2002

A Case for Multi-key Secure Video Proxy: Theory, Design and Implementation

Siu F. Yeung
John C.S. Lui
David K.Y. Yau

Purdue University, yau@cs.purdue.edu

Report Number:
02-011

https://docs.lib.purdue.edu/cstech/1529

This document has been made available through Purdue e-Pubs, a service of the Purdue University Libraries. Please contact epubs@purdue.edu for additional information.
A CASE FOR A MULTI-KEY SECURE VIDEO PROXY: THEORY DESIGN AND IMPLEMENTATION

Siu F. Yeung
John C.S. Lui
David K.Y. Yau

CSD TR #02-011
June 2002
A Case for a Multi-Key Secure Video Proxy: Theory, Design, and Implementation

Siu F. Yeung
Department of Computer Science & Engineering
The Chinese University of Hong Kong
sfyeung@cse.cuhk.edu.hk

John C. S. Lui*
Department of Computer Science & Engineering
The Chinese University of Hong Kong
cslui@cse.cuhk.edu.hk

David K. Y. Yau†
Department of Computer Sciences
Purdue University
West Lafayette, IN 47907
yau@cs.purdue.edu

ABSTRACT
Because of limited server and network capacities in multimedia streaming, proxies are commonly used to cache multimedia objects such that, by accessing nearby proxies, clients can enjoy smaller start-up latencies and reduced packet loss and delay jitters for their requests. However, the use of video proxies increases the risk that multimedia data are exposed to unauthorized access by intruders. In this paper, we present a framework for implementing a secure video proxy or, more generally, a secure proxy architecture. The framework employs a notion of asymmetric reversible parametric sequences to provide the following security properties: (1) data confidentiality during transmission, (2) end-to-end data confidentiality, (3) data confidentiality against proxy intruders, and (4) data confidentiality against member collusion. Our framework is grounded on a multi-key RSA technique such that system resilience against attacks is provably strong given standard computability assumptions. We also propose the use of a set of encryption configuration parameters to trade off proxy encryption throughput against the viewing quality of video by unauthorized parties. Implementation results on a Pentium III/800 MHz machine show that our techniques can simultaneously achieve high encryption throughput and extremely low video quality (in terms of both PSNR and the visual quality of decoded frames) during unauthorized viewing.

Keywords
Security, Asymmetric Parametric Sequence Functions, Multi-Key RSA, Video Proxy

1. INTRODUCTION
The emergence of the Internet as a pervasive form of communication, as well as advances in digital video and compression technologies, has led to the recent wide deployment of continuous media streaming over the network. A wide range of applications such as video-on-demand, distance learning, and corporate telecasts and narrowcasts are now enabled by the ability to stream video/audio data from servers to clients across a wide area. However, because of the high bandwidth requirement (e.g., a high quality video stream usually has a bandwidth requirement of over 1 Mb/s) and the long duration nature (e.g., from tens of minutes to several hours) of digital video, server and network bandwidths are major limiting factors in achieving a scalable streaming service. Consequently, there has been a lot of research on developing techniques for bandwidth-efficient distribution of multimedia data to a large client population. One common solution, for example, is to use a multimedia proxy to perform some form of data caching (say, prefix caching), so that clients can access the cached video from their nearby proxies to minimize delay and conserve bandwidth.

One major problem with the multimedia proxy approach is the risk of revealing the original video data to unauthorized parties. For example, when the original data are sent from server to proxy, anyone that eavesdrops on the communication link between the source and the proxy can gain access to the video information. Some "naive" approaches to counter the problem are:

- **Encryption using a secret key between the server and the proxy:** Under this approach, the server and the proxy will exchange a secret key $\lambda'$ for encrypting the video data. The source encrypts the data based on $\lambda'$ and sends the encrypted data to the proxy. The proxy, upon receiving the encrypted data, can perform decryption and cache the video data in clear form. There are several problems with this approach, including:

  - **Data insecurity at the proxy:** Since the cached...
data at the proxy are the original multimedia data, any intruder who gains access to the proxy’s storage can access the original data.

- **Data insecurity between the proxy and clients:** Since the data transfer between the proxy and its clients can be over an insecure channel, one can eavesdrop on this channel and gain access to the original multimedia data.

