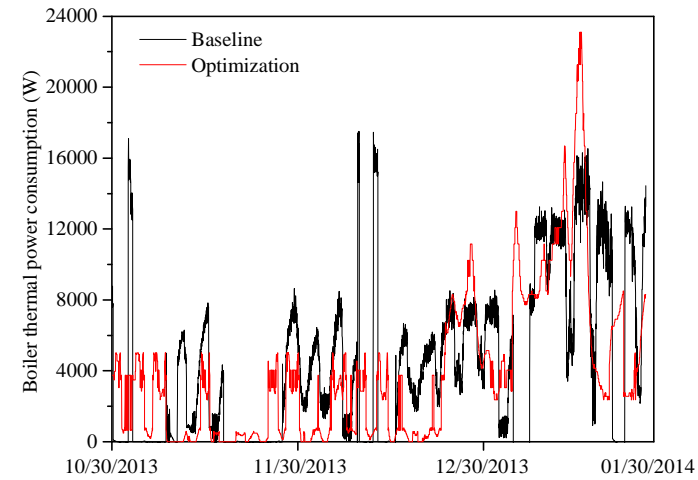
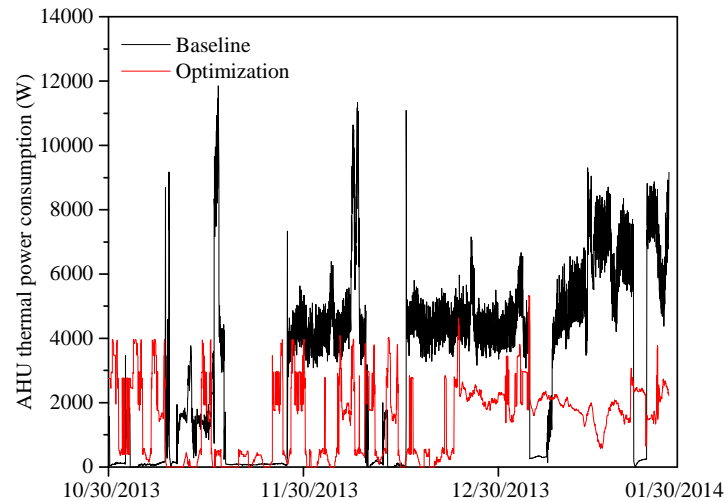




Results and Discussions



Energy consumption

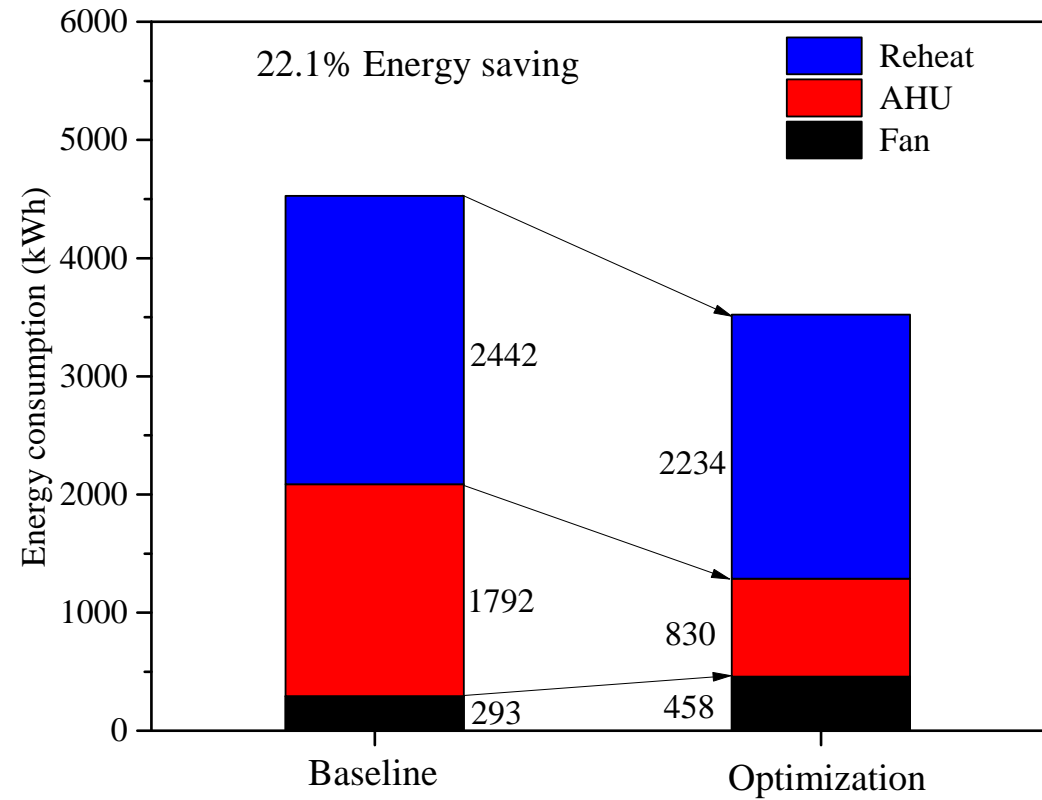




Results and Discussions



Energy consumption





Conclusions and Future work



Conclusions

- The model-based optimal control greatly saves the total energy consumption.
- The room air temperature by the model-based optimal control is more stable.
- The energy saving of model-based optimal control is realized by increasing fan supply air flow rate to reduce the AHU energy consumption and VAV box reheat coil energy consumption.



Conclusions and Future work



Future work

- The data-driven model is based on a fixed historical data set. It is better to use a moving window to incorporate HVAC operation changes.
- Additional optimal control in the cooling mode will be conducted to analyze the annual energy performance.
- Demonstration and implementation of the proposed optimal control in the Building Energy Management System in a real building.



Thanks!

Any questions?

