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UNDERSTANDING VALVE DYNAMICS

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ABSTRACT

The objective of this paper, that deals with modeling dynamics of self-acting compressor valves, is not a creation of a model that produces charts and diagrams that perfectly agree with the experiment. Rather than that, the model is intended to provide understanding and deeper insight into the function of self-acted compressor valves. It also intends to provide input for designers before the compressor is designed and built. The equivalent one-degree-of-freedom system with several types of non-linearity is used. Each valve, suction or discharge, may have unlimited lift, or its lift may have rigid or flexible stop with or without a mass, and with or without a rebound. The friction force and the sticktion force are also considered. Over thirty design-parameters that affect function of each valve can be investigated. A compressible flow of gas through the valve is considered as well as the leakage of gas between the wall of the cylinder and the piston. Friction losses in bearings and due to the motion of the piston are also considered. The function of each valve starts from well-defined initial conditions. This approach enables investigation of individual parameters, and how each of them affects function of the valve, compressor capacity and coefficient of performance. Program is written in Visual Basic for Applications (VBA) as a macro in EXCEL spreadsheet.

MODELS OF SELF-ACTING VALVES

A proper function of compressor valves is essential to compressor performance. The difficulty in valve design arises from the interaction of the flow of compressible gas and a dynamics of a mechanical system, the valve. Both the non-linear thermodynamics and non-linear dynamics of flexible structures are involved. Despite the progress in computational techniques and mathematical modeling, the simplest models still give best result [9]. Thus, a single-degree-of-freedom mechanical system has been chosen to analyze function of compressor valves, case 1 through 5, and two-degree-of-freedom model of case 6 in Figure 1.

A reed valve is most common type of self-acting valve used in refrigeration and air-conditioning positive displacement reciprocating compressors. Some designs also use discus valves that are true single-degree-of-freedom systems. By inspecting available patent literature (too many to list all of them), one can identify several types of equivalent single-degree of freedom models of reed valves. While there are two types of suction reed valves, reed with a lift-limiter (stop) or a reed without a lift-limiter, the designs of discharge valves are more numerous. Figure 1 shows, schematically, six so far identified equivalent models of compressor valves.

Model 1: Is a clamped-free model of a reed valve or a discus valve.

Model 2: Is the model 1 of a reed valve with a stopper. When the reed hits the stop, the model changes to clamped-hinged type of beam, its mass and stiffness suddenly changes, k_1 becomes k_2 and m_1 becomes m_2 .

Model 3: Is a valve with hard sop. The stop may be perfectly soft (coefficient of restitution equal to zero), or perfectly resilient (coefficient of restitution equal to one), or a real stop (with the coefficient of restitution $0 < k < 1$). The sticktion force can also be considered if applicable.

Model 4: Is a valve with mass-less stop. Mass of valve remains unchanged while stiffness suddenly changes from k_1 to $k_1 + k_2$. This model is adequate when, for example, a relatively heavy disc hits much lighter spring.

Model 5: Is a model of the valve that has flexible stop. A rigid frame supports both, the valve and the stop. The mass of the stop is comparable with the mass of the valve. The impact of both the masses can be ideal or real ($1 \geq$ coefficient of restitution ≥ 0), or a sticktion force can exist between the valve and the stop for a short time interval.

Model 6: This model differs from the model 5 in that it has the valve supported by a flexible stop, which mass is comparable with the mass of the valve. The motion of the valve starts as a two-degree-of-freedom system. When the

valve hits the stop it may or it may not rebound ($1 \geq$ coefficient of restitution ≥ 0), or a sticktion force can exist between the valve and the stop for a short time interval. The stop may or may not be pushed against the plate (be preloaded).