- **End-to-end encryption using a secret key between the server, the proxy and the clients:** Under this approach, the server, the proxy and all the clients behind the multimedia proxy will share a common secret key $X$. The source encrypts the data based on $X$ and sends the data to the multimedia proxy. The proxy, upon receiving the encrypted data, caches the data in its local storage. Whenever a client wants to access the multimedia data, the encrypted copy will be sent to that client. Since the client also knows the secret key, it can decrypt and extract the original data. An intruder can still eavesdrop on the communication link between the proxy and the client, but it will not be able to decrypt the data. The major problem with this approach is that there is a high risk of revealing the secret key $X$. The reason is that a proxy needs to support a large number of clients, and if any of these clients is compromised, an intruder can use the revealed secret key $X$ to gain access to the original multimedia data.

- **Heterogeneous secret keys between the server-proxy pair and the proxy-client pairs:** Under this approach, the server encrypts the data based on a common secret key $X$ that is shared between the server and the proxy only. Upon receiving the data, the proxy caches the encrypted data. Whenever a client, say $i$, wants to access the multimedia data, the proxy will (1) decrypt the data based on the secret key $X$, (2) encrypt the data based on a common secret key $X_i$ between the proxy and the client $i$. The client $i$, upon receiving the encrypted data, can gain access to the original data because it knows the common secret key $X_i$. The potential problem with this approach is that it requires high computational overhead at the proxy, because the proxy needs to perform decryption and encryption for every admitted client. This can limit the number of concurrent clients that the proxy can support.

In this paper, we present a proxy encryption framework having the following properties:

- The multimedia proxy will only cache encrypted video data and data decryption will only happen at the endpoints (e.g., the clients). Therefore, the original video data will not be revealed at any intermediate node.
- The multimedia proxy will perform encryption operations only (i.e., it performs no decryption at all); this reduces the computational overhead at the proxy, and hence allows to support a higher number of concurrent clients.
- Data encryption and decryption operations are based on well accepted encryption theory that it is computationally infeasible to extract the original multimedia data without knowledge of the expected decryption key.
- **Membership collusion** is avoided, such that given (1) the decryption key of client $i$, (2) the encrypted data of client $j$, and (3) possibly all the encryption keys, one still cannot derive the original video data.

The rest of the paper is organized as follows. In Section 2, we present multi-key encryption based on the asymmetric reversible parametric sequence. We then present an efficient algorithm to implement the asymmetric reversible parametric sequences such that the proxy server will have the claimed properties. In Section 3, we present the architecture of our video proxy and the communication protocols between the (1) the proxy and the server, and (2) the clients and the proxy. In Section 4, we report experiments to illustrate the encryption data rate achievable on a commodity Pentium machine, and give quantitative and qualitative analyses of the encrypted video quality. Related work in multimedia proxies is presented in Section 5. Section 6 concludes.

2. MULTIPLE KEY ENCRYPTION THEORY

In this section, we state the theory behind the design of a multi-key secure video proxy. The main theory is based on the reversible parametric sequence (RPS) [5]. We first present the formal definition of RPS and its utilities. We then present an implementation of RPS using the multi-key RSA technique.

2.1 Reversible Parametric Sequence

Let $f : IN^2 \rightarrow IN$ be a function which has the following property: if $Y = f(X,e)$, it is computationally infeasible to find $e$ given that we know $X$ and $Y$.

Assume that we have a finite sequence $\{e_0, e_1, \ldots, e_N\}$ of $N+1$ elements. (Elements in this sequence do not need to be unique.) Define a finite data transformation sequence

$$D = \{D_0, D_1, \ldots, D_N\}$$

based on the function $f$ and the finite sequence $\{e_i\}_{0 \leq i \leq N}$ such that

- $D_0 = \text{original data}$
- $D_i = f(D_{i-1}, e_i)$ for $0 \leq i \leq N$.

We have the following definitions of reversible parametric sequences.

**Definition 1.** $D$ is a reversible parametric sequence of the function $f$, denoted as $\text{RPS}_f$, if for all $(X, Y) \in \text{IN}^2$ and $-1 \leq i < j \leq N$, there exists a computable function $\Omega_{i,j}$ such that

$$D_i = \Omega_{i,j}(D_j) \text{ for } -1 \leq i < j \leq N.$$

**Definition 2.** A $\text{RPS}_f$ is called a symmetric reversible parametric sequence of $f$, denoted as $\text{SRPS}_f$, if the function
Two sequences in Figure 2. The proxy can request to obtain the sequence encrypted data if given the data to implement a secure video proxy.

