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ABSTRACT

The use of modified predicate transition nets for the modeling of computer communication protocols is investigated in this paper. The lower three layers of the OSI architecture are of primary concern. On the Network Layer (Layer 3), fragmentation and reassembly, routing, store and forward buffering and congestion control mechanisms are treated. The Data-Link Layer (Layer 2) leads to window-flow control, time-out retransmission and transmission error recovery models. These mechanisms may repeatedly dealt with in the different layers of the computer communication architecture.

Non-prime transitions can be embedded into the modified predicate transition nets hence a top-down modeling is possible. The present paper uses a hierarchical modeling approach to describe complex communication mechanisms in terms of simpler constructs. Models developed using the modified predicate transition nets can be automatically translated into simulation programs. The paper presents the translation of a computer communication model into a program, using a process oriented simulation language, ASPOL.

1. Introduction

The Open-Systems Interconnection (OSI) reference model [1] is a framework for defining standards for interconnection of heterogeneous computers. It partitions the computer communication functions into a vertical set of seven layers. Each layer provides services to the next higher layer, and relies on the next lower layer to perform more primitive functions. Layer \( n \) on one host carries on a conversation with layer \( n \) on another host. The rule and conventions used in this conversation are collectively known as a (peer-to-peer) protocol.

For computing systems and especially for systems of the complexity of a computer network, modeling is essential during system design, implementation and throughout the entire system life. In connection with computer communication protocol design,
modeling is necessary in order to predict the feasibility and the performance of the protocols.

Simulation can be used to evaluate the model of a system after the model has been mapped into a computer program which describes the interesting behavior of the system. A simulation model of a computer communication architecture emphasizes a sufficiently precise representation of protocols and protocol hierarchies.

Some directions in the communication protocol research are:

- Formal protocol specification and validation. The objective is to prove protocol correctness, to avoid inconsistencies and system deadlocks [2-7].

- Protocol performance evaluation. Relevant performance characteristics are the delay of data within a layer as a function of the different values of the layer parameters, the utilization of computer network elements as a function of the network load, etc. An important objective of the performance evaluation is to provide information for the optimal structuring of a communication architecture as well as implementation guidelines for example the amount of memory space needed for protocol implementation on a given host. Another objective of the performance evaluation is to predict the network characteristics important from a user’s perspective as delay, throughput, etc. The research reported in this paper belongs to this category.

- Study of implementation methods allowing translation of the protocol models into program structures.

Very often a hierarchical modeling is possible, a complex system can be decomposed into subsystems. Each subsystem can be modeled separately and its model can be evaluated independently. The behavior of the entire system can be investigated by combining the previous results.

In recent years a considerable effort has been invested into modeling and analysis of computer communication protocols. Two approaches to modeling, namely the finite state automata approach [8] and the simulation language approach [9-12] have been investigated in the past. More recently queueing models have been also considered [13,41]. The Petri net models are used mostly for the specification and validation of protocols [6,7], but they seem a natural tool for protocol performance analysis [14-16].

The introduction of Petri nets can be traced back to the dissertation of C.A. Petri [17]. The theory of Petri nets has been further developed and applied to modeling and analysis of modern computing systems [18-20]. Recent work done on General Net Theory and related models can be found in [21], and surveys of Petri nets in [14, 15, 22].

The capabilities of Petri nets to represent concurrent, conflicting, nondeterministic and asynchronous events are their most useful properties for modeling of computer communication networks. Petri net models are especially suitable to describe the data exchange aspect of the protocols being modeled. Data exchange is generally represented as a part of the certain token exchange in Petri nets. Petri nets can be used to model both the static and the dynamic properties of computer networks. Static properties of networks are represented by the graph part of a Petri net. Dynamic properties of networks can be derived from the Petri net graph, the initial marking and the firing rules.
However, Petri net models suffer from two severe limitations:

- Modeling of a complex system leads to a very intricate and quite unreadable graph.
- Performance evaluation of the obtained model is impractical if the time concept is not introduced into the Petri nets.