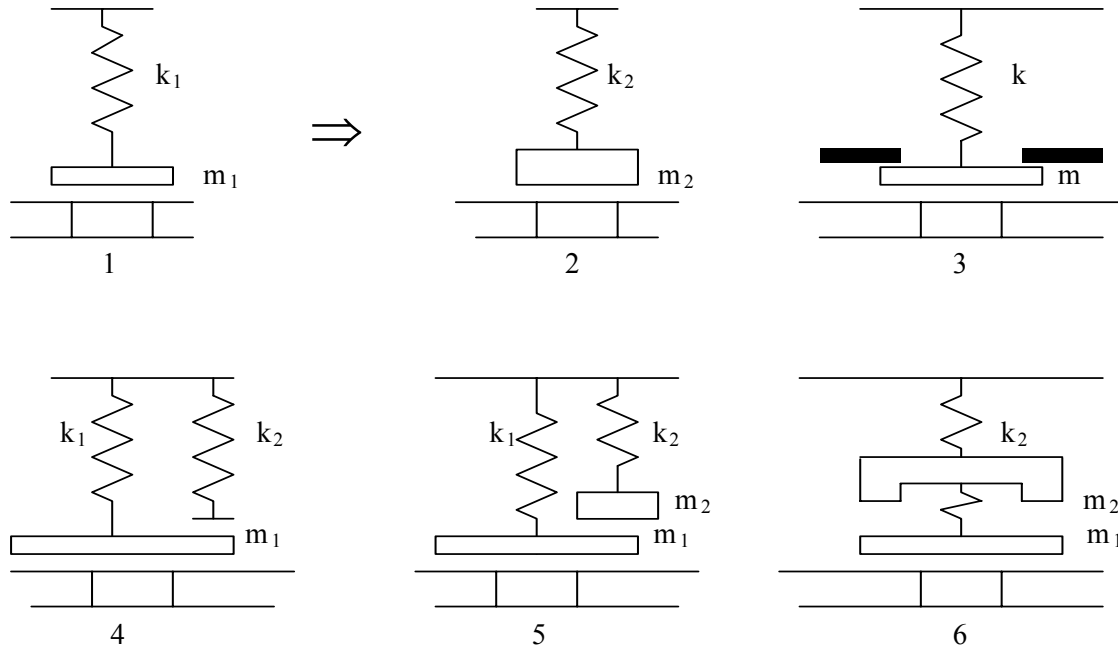


Figure 1: Lumped parameter models of compressor valves.

EQUATION OF MOTION

The equation of motion of the valve and all the other supporting equations are similar to those presented in [2], [3], [4], [8],[9],[10], [11] with some modifications. The space available does not permit detailed derivations.

Except Model 1 the mass and stiffness change abruptly when the valve hits the stop. That means the parameters in the equation of motion are functions of displacement

$$m_v(x_v) \cdot \ddot{x}_v + c_v \cdot \dot{x}_v + k_v(x_v) \cdot x_v = F_{pV} + F_G - F_{\text{Friction}} - F_{\text{Sticktion}} - F_{V\text{-Preload}} \quad (1)$$

$$m_s \cdot \ddot{x}_s + c_s \cdot \dot{x}_s + k_s \cdot (x_s - x_{ST}) = -F_{S\text{-Preload}}$$

Where is:

x	Lift [m]	k	stiffness [N.m ⁻¹]
F _p	force due to pressure differential [N]	m	mass [kg]
F _G	force due to gas flow [N]	c	coefficient of viscous damping [N.s.m ⁻¹]
v,s	index indicating valve or stop	x _{ST}	height of stop [m]

The abrupt changes in the magnitude of mass of the valve and its stiffness that occur when the lift of the valve hits the stop have been already explained. The explanation of the remaining forces follows.