Figure 1: A graphical representation of two $RPS_j$ sequences.

Video Proxy

Source

$D_1$ $D_2$ $D_3$ $D_4$ $D_5$

$e_1$ $e_2$ $e_3$ $e_4$ $e_5$

$D_0$

$D_0'$

$e_1'$ $e_2'$ $e_3'$ $e_4'$ $e_5'$

Figure 2: A graphical representation of an $ARPS_j$ sequence for the secure video proxy.

$\Omega_{i,j}$ can be computed from the knowledge of the sub-sequence \{e$_{i+1}$, \ldots, e$_j$\}.

Definition 3. A $RPS_j$ is called an asymmetric reversible parametric sequence of $j$, denoted as $ARPS_j$, if it is computationally infeasible to determine the function $\Omega_{i,j}$ based on the knowledge of the sub-sequence \{e$_{i+1}$, \ldots, e$_j$\}.

To understand this concept, we use a graph to represent a reversible parametric sequence $RPS_j$. Figure 1 illustrates two $RPS_j$ sequences. In the figure, the original data $D_{-1}$ are transformed to $D_0$ (or $D_0'$) using $D_0 = f(D_0', e_0)$. If $e_i \neq e_i'$, then the intermediate data $D_i$ will not be equal to $D_i'$, for $1 \leq i \leq N$. For a symmetric reversible parametric sequence $SRPS_j$, one can compute the original data $D_{-1}$ if given the data $D_j$ (or $D_j'$) and the sequence \{e$_0$, \ldots, e$_j$\} (or \{e$_0'$, \ldots, e$_j'$\}), for $0 \leq j \leq N$. In other words, given the information \{e$_0$, \ldots, e$_j$\} and $D_j$, one can construct a decryption function $\Omega_{j-1,j}$ so as to obtain the original data $D_{-1}$. For an asymmetric reversible parametric sequence $ARPS_j$, one cannot compute the original data $D_{-1}$ even if given the data $D_j$ (or $D_j'$) and the sequence \{e$_0$, \ldots, e$_j$\} (or \{e$_0'$, \ldots, e$_j'$\}), for $0 \leq j \leq N$.

One can use the properties of an asymmetric reversible parametric sequence $ARPS_j$ to implement a secure video proxy. To illustrate, consider a graphical representation of an $ARPS_j$ sequence in Figure 2. The proxy can request to obtain the encrypted version of the original data $D_{-1}$ from the source. Based on an encrypted key $e_0$, the source will transmit the encrypted data $D_0$ to the proxy, and the encrypted data $D_0$ will be cached at the proxy's local storage. When a client $i$ requests the data, the proxy will further encrypt the encrypted data $D_0$ using the encryption key $e_i$ and send the resulting encrypted data $D_i$ to client $i$. Client $i$, upon receiving $D_i$, can decrypt the data to obtain the original data $D_{-1}$. If $i$ is given a decryption function $\Omega_{-1,j}$ (this is a property of reversible parametric sequences). In addition, when the encryption is carried out using an asymmetric reversible parametric sequence, then even when an entity holds on to all the encryption keys $e_i$, for $0 \leq i \leq N$, it still cannot decrypt any of the encrypted data $D_i$ being cached, for $0 \leq i \leq N$, in order to obtain the original data $D_{-1}$.

Therefore, one can use an asymmetric reversible parametric sequence $ARPS_j$ to implement a video proxy which has the following properties:

- **Data confidentiality during transmission**: Since the original data $D_{-1}$ are encrypted, an intruder who eavesdrops on the link between the source and the proxy can only access $D_0$ and will not be able to extract the original data. The same conclusion holds when an intruder eavesdrops on the link between the proxy and the client $i$. The intruder can only access $D_i$ and will not be able to extract the original data.

- **End-to-end data confidentiality**: Because of the $RPS_j$, decryption of the original data $D_{-1}$ only takes place at the endpoints (e.g., the clients). The proxy and clients only store the data encrypted as $D_0$ and $D_i$. Hence, even if an intruder gains access to the proxy's or client's local storage, the original data $D_{-1}$ will not be revealed.

