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Exploration of the limits to mobility in two-dimensional hole systems in GaAs/AlGaAs quantum wells

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We report on the growth and electrical characterization of a series of two-dimensional hole systems (2DHSs) used to study the density dependence of low temperature mobility in 20-nm GaAs/AlGaAs quantum wells. The hole density was controlled by changing the Al mole fraction and the setback of the δ -doping layer. We varied the density over a range from $1.8 \times 10^{10} \text{ cm}^{-2}$ to $1.9 \times 10^{11} \text{ cm}^{-2}$ finding a nonmonotonic dependence of mobility on density at $T = 0.3 \text{ K}$. Surprisingly, a peak mobility of $2.3 \times 10^6 \text{ cm}^2/\text{Vs}$ was measured at a density of $6.5 \times 10^{10} \text{ cm}^{-2}$, with further increase in density resulting in reduced mobility. We discuss possible mechanisms leading to the observed nonmonotonic density dependence of the mobility. Relying solely on interface roughness scattering to explain the observed drop in mobility at high density requires roughness parameters that are not consistent with measurements of similar electron structures. This leaves open the possibility of contributions from other scattering mechanisms at high density.

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I. INTRODUCTION

Two-dimensional hole systems (2DHSs) on (001)-oriented GaAs offer an interesting alternative to the more widely studied two-dimensional electron systems (2DESs). 2DHSs on (001) GaAs have effective masses roughly 4.5 to 7.5 times larger¹⁻³ than that in corresponding 2DESs, which increases the importance of Coulomb interactions relative to the kinetic energy resulting in enhancement of importance of many-body effects. In addition, the p -wave symmetry of the valence band in GaAs leads to a much-reduced hyperfine coupling of hole spins to the atomic nuclei that makes them an exciting alternative to electrons for quantum dot spin-based qubits.⁴⁻⁶ The presence of spin-orbit coupling and light/heavy-hole mixing in the valence band of GaAs also allows extensive band structure engineering.⁷⁻⁹ This feature has been exploited to alter the nature of ground states in the quantum Hall regime.^{10,11}

Here we describe our efforts to understand the limits to low-temperature mobility for (001) 2DHSs. Continued improvement in 2DHS quality is motivated by the well-established paradigm for 2DESs that increased low-temperature mobility often leads to the observation of new correlated ground states.¹² Historically, improvement to the low-temperature mobility of 2DHSs has lagged behind that of 2DESs due to the lack of a p -type dopant in GaAs that does not diffuse or segregate significantly at typical molecular beam epitaxy (MBE) growth temperatures $\sim 635^\circ\text{C}$. Si can act as a low-diffusivity acceptor on the (311)A face of GaAs, but subsequent transport experiments are known to be complicated by a significant mobility anisotropy due to surface corrugation.¹³ However, recent use of low-diffusivity carbon doping (C-doping)¹⁴⁻¹⁶ has rapidly led to low-temperature mobilities $> 10^6 \text{ cm}^2/\text{Vs}$ without the accompanying transport anisotropy. Purely from a growth standpoint, then, there does not appear to be any reason why low-temperature hole mobilities should not approach that of electrons once scaled by the appropriate effective mass.

Presently, it is widely believed that uniformly distributed ionized background impurities limit the mobility in the best 2DESs.¹⁷ However, the highest hole mobility reported to date¹⁹ of $2.6 \times 10^6 \text{ cm}^2/\text{Vs}$ is still about a factor of 2 lower than record mobility 2DESs grown in the same MBE chamber¹² once the heavy hole to electron effective mass ratio of $0.4m_e:0.067m_e$ is taken into account. The question, then, remains: If sufficiently reducing background impurities¹⁷ is the main obstacle to reaching an electron mobility of $100 \times 10^6 \text{ cm}^2/\text{Vs}$, what are the key ingredients to a hole mobility of $15 \times 10^6 \text{ cm}^2/\text{Vs}$?

II. EXPERIMENT

In order to answer this question, we have begun to explore the impact of varying structural parameters on the resulting mobility. Samples in this work were grown in a customized Veeco GenII MBE, which has recently achieved *electron* mobilities $> 20 \times 10^6 \text{ cm}^2/\text{Vs}$ and extremely large excitation gaps for the fragile $\nu = 5/2$ fractional quantum Hall state. C-doping was performed with a carbon filament capable of producing a doping rate of $2.8 \times 10^{10} \text{ cm}^{-2}/\text{s}$ at a total power (including parasitic dissipation) of $\sim 150 \text{ W}$.¹⁸ In this experiment, we utilized a 20-nm quantum well situated 190 nm below the surface and asymmetrically δ -doped from above at a setback d of 80, 110, or 140 nm. The Al mole fraction x was also varied between 0.07 and 0.45 to allow further tuning of the 2DHS density. Table I summarizes the structures grown in the experiment, and Fig. 1 shows the epilayer design.