Force of Gas Pressure

The force F_p due to the pressure differential across the valve is

$$F_p = \frac{\pi}{8} \cdot \left[(p_2 - p_1) \cdot d_1^2 + (p_2 + p_1) \cdot d_2^2 \right]; \quad p_2 > p_1 \quad (2)$$

Where is

d ₁	inner diameter of valve seat [m]	p ₂	pressure down the stream [Pa]
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d_2 outer diameter of valve seat [m]

p_1 pressure up the stream [Pa]

Force of Gas Flow

The dynamic force of the gas flow is

$$F_G = C_D \cdot A_p \cdot \rho_p \cdot \frac{w_p^2 - v^2}{2} \quad (3)$$

Where is:

C_D drag coefficient of valve

ρ_p density of gas in the port [$\text{kg}\cdot\text{m}^{-3}$]

A_p area of the valve [m^2]

v velocity of valve [m]

w_p velocity of gas in the port [$\text{m}\cdot\text{s}^{-1}$]

Velocity of gas

The velocity of gas in the port and within the seat is calculated in two steps. First, the velocity of frictionless compressible flow is calculated using [1]

Where p_1 , ρ_1 , and n_1 are the inlet pressure, inlet density, and inlet polytropic exponent respectively, and p_2 and w_2 are outlet pressure and outlet velocity respectively. Pressure loss due to gas friction is [1], [6]

$$w_2 = \sqrt{2 \cdot \frac{n_1}{n_1 - 1} \cdot \frac{p_1}{\rho_1} \left[1 - \left(\frac{p_2}{p_1} \right)^{\frac{n_1}{n_1 - 1}} \right]} \quad (4)$$

$$p_L = \lambda \cdot \frac{L}{d} \cdot \frac{\rho \cdot w^2}{2}; \text{ where } \lambda = \frac{64}{\text{Re}} \text{ for } \text{Re} < 2320; \lambda = \frac{0.3164}{\sqrt[4]{\text{Re}}} \text{ for } \text{Re} > 10^4 \quad (5)$$

$$\lambda = \frac{0.3164}{\sqrt[4]{\text{Re}}} - \frac{64}{\text{Re}} \cdot (\text{Re} - 2320) \quad \text{for } 2320 < \text{Re} < 10^4$$

The Reynolds number Re is

$$\text{Re} = \frac{w \cdot \rho}{\mu} \cdot 2 \cdot x \quad \text{for valve opening}; \quad \text{Re} = \frac{w \cdot \rho}{\mu} \cdot d_p \quad \text{for the port} \quad (6)$$

Where is

d_p diameter of the port [m]

w velocity of gas

The corrected velocity of compressible gas with friction is calculated from [6]

$$w_2 = \sqrt{\frac{2 \cdot \frac{n}{n-1} \cdot \frac{p_1}{\rho_1} \cdot \left[\left(\frac{p_2}{p_1} \right)^{\frac{n}{n-1}} - 1 \right]}{\left(\frac{p_2}{p_1} \right)^{\frac{2}{n}} \cdot \left(\frac{A_2}{A_1} \right)^2 - \left(1 + \sum_i \xi_i + \sum_j \lambda_j \cdot \frac{L_j}{d_j} \right)}} \quad (7)$$

Where is:

ξ_i inlet resistance coefficients of the valve and the port

λ_j friction resistance coefficient of the valve opening and the port

Velocity of gas calculated from equation (4) or (6) is reiterated using equation (5) and (6) one more time. The velocity of gas at the valve outlet can not exceed critical velocity w_c . The gas velocity becomes critical when the pressure ratio r exceeds critical pressure ratio r_c , that is when

$$r_c \geq \left(\frac{p_2}{p_1} \right)_c = \left(\frac{2}{k+1} \right)^{\frac{k}{k-1}}, \quad \text{critical velocity is } w_c = \sqrt{2 \cdot \frac{k}{k+1} \cdot \frac{p_1}{\rho_1}} \quad (8)$$

The velocity of gas in the port and at the valve outlet is different except in the case when the valve lift is $x \geq d_p/4$, where d_p is port diameter. The velocity of gas that strikes the valve is

$$w_v = \frac{A_P}{A_V} \cdot \frac{\rho_P}{\rho_V} \cdot w_P; \quad A_V = \pi \cdot d_2 \cdot x \quad \text{is valve area,} \quad A_P = \frac{\pi \cdot d_p^2}{4} \quad \text{is port area} \quad (9)$$