- **Data confidentiality against proxy intruders**: If an intruder compromises the proxy server or a client's machine, and if the encryption process is an $SRPS_j$, then the intruder, on knowing $e_0$ and $e_i$, can gain access to $D_{-1}$. This is because the function $\Omega_{-1,0}$ can be computed from the knowledge of $e_0$ and $e_i$ such that the original data can be revealed by $D_{-1} = \Omega_{-1,0}(D_0)$. On the other hand, if the encryption process is an $ARPS_j$, then even if $e_0$ and $e_i$ are compromised, the original data $D_{-1}$ cannot be revealed, because the function $\Omega_{-1,0}$ is computationally infeasible to determine in this case.

- **Data confidentiality against member collusion**: If the encryption process is $SRPS_j$, member collusion is possible when a client $j$ gains access to to (1) $e_i$ and $e_j$ (where $i, j > 0$), (2) the encrypted data $D_i$, and (3) the decrypting function $\Omega_{-1,j}$. In this case, client $j$ (i.e., the intruder) can access the original data $D_{-1}$. For example, given $e_i$ and $D_i$, the intruder can obtain $\Omega_{-1,0}$ and thus obtain $D_0 = \Omega_{-1,0}(D_i)$. Given the knowledge of $e_j$ and $D_0$, it can obtain $D_j$ by $D_j = f(D_0, e_j)$. Since the intruder knows the decryption function $\Omega_{-1,i}$, the original data $D_{-1}$ are revealed by $D_{-1} = \Omega_{-1,0}(D_j)$. However, if the encryption process is an $ARPS_j$, the intruder cannot reveal the original data $D_{-1}$ because the function $\Omega_{-1,i}$ is computationally infeasible to determine.

### 2.2 Implementation of $ARPS_j$

We need a practical and efficient algorithm to realize the properties of an asymmetric reversible parametric sequence.
In our work, we use multi-key RSA to implement an ARPS. We first present the basic idea of RSA. We then extend the concept to a multi-key RSA framework.

For standard RSA (or single-key RSA), one needs to generate two distinct large prime numbers \( p \) and \( q \). Let us define
\[
  n = pq, \\
  \phi = (p - 1)(q - 1).
\]
To encrypt a given data item \( D_{-1} \), one has to find an encryption key \( e_0 \) such that the integer \( e_0 \) satisfies
\[
  1 < e_0 < \phi, \quad \text{and} \quad \gcd(e_0, \phi) = 1.
\]

To encrypt the data \( D_{-1} \), we generate a cipher \( C \) based on the encryption key \( e_0 \) wherein
\[
  C = (D_{-1})^{e_0} \pmod{n}.
\]
The cipher \( C \) can be transmitted over an insecure channel. The receiver needs to have a decryption key \( d_0 \) to decrypt the cipher. This decryption key \( d_0 \) is an integer and is selected such that:
\[
  1 < d_0 < \phi, \quad \text{and} \quad (e_0d_0) = 1 \pmod{\phi}.
\]

Upon receiving the cipher, the receiver can decrypt the cipher \( C \) and obtain the original data \( D_{-1} \) by
\[
  D_{-1} = C^{d_0} \pmod{n}.
\]

We can extend the single-key RSA technique to a multi-key RSA technique. Consider the proxy server as an example. The proxy server needs to generate two large prime numbers, say \( p \) and \( q \). In addition, it needs to generate a sequence of encryption keys \( \{e_i\}_{0 \leq i \leq N} \) such that
\[
  1 < e_i < \phi, \quad \gcd(e_i, \phi) = 1.
\]
The proxy server will send the encryption key \( e_0 \) and \( n \) over a secure channel to the source. The source will encrypt the original data \( D_{-1} \) using \( e_0 \) and generate a cipher \( D_0 \) using
\[
  D_0 = (D_{-1})^{e_0} \pmod{n}.
\]
Upon receiving the cipher \( D_0 \), the proxy can store the encrypted data in its local storage. Whenever a client \( i \) wants to access the data from the proxy, the proxy can retrieve the encrypted data \( D_0 \) from its local storage, and encrypt \( D_0 \) using the encryption key \( e_i \) by
\[
  D_i = (D_0)^{e_i} \pmod{n}.
\]
Moreover, the proxy generates a decryption key \( d_i \) for client \( i \). The decryption key \( d_i \) has to satisfy the following two conditions:
\[
  1 < d_i < \phi, \quad \text{and} \quad (e_0e_i)d_i = 1 \pmod{\phi}.
\]