Square samples were prepared using InZn contacts annealed at 430°C for 15 min in H_2/N_2 forming gas. Characterization was performed in the dark and after illumination with a red LED at $T = 300 \text{ mK}$ using standard lock-in techniques, and the density was determined from quantum Hall effect (QHE) minima. Illumination typically resulted in ~ 3 – 5% increase in density and as much as a 27% increase in

TABLE I. Summary of structural parameters including δ -doping setback distance d , Al mole fraction around the dopants x_d , Al mole fraction surrounding the quantum well x_w , 2DHS density p , and $T = 300$ mK mobility after illumination μ .

Sample	d (nm)	x_d	x_w	p (10^{11} cm $^{-2}$)	μ (10^6 cm 2 /Vs)
1	80	0.24	0.24	1.1	1.2
2	80	0.24	0.24	0.98	1.4
3	80	0.45	0.45	1.9	0.55
4	80	0.10	0.10	0.32	1.8
5	80	0.35	0.35	1.4	0.80
6	80	0.20	0.20	0.80	1.6
7	80	0.07	0.07	0.18	1.3
8	110	0.10	0.10	0.29	1.5
9	140	0.10	0.10	0.23	1.4
10	110	0.24	0.24	0.70	1.6
11	80	0.16	0.16	0.65	2.3
12	110	0.13	0.13	0.36	1.8
A	80	0.45	0.16	1.7	0.73
B	80	0.45	0.24	1.5	0.78
C	80	0.35	0.16	1.34	1.3
D	80	0.35	0.24	1.30	1.1

mobility for low-density samples. Transport data also showed a qualitative improvement after illumination, indicating that illumination increases the homogeneity of the 2DHS and has a favorable impact on the screened disorder potential. Figure 2 shows transport data of the highest mobility sample and a low density sample; the number of nascent fractional QHE features attest to the sample quality.

Figure 3(a) shows the measured mobility as a function of density for various values of d . We note that remote ionized impurity (RI) scattering does not play a significant factor in limiting the mobility since within experimental uncertainty there is no meaningful difference between the mobility at different values of d for the same density. However, increased d should allow these samples to be gated to ultralow densities before RI scattering begins to cause the mobility to rapidly drop off with further decreased density.¹⁹ The most interesting feature of the data in Fig. 3(a), however, is the strongly nonmonotonic dependence of the mobility on density. For 2DESs in this density range with such a large value of d ,

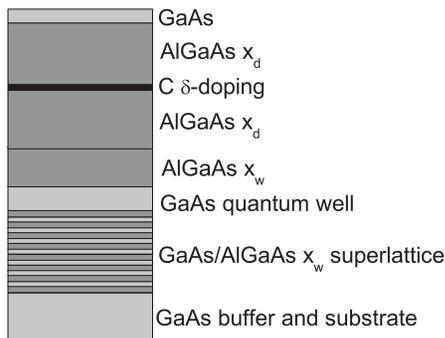


FIG. 1. Layer structure of devices in this experiment. Note the use of two different Al mole fractions x_w and x_d in some of the devices as indicated in Table I.

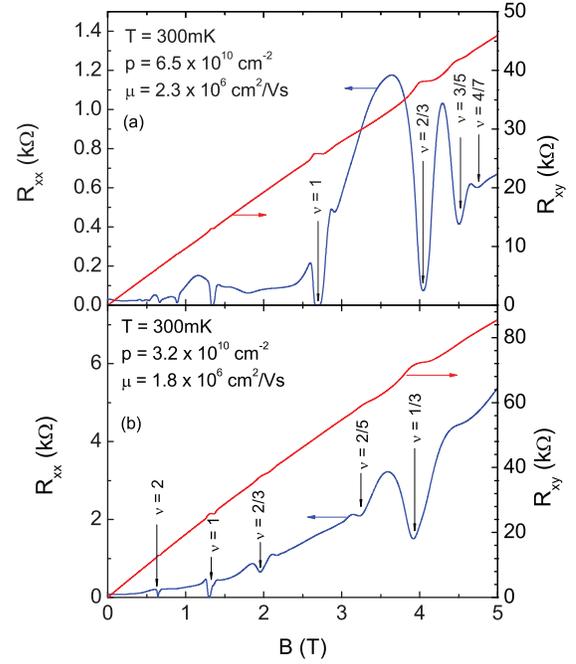


FIG. 2. (Color online) Magnetotransport at $T = 300$ mK after illumination with a red LED of (a) peak mobility sample and (b) low-density sample that exhibits many nascent fractional QHE features.

one would expect the mobility to monotonically increase with density^{12,17,20,21} following a power-law dependence $\mu \propto p^\alpha$, where $\alpha \sim 0.6-0.8$, with ionized background impurity (BI) scattering being the dominant scattering mechanism. In analyzing our results, we, first, note that the effective mass is known to vary throughout the density range of our samples due to the valence band nonparabolicity arising from light- and heavy-hole band mixing. By performing a linear fit to cyclotron resonance data on 2DHSs in (001) 20-nm quantum wells in Refs. 1 and 2 and assuming the cyclotron mass plateaus at $0.5m_e$ at high density, we estimate the transport lifetime for our structures as shown in Fig. 3(b). The transport lifetime, however, follows the same nonmonotonic behavior as the mobility, which indicates a competition between different scattering mechanisms throughout the density range of our experiment in addition to the changing mass.