Petri nets have evolved over the past decade in order to provide a more compact representation of real systems. The place-coloured nets [23] and the predicate-transition nets [24,25] have been proposed. In both cases the size of the network representing a real system has been reduced by increasing the power of the representation. The resulting nets are more readable. The validation of communication protocols [6,7] had been carried out in the framework of these extension nets.

An important extension of Petri nets is related to the need to embed in the net model the time involved in system operations by allowing timed transitions. One of the first efforts in this direction is represented by E-nets [26]. The main difference between E-nets and Petri nets is the former's introduction of a fixed time delay between enabling and firing of every transition. Another approach proposed [27,28] is to associate with each transition a range of firing time values bounded by a maximum and a minimum firing time. There are also stochastic Petri net models [29-31] in which a random firing time is associated with each transition.

Time can be introduced in the net by associating an exponentially distributed firing time to some transitions so that the Petri nets may include both timed and immediate transitions. Such nets were discussed in reference [14] and applied to the performance evaluation of multiprocessor systems. There is correspondence between such nets and continuous time Markov chains, so the evaluation of the systems can be achieved by classical probabilistic analysis. Recently, the discrete time stochastic Petri nets [32] were proposed.

Predicate-transition nets, enhanced with stochastic transition time, are proposed as a suitable framework for modeling the communication protocols in a computer network. In order to illustrate this, we have considered some common mechanisms used the three lower layer protocols for the ISO reference model. In the first section of the paper a modified predicate-transition net is presented. In the second section, the computer network model based upon the modified predicate-transition nets is analyzed. Finally, the mapping of the network model into program structure is discussed.

2. Modified Predicate-Transition Nets

The Petri nets used in this paper are a modified version of the Predicate-Transition Nets and Generalized Stochastic Petri Nets. The elements of the Modified Predicate-Transition Nets are the following:

1. **Token types**

   In the modified nets there are three types of tokens.

   **Type 1** Tokens with no attribute. They are used to represent the synchronization operations among concurrent activities.

   **Type 2** Tokens with one attribute only. The attribute is an integer which may represent for example the value of a counter.
Type 3 Tokens with multiple attributes. The first item in the attribute record is used to identify the token subtype. Each subtype represents a different data unit exchanged by the communication protocols. We recognize the following subtypes: message, packet, frame, and bit stream. A token representing a message has three attributes, subtype=m, destination address a, and message length l. A token representing a packet has six attributes: subtype=p, the packet sequence number s, the destination address a (copied from the message), the packet length l, the last packet in a message flag la, and the neighbor to neighbor packet sequence number s1. A token representing a frame has eight attributes: the subtype=f, the data link sequence number s2, the packet type (data,ACK, NAK, res, ref, etc.) and the last five attributes are copied from the packet. A token conversion process occurs whenever the corresponding data unit crosses the boundary of a communication layer and it corresponds to the encapsulation and decapsulation process performed by the different protocol layers.

(2) Places
They are the first type of nodes in the graphs. A place is represented by a circle and has a name consisting of one or more upper-case characters. A place can contain a finite number of tokens, determined by its capacity. We distinguish two types of places: places of the first type are used to represent the queues of interest in the performance evaluation of system and they contain Type 3 tokens. Places of the second type are used to represent system environments.

(3) Transitions
Transitions are the second type of nodes in the graphs. A transition is represented by a bar or a rectangle and has a name consisting of one or more upper-case characters. Nonprime transitions representing model subnets are represented graphically as rectangles. This possibility enables top-down hierarchy structuring and information hiding. A similar structuring method for distributed software system design has been discussed in [34]. Predicates can be inscribed on transitions: they specify relations between variables of different tokens from the input places of the transitions. It is possible to evaluate the interesting performance aspects in the modelled system by introducing "time" into the transitions [14, 33]. There are two types of transitions: timed and immediate. An exponentially distributed random time (possibly marking-dependent), denoted by T( ), between enabling and firing of a transition can be associated with timed transitions only.