Computing these decryption keys \( d_i \) can be easily achieved using the Extended Euclidean Algorithm [7]. The proxy sends the decryption key \( d_i \) and \( n \) to client \( i \) over a secure channel. The encrypted data \( D_i \), on the other hand, can be sent over an insecure channel. Client \( i \), upon receiving the encrypted data \( D_i \), can decrypt the data using \( d_i \) by:
\[
  D_{-1} = \Omega, (D_i) = (D_i)^{d_i} \pmod{n}. \quad (7)
\]

Example: To illustrate, consider the following simple example. Suppose that the two primes are \( p = 5 \) and \( q = 7 \) (in reality, \( p \) and \( q \) have to be large). Accordingly, \( n = 5 \times 7 = 35 \) and \( \phi = (5 - 1) \times (7 - 1) = 24 \). Let there be three encryption keys: \( e_0 = 5, e_1 = 11 \) and \( e_2 = 13 \). If the original data \( D_{-1} = 10 \), the cached data in the proxy server will be
\[
  D_0 = 10^3 \pmod{35} = 5.
\]
When client 1 requests the data, the proxy will generate a decryption key \( d_1 \) such that \( (5 \times 11)d_1 = 1 \pmod{24} \). Using the Extended Euclidean Algorithm, we have \( d_1 = 7 \). Therefore, the encrypted data for client 1 is
\[
  D_1 = (D_0)^{d_1} \pmod{n} = 5^{11} \pmod{35} = 10 \]
and client 1 can decrypt the data \( D_1 \) and get back the original data \( D_{-1} \) by
\[
  D_{-1} = (D_1)^{d_1} \pmod{n} = 5^7 \pmod{35} = 10.
\]
When client 2 requests the data, the proxy will generate a decryption key \( d_2 \) such that \( (5 \times 13)d_2 = 1 \pmod{24} \). Using the Extended Euclidean Algorithm, we have \( d_2 = 17 \). Therefore, the encrypted data for client 1 is
\[
  D_2 = (D_0)^{d_2} \pmod{n} = 5^{13} \pmod{35} = 5 \]
and client 2 can decrypt the data \( D_2 \) and get back the original data \( D_{-1} \) by
\[
  D_{-1} = (D_2)^{d_2} \pmod{n} = 5^{17} \pmod{35} = 10.
\]

Theorem 1. The above proxy encryption framework is a reversible parametric sequence.


Theorem 2. The above proxy encryption procedure is an asymmetric reversible parametric sequence.


3. VIDEO PROXY: ARCHITECTURES AND PROTOCOLS

In this section, we describe in detail our server-proxy-client architecture. The video server, the video proxy and the clients have been implemented in C++ on a Linux platform. In our current implementation, we use a 512-bit RSA key to implement various encryption and decryption operations, but this can be easily extended to accommodate RSA keys with a larger number of bits. Security features such as keys generation, encryption and decryption are implemented using the GNU Multiply Precision (GMP 4.0) library, which
provides arbitrary precision arithmetic on integers, rational numbers, and floating-point numbers. GMP 4.0 provides one of the fastest possible arithmetic library for applications that need higher precision than is directly supported by the basic C types.

### 3.1 Proxy-Server Operations

Figure 3 illustrates the operations between the source video server $S$ and the proxy $P$ for requesting and caching the video data. These operations are:

1. **Key generation:** To request video data from the source video server $S$, the proxy $P$ first randomly generates two large prime numbers $p$ and $q$. Then $P$ computes the prime product $n = pq$, the pseudo-prime product $\phi = (n-1)(p-1)$, and the encryption key $e_0$ via Equations (1) and (2). To ensure security, the two prime numbers $p$ and $q$ should afterwards be deleted from the proxy $P$.

2. **Initiate connection:** The proxy $P$ sends a video request to the video server $S$ through a secure channel using the secure socket layer (SSL) protocol. The video server $S$ needs to authenticate that the request is indeed from the proxy $P$. If the authentication succeeds, the server replies with an acknowledgment back to the proxy $P$.