III. SCATTERING CALCULATIONS

To shed further light on possible scattering mechanisms, we have performed a series of scattering calculations, including the effects of BI, RI, alloy, and interface roughness (IR) scattering. We follow the derivation of the transport relaxation time in Ref. 22, which assumes $T = 0$ and neglects intersubband scattering, multiple scattering events, and correlation between ionized impurities. This simple calculation is intended to elucidate the expected trend of the mobility as the density is increased and determine if scattering mechanisms dominant in 2DESs can qualitatively explain our observations. More sophisticated calculations have been made by S. Das Sarma and coworkers.^{17,23,24} Transport relaxation times are calculated individually and then the total mobility is calculated using Mathiessen's rule. For BI and RI scattering the transport

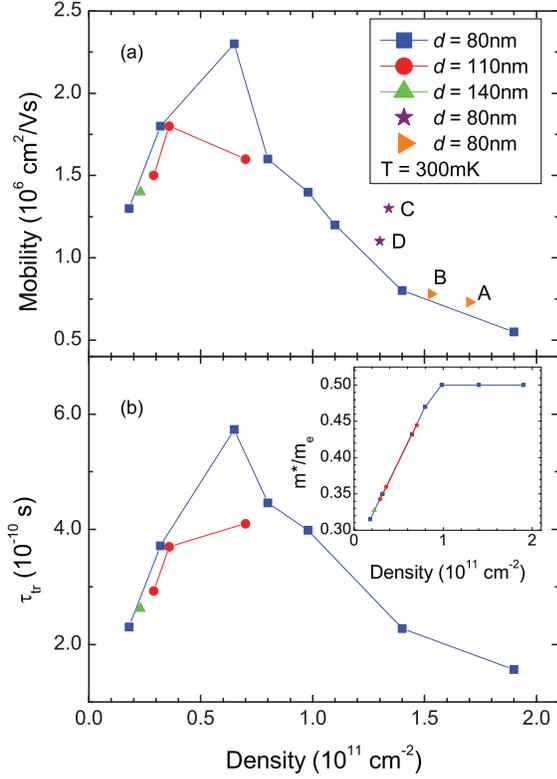


FIG. 3. (Color online) (a) $T = 300 \text{ mK}$ mobility after illumination with a red LED as a function of density for various dopant setback distances d . Solid lines are guides to the eye. For fixed d the density was controlled by varying the Al mole fraction x . Samples were grown in random order to avoid continued machine cleanup from skewing the observed trend in mobility. Samples A–D were grown with varying x at fixed p to test the effect of alloy and interface roughness scattering on the mobility (see text). (b) Transport lifetime estimated as a function of density. (Inset) Effective mass for our structures as a function of density, extrapolated from Refs. 1 and 2.

lifetime is given by

$$\frac{1}{\tau_{tr}(\epsilon_F)} = \frac{m^*}{\pi \hbar^3} \sum_i \int_0^\pi d\theta [1 - \cos(\theta)] \times \left[\frac{2\pi e Z_i e_i}{4\pi \epsilon (q + q_{TF} g_s(\mathbf{q}))} \right]^2 \int_{-\infty}^\infty dz N_i(z) g_{imp}^2(q, z), \quad (1)$$

where m^* is the hole effective mass [as estimated in Fig. 3(b)], \hbar is the reduced Planck constant, θ is the scattering angle, $Z_i e_i$ is the impurity charge, ϵ is the dielectric constant of the semiconductor, \mathbf{q} is the scattering vector, k_F is the Fermi wave vector, q_{TF} is the Thomas-Fermi screening wave vector, and $N_i(z)$ is the i^{th} impurity distribution, and the form factors are given by

$$g_s(\mathbf{q}) = \int \chi^2(z) \chi^2(z') \exp(-q|z - z'|) dz dz', \quad (2)$$

$$g_{imp}(q, z) = \int \chi^2(z') \exp(-q|z' - z|) dz', \quad (3)$$

where $\chi(z)$ is the self-consistently calculated²⁵ envelope function in the effective mass approximation. For the BI

calculation we use a three-dimensional impurity concentration N_{3D} as a fitting parameter and find the best agreement with the experimental data for $N_{3D} = 2 \times 10^{13} \text{ cm}^{-3}$. We use a remote impurity sheet concentration N_{RI} equal to the hole concentration p . A more realistic value of N_{RI} could also include some of the ionized impurities due to the surface compensation; however, we assume a simple parallel-plate capacitor model of the surface- δ -layer charge and, thus, neglect the surface compensation contribution to N_{RI} . This neglect of charge due to surface compensation is typical in these types of calculations.^{17,26,27} For our purposes, though, the exact value of N_{RI} is not important since it will not change the qualitative dependence of the RI-limited mobility as p is varied.