Cylinder Pressure

Pressure in the cylinder is governed by the expression

$$p_C = p_{C0} \cdot \left(\frac{M_0 + \Delta M}{\rho_{C0} \cdot V_C} \right)^{n_0}; \quad M_0 = A_C \cdot \rho_{C0} \cdot s_0; \quad \Delta M = (A_P \cdot \rho_P \cdot w_P - \dot{M}_{BB}) \cdot \Delta t \quad (10)$$

$$\dot{M}_{BB} = \beta_B \cdot \left(\frac{\pi \cdot (D_C - D_P)^3 \cdot (D_C + D_P) \cdot (p_C - p_S)}{96 \cdot \mu_{C \text{ or } S} \cdot L_P} + \frac{(D_C - D_P) \cdot L_P \cdot v_P}{2} \right) \cdot \rho_{C \text{ or } S} \quad (11)$$

Where is:

M_0	initial mass of gas in the cylinder [kg]	L_P	length of piston [m]
\dot{M}_{BB}	blow-by mass flow rate [$\text{kg} \cdot \text{s}^{-1}$]	v_P	piston velocity [$\text{m} \cdot \text{s}^{-1}$]
Δt	is time interval [s]	$\rho_{C \text{ or } S}$	gas density [$\text{kg} \cdot \text{m}^{-3}$]
β_B	blow bay coefficient	$\mu_{C \text{ or } S}$	dynamic gas viscosity [Pa.s]
D_C	cylinder diameter [m]	p_S	suction pressure [Pa]
D_P	piston diameter [m]	p_C	cylinder pressure [Pa].

In equation (10) and (11), index C means cylinder, index 0 means initial state of gas in the cylinder; index P means port, and \dot{M}_{BB} is mass flow rate of gas that escapes from the cylinder (during compression), or enters the cylinder (during suction) through the gap between the piston and the wall of the cylinder. The blow by coefficient is the decimal fraction of piston circumference open to the gas flow [5].

Density of gas in the cylinder is calculated from

$$\rho_C = \rho_{C0} \cdot \left(\frac{p_C}{p_{C0}} \right)^{\frac{1}{n_0}} \quad (12)$$

Where

ρ_{C0}	is initial density of gas in the cylinder [$\text{kg} \cdot \text{m}^{-3}$]
p_{C0}	is initial pressure of gas in the cylinder [Pa]

Friction Force

The design of discharge valve considered in this paper has spring that has free shape close to the arc of a circle. When the valve opens, the arc is stretched and the ends of the spring rub against the frame. Using principle of virtual work, the friction force is derived as

$$F_{\text{Friction}} = F_F = v \cdot k \cdot [h - (x_0 + x)] \cdot \frac{8}{3} \cdot \sqrt{\frac{3 \cdot [h - (x_0 + x)]^2}{3 \cdot L^2 - 16 \cdot [h - (x_0 + x)]^2}} \quad (13)$$

Where is:

F_F	friction force [N]	h	height of arc of unloaded spring [m]
v	coefficient of friction	x_0	initial compression of spring [m]
k	linear spring constant [$\text{N} \cdot \text{m}^{-1}$]	x	valve lift [m].
L	length of the arc of unloaded spring [m]		

Sticktion force

The magnitude of sticktion force depends on the geometry of the valve seat and the geometry of the oil film. There is two possible geometry of the valve seat. The first one is a flat valve approaching (or separating from) a flat seat that is parallel with the valve. The second one is a flat valve that approaches (or separates from) a parallel valve seat that has a doughnut shape cross-section. One needs to consider the difference between the force of approach and the force of separation because the initial thickness of oil film for the valve separation depends on the force that pushes

the valve against the seat. The sticktion force of approach starts when the valve that is approaching the valve seat touches the surface of the oil film. The oil is pushed out of the valve gap. On the other hand, when the valve starts to separate from the valve seat oil has to flow into the opening gap. Two situations can happen. The oil film is relatively thick, and there is enough oil flowing into the valve gap; the force of separation will be the same as the force of approach. Or, the oil film is relatively thin, and the quantity of oil in the valve gap remains constant during the valve separation (oil starved gap) the force of separation is different from the force of approach. It is assumed the thickness of oil film on the seat and on the valve is the same, and that both together constitute the total thickness of oil film when the valve goes into the contact with the seat or the stop.