3. **Authentication of video server $S$:** The proxy $P$ authenticates whether the acknowledgment received from the previous step is indeed from the video server $S$.

4. **Transmission of encryption key:** If the authentication is successful, the proxy $P$ sends its encryption request key $e_0$ and $n$ to the video server $S$ through a secure channel.

5. **Data encryption and streaming:** The video server $S$ uses the encryption key $e_0$ and $n$ to encrypt the video data packets. The degree of encryption is based on the encryption configuration parameters (ECP) which we will describe in Section 3.3. The video server $S$ then streams the encrypted data packets to the proxy $P$ via an ordinary and possibly insecure channel. Upon receiving the encrypted data packets, the proxy caches the data without decryption or modification.

### 3.2 Client-Proxy Operations

Figure 4 illustrates the operations between the client $i$ and the proxy $P$ for streaming the encrypted data. These operations are:

1. **Initiate connection:** To request a video via the proxy $P$, the client $i$ sends a connection request to the proxy $P$ through a secure channel using SSL.

2. **Authentication of client:** The video proxy $P$ authenticates that the connection request is indeed from a valid client $i$.

3. **Key generation:** The proxy $P$ checks whether the requested video is cached or not. If it is not cached, the proxy will request the video from the video server $S$ using the operations described above. If the video is cached, the proxy $P$ generates an encryption key $e_i$ based on Equations (1) – (2), and a decryption key $d_i$ based on Equations (5) – (6).

4. **Transmission of decryption key:** The proxy $P$ sends the decryption key $d_i$ and $n$ to client $i$ through the secure channel.

5. **Data encryption and streaming:** Based on the encryption key $e_i$ and the encryption configuration parameters (ECP), the proxy $P$ encrypts the cached data $D_0$ using Equation (4). The newly encrypted data $D_i$ can then be sent to the client $i$ over an insecure channel. If the video data are not cached in the proxy $P$, $P$ requests the data from the video server $S$ using the operations described above. then, in a pipeline fashion, caches the data While blocks of data for $D_0$ are
received and cached in the proxy’s local storage, the proxy – in a pipeline fashion – encrypts the \( D_i \) data blocks to the \( D_i \) data blocks, and the \( D_i \) data blocks are sent to the client \( i \). The client \( i \), upon receiving the encrypted data \( D_i \), can decrypt the data using the previously received decryption key \( d_i \) generated by Equation (7).

### 3.3 Encryption Configuration Parameters

Although the proxy \( P \) does not need to perform any decryption, the RSA encryption operation – even when implemented using the optimized GMP 4.0 library – can still be expensive. Since \( P \) has to perform encryption for every client \( i \), the encryption overhead can limit the achievable streaming throughput and the number of concurrent clients that the proxy can support.

To reduce the computational overhead at the proxy we perform encryption based on selectable encryption configuration parameters (ECP). The idea consists in not performing encryption on an entire video stream, but instead on selected data blocks in the video stream. Note that for certain video formats, encrypting a complete video stream is inherently redundant. For example, if video data are encoded using MPEG-1, then one might argue that encrypting all the I frames in the video sequence would suffice, since the other frames depend on the I frames in decoding.

We propose to use a general encryption method that can reduce the encryption overhead at the proxy for a variety of commonly used video encoding formats (such as MPEG-1, MPEG-2, and Quicktime). We exploit the observation that, for video encoding that accounts for inter-frame data dependencies, a video stream only needs to be encrypted up to a certain percentage for decoding to be practically useless by an unauthorized viewer, in that either the video cannot be decoded, or the quality of the decoded video will be so poor that it is unacceptable for viewing. ECP specifies a packet based encryption pattern given by four adjustable parameters, namely

- \( S_{pkt} \), the expected number of bytes in a data packet.
- \( I \) – the video stream is to be partitioned into successive groups each having \( I \) consecutive packets, and a single packet encryption operation is to be applied to the first packet of each group.
- \( P \) – for a packet to which the packet encryption operation is to be applied, the fraction of data within the packet that should be encrypted.
- \( B \) – for a packet to which the encryption operation is to be applied, the number of encryption blocks that should be evenly distributed within the packet.