To calculate alloy scattering we use the virtual crystal approximation with a square-well potential limited over a spherical range²⁸ that is independent of temperature in 2D systems.²⁹ The alloy-limited relaxation lifetime is unscreened due to its short-range nature and given by^{22,30}

$$\frac{1}{\tau_{alloy}(\epsilon_F)} = \frac{4\Omega^2 m^* U^2 x(1-x)}{a^3 \hbar^3} \int_{\text{barrier}} \chi^4(z) dz, \quad (4)$$

where $a = 0.565 \text{ nm}$ is the lattice constant of the compound semiconductor, Ω is the volume of the scattering potential given by $\Omega = (4/3)\pi r^3$, and $r = (\sqrt{3}/4)a$ is the nearest-neighbor separation. There is a broad range of estimates of the magnitude of the scattering potential U in the literature,³⁰ ranging from 0.12 to 1.56 eV. We take $U = 1 \text{ eV}$ (as suggested in Ref. 22) as a rough estimate.

To examine the possible effect of interface roughness scattering, we employ a simple model that makes use of the Fang-Howard variational wave function and associated potential³¹ that takes the distortion of the wave function with increased density into account. In this model, the IR scattering rate is given by^{32,33}

$$\frac{1}{\tau_{IR}(\epsilon_F)} = \left(\frac{\Delta \Lambda e^2 p}{2\epsilon} \right)^2 \frac{m^*}{\hbar^3} \int_0^\pi \left[\frac{q}{q + g_s(\mathbf{q}) q_{TF}} \right]^2 \times (1 - \cos \theta) \exp(-\Lambda^2 q^2 / 4) d\theta, \quad (5)$$

where the wave function used to calculate g_s is

$$\chi(z) = \begin{cases} \frac{1}{\sqrt{2}} b^{3/2} z e^{-bz/2} & z > 0 \\ 0 & z \leq 0 \end{cases},$$

where the variational parameter is^{32,34}

$$b = \left(\frac{33m^* e^2 p}{8\hbar^2 \epsilon} \right)^{1/3}. \quad (6)$$

We take one monolayer roughness height to be a reasonable estimate and, thus, set $\Delta = 0.2825 \text{ nm}$ and use Λ as a fitting parameter with the result that $\Lambda = 6 \text{ nm}$.

As a justification for using the Fang-Howard wave function to model our asymmetric quantum-well system, we show, in Fig. 4, a comparison of the self-consistently calculated valence band edges for quantum-well (QW) sample 3 and a single heterojunction (SHJ) along with the self-consistently calculated wave function for the QW structure and the Fang-Howard wave function, which is often taken as an approximation of the wave function in SHJ structures. The band edges show that the bottom barrier of the QW changes

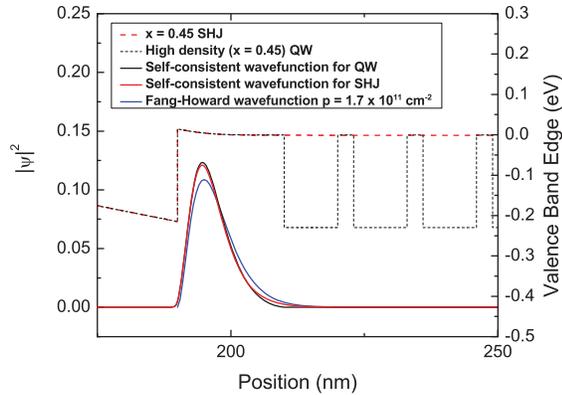


FIG. 4. (Color online) Dashed lines show a comparison of the self-consistently calculated valence band edges (dashed lines) for the high-density sample 3 and a single heterojunction sample with $x = 0.45$. Solid lines show a comparison of the self-consistently calculated wave function for sample 3 and the Fang-Howard variational wave function.

the confining potential very little, and the high-density samples (where IR scattering could be important) can be, therefore, approximated by the Fang-Howard model.

IV. DISCUSSION

The results of our calculations are compared with the $d = 80$ nm experimental results in Fig. 5. It is clear that even with a changing effective mass and wave-function profile the BI- and RI-limited mobilities steadily increase with increasing density and, therefore, cannot account for the drop in mobility at high density. The exact contributions of alloy and interface roughness scattering are initially less clear, however. We will address alloy disorder first.

If U is large enough, alloy scattering could conceivably contribute to the drop in mobility seen in the experimental data. Before continuing, it should be noted that the slight increase in the calculated alloy-limited mobility at high density

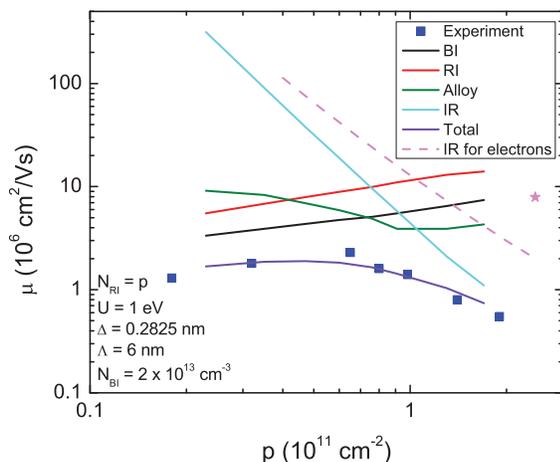


FIG. 5. (Color online) Comparison of $d = 80$ nm experimental data with mobility calculations. N_{BI} and Λ are used as free parameters to obtain a good fit to data. Pink star represents SHJ 2DES grown during this experiment.