Sticktion Force of Approach - Flat Seat - Oil-Filled Gap

When flat plate approaches parallel an annular valve seat, and both are covered with oil film, the squeeze film force is [7]

$$F_S = F_A = C \cdot \frac{v}{x^3}; \quad C = \frac{3 \cdot \pi \cdot \mu \cdot (d_2^2 - d_1^2)}{32} \cdot \left(1 - \frac{d_2^2 - d_1^2}{(d_2^2 + d_1^2) \cdot (\ln d_2 - \ln d_1)} \right) \quad (14)$$

Where is

F_S	sticktion force [N]	d_1	inner diameter of seat [m]
d_2	outer diameter of seat [m]	μ	viscosity of oil [Pa.s]

Sticktion force of approach is inversely proportional to the third power of instantaneous thickness of oil film.

Sticktion Force of Separation - Flat Seat - Oil-Filled Gap

In this case, the sticktion force of separation is the same as the force of approach. Equation (14) applies.

Sticktion Force of Separation - Flat Seat - Oil-Starved Gap

This is the case of raised seat with a recess on both sides of the seat or a seat with trepan.

$$F_S = C \cdot \frac{v}{x^3}; \quad C = \frac{3 \cdot \pi \cdot \mu \cdot (r_B^4 - r_A^4)}{2} \cdot \left(\frac{r_B^2 - r_A^2}{(r_B^2 + r_A^2) \cdot (\ln r_B - \ln r_A)} - 1 \right)$$

$$r_A = \frac{d_1}{4} \cdot \left(1 + \frac{x_0}{x} \right) + \frac{d_2}{4} \cdot \left(1 - \frac{x_0}{x} \right); \quad r_B = \frac{d_1}{4} \cdot \left(1 - \frac{x_0}{x} \right) + \frac{d_2}{4} \cdot \left(1 + \frac{x_0}{x} \right) \quad (15)$$

Where

x	thickness of oil film [m]	x_0	initial thickness of oil film [m]
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By inspecting equation (15), one can see, the force of separation is inversely proportional to the seventh power of instantaneous thickness of oil film.

Sticktion Force - Doughnut Shaped Seat

In this case, there is a little difference, that can neglected, between the oil-filled and oil-starved gap because the oil film on the seat follows the curvature of the seat. The sticktion force of approach is the same as the sticktion force of separation

$$F_S = C \cdot \frac{v}{\sqrt{x^3}}; \quad C = 3 \cdot \sqrt{2} \cdot \pi^2 \cdot \mu \cdot \sqrt{r_s^3} \cdot D_s \quad (16)$$

Where

D_s	is diameter of contact circle [m]	r_s	radius of seat [m]
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Valve pre-load

Frequently, valves are assembled, intentionally or because of tolerance chaining, so that the valve is pushed against its seat. It is believed that this force helps to improve sealing and prevents rebound of the valve from its seat. On the other hand it also delays valve opening that results in bigger spike on the cylinder pressure. In any case, the impact of this force on the function of the valve has to be taken into consideration.