In our current implementation, we use UDP as the transport protocol for data transmission. The entire video stream will be divided into UDP packets with each packet having a payload size of \( S_{pkt} = 1400 \) bytes. For every \( I \geq 1 \) consecutive UDP packets, we will select the last UDP packet for encryption. For the encrypted packet, it will be further divided up into sub-blocks and only some of the sub-blocks will be encrypted. In our current implementation, the sub-block size is chosen to be 4 bytes less than the RSA key length (e.g., 60 bytes for 512-bit RSA) and the encryption will be based on this sub-block unit size. The total length of data to be encrypted within a packet is equal to \( P \times S_{pkt} \) rounded up to the nearest multiple of the sub-block size. The encrypted sub-blocks will then be regrouped as \( B \) consecutive blocks of data, and the blocks will be distributed evenly across the whole packet.

Figure 5 illustrates a possible set of encryption configuration parameters, where the packet size \( S_{pkt} \) is equal to 1400 bytes, \( I = 2 \) (i.e., out of every two consecutive packets, we select the first one for encryption), the fraction \( P \) is equal to 0.5, and \( B = 4 \) blocks are to be evenly distributed across an encrypted packet. The four configuration parameters allow us to achieve varying degrees of encryption and levels of video quality for the decoded stream. In Section 4, we illustrate the computational and quality tradeoffs implied by these parameters.

### 4. EXPERIMENTS

In this section, we report experiments that quantify the encryption throughput, and the peak signal-to-noise ratio (PSNR) and the visual quality of the decoded video, in the context of our secure video distribution architecture.

In our current implementation, we use encryption configuration parameters (ECP) to control the amount of encryption applied to blocks of video data. The experimental results are taken on an 800 MHz Pentium-III Linux machine with 256 MBytes of main memory. The video samples used in these experiments are a set of video sequences, each being an 18 MByte MPEG-1 stream or a 4.47 MByte Quicktime stream.

**Experiment 1: Encryption Throughput Analysis:**

In this experiment, we consider the effect of the parameters \( P \) and \( I \) on the encryption throughput, measured as \( \rho \) in MBytes/s. Assume that we are encrypting an MPEG-1 stream with an average bit rate of 1.5 Mbps. Given the assumption, the average number of concurrent MPEG-1 streams that a proxy can support is \( M \), where \( M = \rho/(1.5/8) \). Table 1 illustrates the encryption throughput \( \rho \) and the average number of concurrent MPEG-1 streams \( (M) \) under different values of \( P \) and \( I \), when \( B = 1 \). As we can observe from Table 1, if we encrypt 25.7% of each video packet (i.e., \( I = 1 \)), the encryption throughput achieved is
only around 2.13 MBytes/s, which implies that we can only concurrently handle about 11 MPEG-1 streams. On the other hand, if we encrypt one video packet for every 10 packets (i.e., $I = 10$) and for each video packet encrypted, we encrypt only 4.3% of its data, then the encryption throughput improves to 11.82 MBytes/s, which implies that we can concurrently support about 63 MPEG-1 streams. In general, the smaller the values of $P$ and $I$, the higher the encryption throughput and the number of concurrent video streams the system can handle.

Table 2 illustrates the effect of $I$ and $B$ under two different encryption percentage parameters $P$. As we can observe, the parameter $B$ has little effect on the encryption throughput.

**Experiment 2: Peak Signal-to-Noise Analysis:**
In this section, we consider the effect on the video quality as we vary the parameters $I$, $P$, and $B$. One way to quantitatively assess the video quality is by the peak signal-to-noise ratio. In general, for a frame size of $m \times n$ with a total of $l$ frames and 3 color channels (e.g., red, green, and blue, each represented by a 8-bit number), the peak signal-to-noise ratio ($SNR_{peak}$) is calculated using the following equation:

$$SNR_{peak} = 10 \times \log_{10} \left( \frac{255^2}{\frac{1}{3nm} \sum_{z=1}^{m} \sum_{x=1}^{n} (P(x,y,z,c) - \bar{P}(x,y,z,c))^2} \right)$$

where $P(x,y,z,c)$ means that the pixel value at coordinates $(x,y)$ in the $z$-th frame for color channel $c$, where $c = 1$, $c = 2$, and $c = 3$ correspond to the color channels red, green, and blue, respectively. In our experiment, the values of $m$, $n$, and $l$ are 640, 480, and 1000, respectively. Values of $P$ are obtained from the video frames decoded by a client which does not have access to the decryption key, while values of $P$ are obtained from the original video frames. Note that a lower value of $SNR_{peak}$ indicates that the encrypted stream is more highly distorted from the original video data stream.