is simply due to the saturation of the effective mass as shown in the inset of Fig. 3(b). We have repeated the calculations (not shown) without forcing the mass to plateau at $0.5m_e$, but even with a mass as high as $0.7m_e$ at high density the alloy-limited mobility does not appear to be limiting the total mobility. To test the contribution of alloy scattering, we grew a series of four test structures [labeled A-D in Fig. 3(a)] in which x_d , the Al concentration starting 25 nm above the quantum well (e.g., around the δ -doping layer), was kept fixed to keep the density constant while x_w , the Al concentration around the quantum well, was varied between $x_w = 0.16$ and $x_w = 0.24$. Samples A, B, and 3 ($x_d = 0.45$) suggest that x_w has no impact on the mobility, though there is scatter in the resulting density that we attribute to wafer-to-wafer variation and possible variation in the illumination. Samples C, D, and 5 ($x_d = 0.35$), however, suggest that increased x_w does cause the mobility to decrease somewhat. Most importantly, this is the opposite trend that would be expected if alloy scattering per se were limiting the mobility. Our calculations for the test structures (not shown) and Ref. 33 predict that the alloy-limited mobility would increase for increased x_w since as x_w is increased for fixed density the wave function is more confined. This, in turn, causes the integral of χ^4 to decrease faster than the $x(1-x)$ term increases in Eq. (4) resulting in a decrease in the alloy scattering rate for increased x_w . The results from this set of structures is consistent, however, with the theory that Al getters impurities,¹² thus, an increase in x_w would locally increase N_{BI} and the associated scattering. Regardless, samples C, D, and 5 show that the negative side effects of increasing x_w are not enough to explain the data of Fig. 3. If the increase in x_w was dominating the mobility we would expect test structures A and C to have significantly higher mobilities than the peak mobility sample 11 due to the higher hole density of the test structures. This, however, is clearly not the case.

Finally, our fit seems initially to indicate that IR scattering is limiting the mobility at high density. However, whenever parameters can be freely adjusted caution must, of course, be exercised to obtain physically meaningful results. The dashed pink line in Fig. 5 shows the IR-limited mobility for a SHJ 2DES in the Fang-Howard model while the pink star shows a 2DES SHJ structure with $x = 0.35$ grown during the course of this experiment. Evidently, the Fang-Howard calculation overestimates the IR scattering by at least a factor of 4. Repeating our self-consistent calculation for BI, RI, and alloy scattering in this 2DES SHJ using the impurity concentrations and alloy potential listed in the inset of Fig. 5 we find that the IR-limited mobility at a density of $2.4 \times 10^{11} \text{ cm}^{-2}$ would have to be $86 \times 10^6 \text{ cm}^2/\text{Vs}$ to fit the measured total mobility of $7.9 \times 10^6 \text{ cm}^2/\text{Vs}$. To get such a high IR-limited mobility we are forced to set $\Delta = 0.1 \text{ nm}$ and $\Lambda = 2.2 \text{ nm}$. Figure 6 shows the result of our calculation for the hole structures using these smaller roughness parameters. With these reduced roughness parameters there is no longer a good fit to the hole data at high density as the IR term makes almost no contribution to the total mobility, though we still obtain a good fit at low to medium density. We conclude that our crude model of interface roughness scattering cannot simultaneously account for our experimental data in both electrons and holes and are, thus, hesitant to conclude that interface roughness scattering is the dominant source of our drop in mobility at high density. Similar

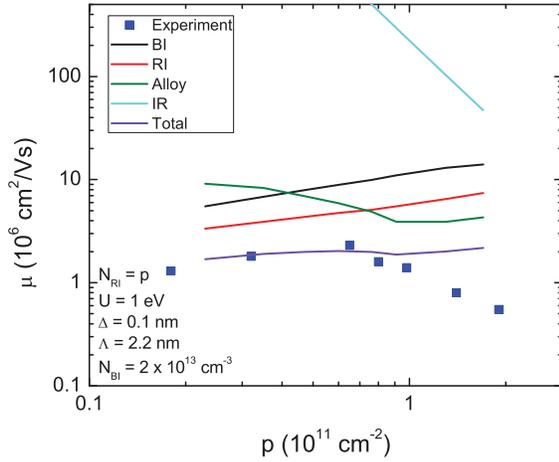


FIG. 6. (Color online) Comparison of $d = 80$ nm experimental data with mobility calculations. Δ and Λ are varied in order for mobility calculations to obtain agreement with an electron structure grown during this experiment (see text).

discrepancies between electron and hole data have been noted in Ref. 35.