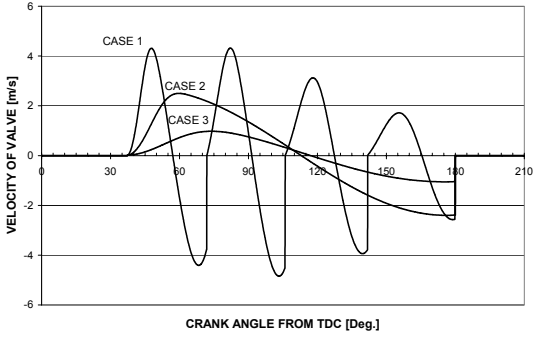


Figure 4: Velocity of valve

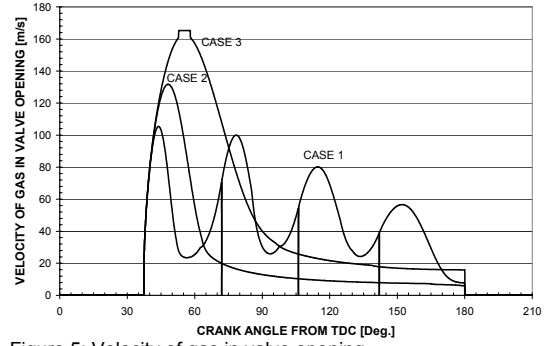


Figure 5: Velocity of gas in valve opening

respectively on the three cases of model 1 from Figure 1. Case number one is a valve close to the real design. Its frequency is 390 Hz and static stiffness is 510 N/m. Case number two is a lighter valve that has frequency of 82 Hz and static stiffness 133 N/m. Case number three is heavier valve with frequency of 87 Hz and static stiffness 900 N/m. In all the three cases valve closes at the BDC, and the quantity of gas that enters the cylinder is the same. Thus, the capacity of the compressor with any of those three valves will be same. The difference will be in the compressor noise due to differences in the mass of the valve and the velocity, magnitude and frequency content of pressure pulsation, and velocity of gas within the valve seat.

Figures 6 and 7 show the impact of oil on the valve lift and cylinder pressure. Presence of oil on the valve seat increases lift and pressure drop. Delayed valve opening and delayed valve closing decreased volumetric efficiency by 7.6 %.

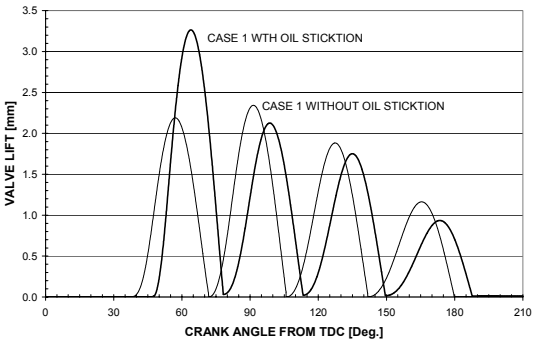


Figure 6: Effect of oil on valve lift

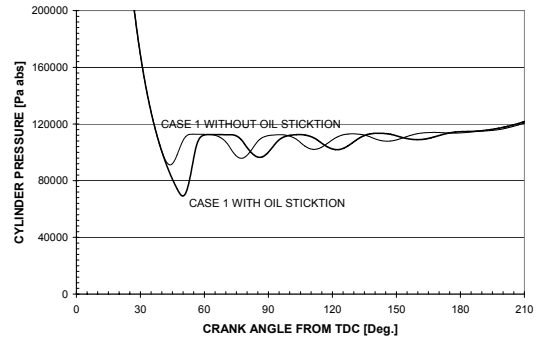


Figure 7: Effect of oil on cylinder pressure

Figure 8 shows effect of flexible stop on valve closing, and Figure 9 shows effect of oil and valve rebound on valve closing.