Table 3 and Table 4 illustrate the peak signal-to-noise ratio $SNR_{peak}$ for different values of $P$ and $I$ with $B = 1$ for MPEG-1 and Quicktime video, respectively. Note that even when we encrypt one out of 10 video packets, and for a selected packet, we only encrypt 4.3% of the data, we still obtain a very low value of $SNR_{peak}$. This indicates that (1) we can apply this encryption technique for different video formats, and (2) we only need to encrypt a small fraction of the video data to achieve both high encryption throughput and high video distortion.

**Experiment 3: Comparison of visual quality of encrypted video:** In this experiment, we consider the effect of the ECP parameters $I$, $P$, and $B$ on the visual quality of the video. Figure 6 illustrates the quality of five consecutive MPEG-1 video frames. Figure 6(a) is the original video frames that a client can decode given access to the decryption key. Figures 6(b)-(e) are the corresponding five video frames when decoded without the decryption key. Note that the video quality is the worst when the ECP parameters are $I = 1$ and $P = 0.043$, which corresponds to encrypting 4.3% of the data for every video packet. Note that when we select $I = 10$, $P = 0.043$, and $B = 1$ (this corresponds to Figure 6(e)), the visual quality of the video is still quite unacceptable for viewing. This shows that we can achieve high encryption throughput (e.g., around 11.82 MBytes/s or about 63 concurrent MPEG-1 streams from Table 1) and, at the same time, ensure that those clients which do not possess the decryption keys will get unacceptable video quality on viewing. Figure 7 shows the corresponding results for five consecutive Quicktime video frames.
6. CONCLUSION
We have presented the design and implementation of a multi-key secure video proxy architecture. Our design is based on the notion of an asymmetric reversible parametric sequence (ARPS). We discussed how ARPS can be applied to a general client-proxy-server architecture. To practically achieve the confidentiality properties of ARPS, we presented a multi-key RSA technique, and proved that the technique realizes an ARPS. In summary, our theoretical results show that the proposed architecture can achieve comprehensive data confidentiality that is provably resilient against attacks, given standard computability assumptions.

We have an implementation of our video streaming architecture — consisting of server, proxy and client — on commodity Pentium III/800 MHz machines running Linux. Our implementation results empirically demonstrate how a set of four ECP parameters can trade off encryption throughput against data confidentiality, for a number of standard MPEG-1 and Quicktime video sequences. They indicate that it is possible to simultaneously achieve high encryption throughput and extremely low video quality (in terms of both PSNR and the visual quality of decoded frames) during unauthorized viewing. For example, by using \( I = 10 \) and \( P = 0.043 \) a single Pentium III/800 MHz machine can concurrently sustain more than 64 distinct MPEG-1 video streams, while giving good protection for the original video data.

7. REFERENCES
Table 4: Effect of $P$ and $I$ on the peak signal-to-noise ratio $SNR_{peak}$ on Quicktime video when $B = 1$.

<table>
<thead>
<tr>
<th>$I$</th>
<th>$P = 0.257$</th>
<th>$P = 0.214$</th>
<th>$P = 0.171$</th>
<th>$P = 0.120$</th>
<th>$P = 0.086$</th>
<th>$P = 0.043$</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>11.38</td>
<td>11.56</td>
<td>11.72</td>
<td>12.13</td>
<td>12.28</td>
<td>12.48</td>
</tr>
<tr>
<td>2</td>
<td>12.15</td>
<td>12.13</td>
<td>12.27</td>
<td>12.55</td>
<td>12.48</td>
<td>12.77</td>
</tr>
<tr>
<td>5</td>
<td>12.63</td>
<td>12.48</td>
<td>12.57</td>
<td>12.97</td>
<td>12.84</td>
<td>12.98</td>
</tr>
<tr>
<td>10</td>
<td>12.97</td>
<td>12.76</td>
<td>12.84</td>
<td>13.24</td>
<td>12.98</td>
<td>13.09</td>
</tr>
</tbody>
</table>

Figure 6: Quality of five consecutive MPEG-1 video frames under different ECP parameters.
Figure 7: Quality of five consecutive Quicktime video frames under different ECP parameters.