Another possible scattering mechanism that must be kept in mind at high density is scattering between the electric subbands of the quantum well, which is known to degrade the mobility in high-density 2DESS.³⁶ To estimate the possibility of such scattering, we use a finite square well with a barrier height of 230 meV and an effective mass of $0.5m_e$, which corresponds to our highest-density sample. This estimate results in an energy spacing of 5.0 meV between the heavy-hole ground and first excited state. Assuming a light hole mass along the (001) direction^{8,34} of $0.090m_e$, the spacing between the heavy-hole and light-hole ground states is 6.4 meV. In both cases, this energy spacing is significantly larger than the Fermi

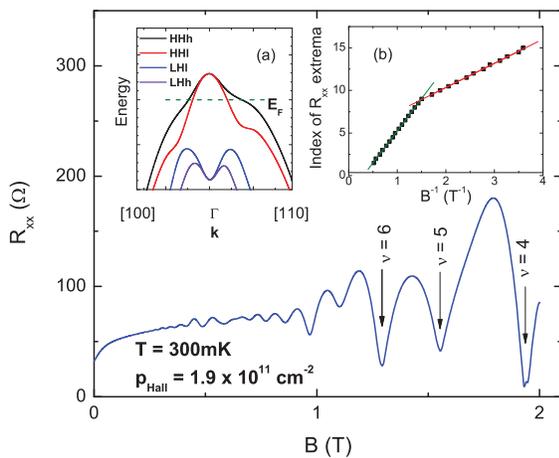


FIG. 7. (Color online) Shubnikov-de Haas oscillations of high density $d = 80$ nm, $x = 0.45$ device. [Inset (a)] Sketch of the spin-split heavy-hole and light-hole ground states in a quantum well. [Inset (b)] Index of extrema in R_{xx} vs. B^{-1} . The high field slope gives the total density of $1.8 \times 10^{11} \text{ cm}^{-2}$, and the low field slope gives the lighter subband density of $7 \times 10^{10} \text{ cm}^{-2}$ while the difference in the two gives the second subband density of $1.1 \times 10^{11} \text{ cm}^{-2}$.

energy, $E_F = \frac{\pi \hbar^2 p}{m^*} \sim 0.9 \text{ meV}$, which precludes a significant contribution from intersubband scattering between the electric subbands.

Next, we note the presence of beating in the Shubnikov-de Haas oscillations in Fig. 7, which is indicative of $B = 0$ spin splitting. Such spin splitting is known to occur in structurally asymmetric devices^{7,9,37} due to Rashba spin-orbit coupling.⁸ We sketch the qualitative effect of this splitting in Fig. 7(a). As the 2DHS density is increased, the electric field (and, hence, spin splitting) in the well is also increased. Furthermore, it is known that the presence of a parallel channel can result in a Hall density that differs from the sum of the subband densities and a measured mobility that differs from that of either subband, even in the absence of intersubband scattering. In our case, we assume that the two parallel channels are noninteracting $B = 0$ spin-split subbands of the heavy-hole ground state. The measured Hall density p_{Hall} and mobility μ_{Hall} in the absence of intersubband scattering are given by³⁴

$$p_{\text{Hall}} = \frac{(p_1 \mu_1 + p_2 \mu_2)^2}{p_1 \mu_1^2 + p_2 \mu_2^2}, \quad (7)$$

$$\mu_{\text{Hall}} = \frac{p_1 \mu_1^2 + p_2 \mu_2^2}{p_1 \mu_1 + p_2 \mu_2}, \quad (8)$$

where $\mu_{1(2)}$ and $p_{1(2)}$ are the mobility and density, respectively, of the first (second) subband. Figure 8(a) illustrates the Hall

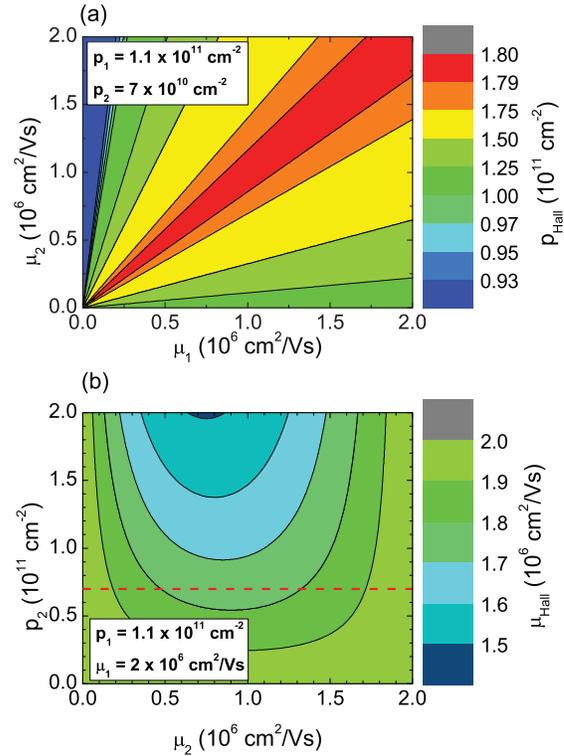


FIG. 8. (Color online) (a) Estimate of the Hall density expected from Eq. (7) using the measured subband densities $p_1 = 1.1 \times 10^{11} \text{ cm}^{-2}$ and $p_2 = 7 \times 10^{10} \text{ cm}^{-2}$. (b) Estimate of the expected measured mobility μ_{Hall} if the high density subband $p_1 = 1.1 \times 10^{11} \text{ cm}^{-2}$ has a high mobility $\mu_1 = 2 \times 10^6 \text{ cm}^2/\text{Vs}$. For the second subband density (dashed red line) $p_2 = 7 \times 10^{10} \text{ cm}^{-2}$ measured in Fig. 7 the expected measured mobility $\mu_{\text{Hall}} \geq 1.75 \times 10^6 \text{ cm}^2/\text{Vs}$.