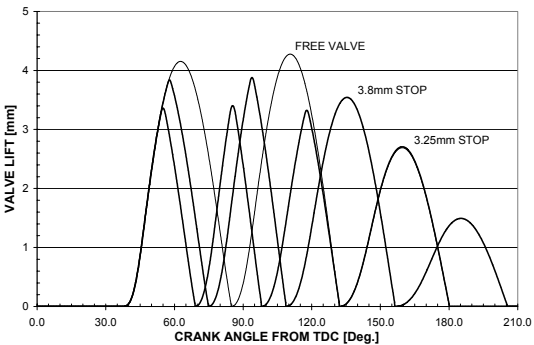


Figure 8: Effect of flexible stop on valve closing

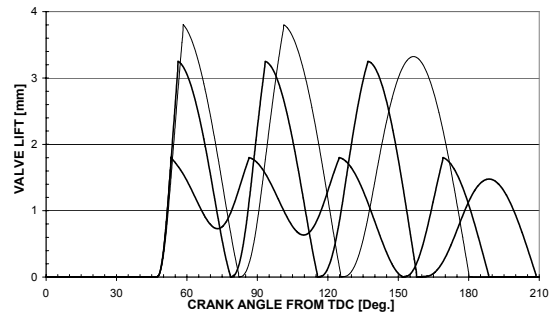


Figure 9: Effect of hard stop, oil and valve rebound on valve closing

MODELING DISCHARGE VALVE

The model of discharge valve (DVD) starts from at bottom dead center, and it assumes the cylinder is fully filled with the gas that has pressure and temperature equal to those in the suction plenum. Altogether, thirty-two parameters have an impact on discharge valve opening and closing, capacity of the compressor, its COP, and the noise of the compressor. This is too many to show in this paper. Some of them have smaller, some of them greater effect on the compressor's capacity, COP, and noise. Some combinations of parameters are more beneficial than the other ones. Three representative valves are shown in Figures 10 through 17.

The natural frequency of the valve is 1157 Hz, static stiffness is 3700 N/m, and the fraction of critical damping is 0.05. The natural frequency of soft stop is 318 Hz, static stiffness is 20kN/m, and the fraction of critical damping is 0.05. The height of stop is 1 mm. The dry friction of the valve spring has relatively small effect, unless the coefficient of friction is considered unrealistically high, say 0.5 or more.

Figure 10 and 11 show almost negligible difference between hard stop and soft stop without oil on the valve lift and cylinder pressure. In addition, the capacity of the compressor and COP were the same.

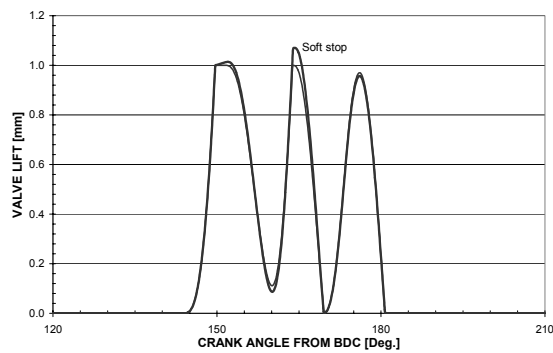


Figure 10: Valve lift with hard or soft stop

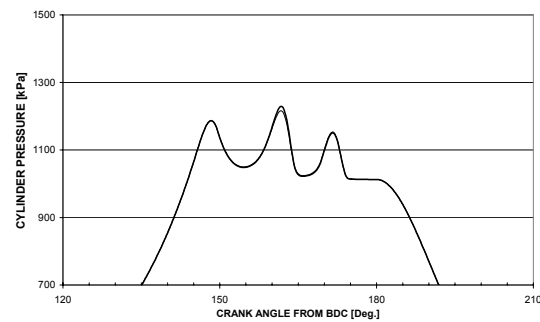


Figure 11: Effect of hard stop and soft stop on cylinder pressure

Figure 12 and 13 show impact of valve rebound (30% energy recuperation) on the valve lift of the same valve as in Figure 11 and 12. While the rebound from the stop has negligible impact on capacity, COP and cylinder pressure, the rebound from the seat decreases compressor's capacity by 2.5% due to the flow-back of the gas.