density as a function of the subband mobilities in our peak density sample (sample 3) predicted by Eq. (7) using the subband densities extracted in Fig. 7. It is clear from Fig. 8(a) that, in order to measure a Hall density $\sim 1.8 \times 10^{11} \text{ cm}^{-2}$, the subband mobilities should be comparable, though the high-density subband should have a slightly higher mobility. In order to estimate the effect of the presence of two subbands on the measured mobility, we, therefore, assume that the high-density subband is also the high-mobility subband. In order to determine if the presence of the lower-mobility subband could by itself account for the drop in mobility seen in Fig. 3, we assume that the high-mobility subband is unchanged from the peak total mobility value ($\sim 2 \times 10^6 \text{ cm}^2/\text{Vs}$) at low density. Figure 8(b) shows, thus, what we would expect to measure as a function of density and mobility in the low-mobility subband if the high-mobility subband has a density $p_1 = 1.1 \times 10^{11} \text{ cm}^{-2}$ as we measure in Fig. 7. For the measured second subband density of $p_2 = 7 \times 10^{10} \text{ cm}^{-2}$ (dashed red line) we see that this parallel subband effect would not decrease the measured mobility below $\sim 1.75 \times 10^6 \text{ cm}^2/\text{Vs}$. We, therefore, conclude that the presence of a second, possibly low-mobility, $B = 0$ spin-split subband cannot explain our observed drop in mobility at high density in the absence of intersubband scattering.

A final possible mechanism for the observed drop in mobility at high density is intersubband scattering between the spin-split subbands of the heavy-hole ground state of the quantum well. The question remains, however, whether there exists a potential capable of coupling the spin-split subbands and causing backscattering. Such scattering is typically neglected in theoretical calculations of the mobility due to the assumed lack of a significant spin-flip mechanism,³⁸ though intersubband hole-hole scattering in inversion-asymmetric structures is not without precedent.³⁹ At this time, more theoretical work is needed to resolve the relative contributions of the different scattering mechanisms.

V. CONCLUSION

In conclusion, we have performed an experimental study of the density dependence of mobility in C-doped (001) GaAs/AlGaAs quantum wells by varying the dopant setback d and Al mole fraction x . The mobility was seen to depend nonmonotonically on the density. At low density the mobility increased with density. The $T = 300 \text{ mK}$ mobility was found to peak at a value of $2.3 \times 10^6 \text{ cm}^2/\text{Vs}$ at a density of $6.5 \times 10^{10} \text{ cm}^{-2}$. This 2DHS mobility is among the highest ever reported. Increasing the density further, however, resulted in a sharp drop in mobility. Scattering calculations indicate that background ionized impurities and remote ionized impurities will not lead to a decrease in mobility at high density even with a changing effective mass, and alloy scattering cannot account for all of our experimental results from various test structures. Interface roughness scattering contributions remain unclear due to the difficulty in obtaining physically reasonable roughness parameters that predict both electron and hole mobilities. Beating in the Shubnikov-de Haas oscillations in our high-density samples is indicative of zero-field spin splitting, which leaves open the possibility of an intersubband scattering contribution to the mobility. Further theoretical work is needed to determine the mechanism and magnitude of such a contribution.

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¹T. M. Lu, Z. F. Li, D. C. Tsui, M. J. Manfra, L. N. Pfeiffer, and K. W. West, *Appl. Phys. Lett.* **92**, 012109 (2008).
²H. Zhu, K. Lai, D. Tsui, S. Bayrakci, N. Ong, M. Manfra, L. Pfeiffer, and K. West, *Solid State Commun.* **141**, 510 (2007).
³M. N. Khannanov, I. V. Kukushkin, S. I. Gubarev, J. Smet, K. von Klitzing, W. Wegscheider, and C. Gerl, *JETP Lett.* **85**, 242 (2007).
⁴D. Brunner, B. D. Gerardot, P. A. Dalgarno, G. Wüst, K. Karrai, N. G. Stoltz, P. M. Petroff, and R. J. Warburton, *Science* **325**, 70 (2009).
⁵B. D. Gerardot, D. Brunner, P. A. Dalgarno, P. Ohberg, S. Seidl, M. Kroner, K. Karrai, N. G. Stoltz, P. M. Petroff, and R. J. Warburton, *Nature* **451**, 441 (2008).
⁶D. V. Bulaev and D. Loss, *Phys. Rev. Lett.* **95**, 076805 (2005).
⁷J. P. Eisenstein, H. L. Störmer, V. Narayanamurti, A. C. Gossard, and W. Wiegmann, *Phys. Rev. Lett.* **53**, 2579 (1984).
⁸R. Winkler, *Spin-Orbit Coupling Effects in Two-Dimensional Electron and Hole Systems* (Springer, Berlin, 2003).
⁹B. Habib, M. Shayegan, and R. Winkler, *Semicond. Sci. Technol.* **24**, 064002 (2009).

¹⁰M. J. Manfra, R. de Picciotto, Z. Jiang, S. H. Simon, L. N. Pfeiffer, K. W. West, and A. M. Sergent, *Phys. Rev. Lett.* **98**, 206804 (2007).
¹¹S. P. Koduvayur, Y. Lyanda-Geller, S. Khlebnikov, G. Csathy, M. J. Manfra, L. N. Pfeiffer, K. W. West, and L. P. Rokhinson, *Phys. Rev. Lett.* **106**, 016804 (2011).
¹²L. Pfeiffer and K. W. West, *Physica E* **20**, 57 (2003).
¹³J. J. Heremans, M. B. Santos, K. Hirakawa, and M. Shayegan, *J. Appl. Phys.* **76**, 1980 (1994).
¹⁴D. Reuter, A. D. Wieck, and A. Fischer, *Rev. Sci. Instrum.* **70**, 3435 (1999).
¹⁵M. J. Manfra, L. N. Pfeiffer, K. W. West, R. de Picciotto, and K. W. Baldwin, *Appl. Phys. Lett.* **86**, 162106 (2005).
¹⁶C. Gerl, S. Schmult, H.-P. Tranitz, C. Mitzkus, and W. Wegscheider, *Appl. Phys. Lett.* **86**, 252105 (2005).
¹⁷E. H. Hwang and S. Das Sarma, *Phys. Rev. B* **77**, 235437 (2008).
¹⁸M.J.M. thanks Ken West and Loren Pfeiffer from Princeton University for sharing their carbon source design on which ours is based.

- ¹⁹J. D. Watson, S. Mondal, G. A. Csáthy, M. J. Manfra, E. H. Hwang, S. Das Sarma, L. N. Pfeiffer, and K. W. West, *Phys. Rev. B* **83**, 241305 (2011).
- ²⁰V. Umansky, R. de Picciotto, and M. Heiblum, *Appl. Phys. Lett.* **71**, 683 (1997).
- ²¹L. Pfeiffer, K. W. West, H. L. Störmer, and K. W. Baldwin, *Appl. Phys. Lett.* **55**, 1888 (1989).
- ²²G. Bastard, *Wave Mechanics Applied to Semiconductor Heterostructures* (Halsted Press, New York, 1988).
- ²³S. Das Sarma and E. H. Hwang, *Phys. Rev. Lett.* **83**, 164 (1999).
- ²⁴S. Das Sarma and E. H. Hwang, *Phys. Rev. B* **61**, R7838 (2000).
- ²⁵Nextnano3 simulator, ©1999–2008, Walter Schottky Institute [<http://www.nextnano.de/nextnano3/index.htm>].
- ²⁶K. Lee, M. S. Shur, T. J. Drummond, and H. Morkoç, *J. Appl. Phys.* **54**, 6432 (1983).
- ²⁷F. Stern, *Appl. Phys. Lett.* **43**, 974 (1983).
- ²⁸J. W. Harrison and J. R. Hauser, *Phys. Rev. B* **13**, 5347 (1976).
- ²⁹D. Chattopadhyay, *Phys. Rev. B* **31**, 1145 (1985).
- ³⁰W. Li, G. A. Csáthy, D. C. Tsui, L. N. Pfeiffer, and K. W. West, *Appl. Phys. Lett.* **83**, 2832 (2003).
- ³¹F. F. Fang and W. E. Howard, *Phys. Rev. Lett.* **16**, 797 (1966).
- ³²T. Ando, A. B. Fowler, and F. Stern, *Rev. Mod. Phys.* **54**, 437 (1982).
- ³³T. Ando, *J. Phys. Soc. Jpn.* **51**, 3900 (1982).
- ³⁴J. H. Davies, *The Physics of Low-dimensional Semiconductors: An Introduction* (Cambridge University Press, Cambridge, 1997).
- ³⁵J. C. H. Chen, D. Q. Wang, O. Klochan, A. P. Micolich, K. D. Gupta, F. Sfigakis, D. A. Ritchie, D. Reuter, A. D. Wieck, and A. R. Hamilton, *Appl. Phys. Lett.* **100**, 052101 (2012).
- ³⁶H. Störmer, A. Gossard, and W. Wiegmann, *Solid State Commun.* **41**, 707 (1982).
- ³⁷H. L. Störmer, Z. Schlesinger, A. Chang, D. C. Tsui, A. C. Gossard, and W. Wiegmann, *Phys. Rev. Lett.* **51**, 126 (1983).
- ³⁸W. Walukiewicz, *Phys. Rev. B* **31**, 5557 (1985).
- ³⁹E. H. Hwang and S. Das Sarma, *Phys. Rev. B* **67**, 115316 (2003).