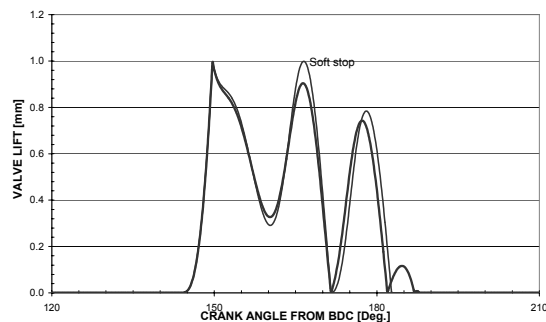


Figure 12: Valve lift - hard stop or soft stop with 30% energy reflection

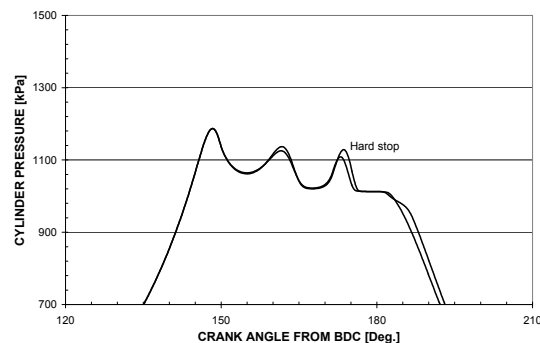


Figure 13: Effect of 30% energy reflection on cylinder pressure

Figure 14 and 15 show impact of oil on the valve with hard or soft stop. While oil sticktion degraded capacity by 4.7%, COP by 4.3 %, and increased cylinder pressure by 216 kPa of the compressor with hard stop, the impact of oil sticktion with soft stop was slightly positive. Figure 16 and 17 shows that two valves with different natural frequencies may be designed to work properly on the same compressor. This contradicts traditional thought that only one valve with a unique frequency can work properly. In this case, the natural frequency of the second valve is 686 Hz and static stiffness 1300 N/m. Natural frequency of the stop is the same as in previous cases, as well as the height of stop. The effect of oil is negative resulting in 1.7-% drop in capacity. Due to much smaller stiffness of valve, the oil sticktion has greater effect on the motion of the valve.

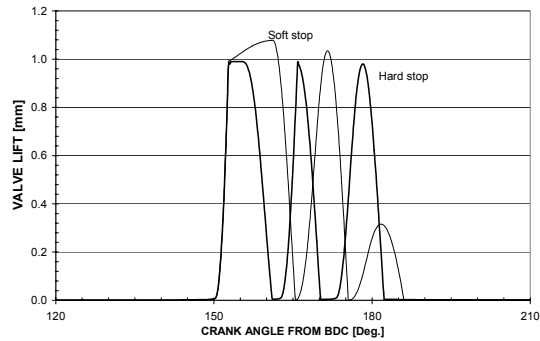


Figure 14: Effect of oil on hard and soft stop



Figure 15: Effect of oil on hard and soft stop

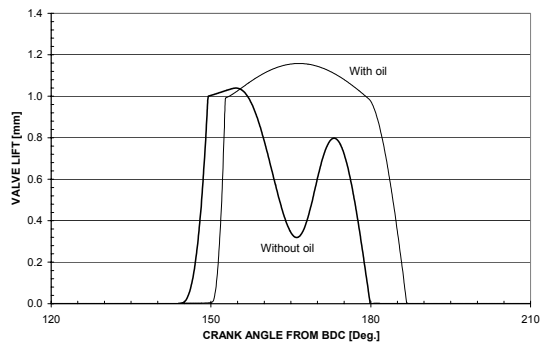


Figure 16: Softer valve with soft stop and with/without oil

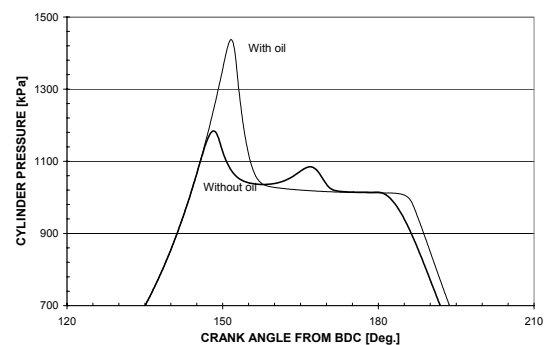


Figure 17: Softer valve with soft stop and with/without oil

CONCLUSION

The valve dynamics software SVD and DVD proved to be an efficient tool that helps to understand behavior of self-acting compressor valves, and how numerous parameters affect capacity, COP and noise of the compressor. The impact of some of valve design parameters on capacity, COP, and noise of the compressor has been positively identified and practically verified.

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