(4) Arcs
Arcs connect transitions and places together. The arcs are labelled with token variables. Operations can be inscribed on outgoing arcs of transitions. An operation performs a computation or a change of the attributes carried by the tokens from the input places, and it forms tokens to be inserted into the output places. In our modified nets multiple arcs between a place and a transition are allowed, and the number of such arcs may vary from zero to a finite
value. In the followings we will show that this extension does not change the property of the predicate-transition nets, but it makes more convenient to describe some mechanisms of the protocols. The variable arc is represented graphically by an arc crossing a small circle, and has an associated range expression.

(5) Firing rule

A transition is enabled when there is at least one token in each of its input places and the predicate associated with the transition is satisfied. If there are the multiple arcs between the input place and the transition, then the transition is enabled when the number of tokens in the input place is at least equal to the number of arcs and the predicate is satisfied. An immediate transition fires immediately after being enabled. When the timed transition is enabled, it fires after a random enabling time, x. The enabling time, x, is exponentially distributed and it is specified by the T(x) associated with the transition. However, the firing of a transition is considered to be instantaneous, so the probability of two or more transitions firing simultaneously is zero. The firing of a transition consists of two steps:

a) removing the tokens (satisfying the predicate) from the input places;
b) adding tokens to the output places after performing the operations specified on the outgoing arcs.

In our model the distribution of the time x associated with a timed transition depends upon the system environment. The main difference between the nets used in this paper and the predicate-transition nets are the introduction of time and of variable arcs (a variable number of arcs may connect a place and a transition, and this number may range from zero to a finite value).

In our paper the following notations are used: \( \oplus \) stands for addition modulo the size of the sequence number. \([x, y]\) denotes the set of integers from x to y, including the lower and the upper bound while \((x, y)\) excludes x and \([x, y)\) excludes y. Due to the modulo operation, it is possible that the set of sequence numbers of the messages to be sent (received) might not be in the number value order. For example when the size of the sequence number of the frame \( M_2 = 8 \) (three bits are used for the frame sequence number), the following frames may be in the sender’s window: 6, 7, 0, 1. To illustrate the sequence relation, the symbol \( \rightarrow \) is used. In the example above, we can say 6 \( \rightarrow \) 1, 7 \( \rightarrow \) 0, 6 \( \rightarrow \) 7, etc. \(| \{ \} |\) denotes the cardinality of a set. For example, \(|\{a, e, d\}|\) is equal to 3. In addition, the relations between the element and the set are often used in the predicates. If a element is contained by a set, this relation is denoted by \( \in \), on the contrary, by \( \notin \). For instance, we can say 3 \( \in \{1,4\} \) and 4 \( \notin \{1,4\} \).

In our model nets, we often use a place representing a counter as an environment state variable in order to control the probability of firing a transition. Such values are presented in the predicates as individual token attributes. From the reference [14], we know the bounded place marking can be tested. The value of the counter or the set element in the model can also be tested and changed, including testing for zero.

The variable-arc nets are useful to model the network protocols, for instance to model the fragmentation of a message of a given length or to model the operation of multiple elements of an entry (queue, set, etc.).
The correspondence between a variable-arc net and a predicate transition net will be discussed in connection with two examples used to model mechanisms of a network layer protocol and of a data link layer protocol.

Example (1). The Fragmentation Mechanism. The network layer breaks up a message into several packets. Two models of this fragmentation mechanisms are presented in Figure 1. In Figure 1.(a) a variable-arc net is used to describe the mechanism. \( X \) represents the arc variable. It is assumed that the maximum length of a packet is 128 bits and the maximum message length is 384 bits hence \( X \) varies in the range 1 to 3.

The following transitions occur in our model:

- **US** is a transition representing the arrival of a message from a user. Messages arrive according to a Poisson distribution with average arrival rate \( \lambda \).
- **FR** is a transition representing the fragmentation process. This transition fires only once, when the message is received, hence the firing condition for transition \( FR \) is: \((f_n=0) AND (0<i<348)\). When it fires, a number \( X \) of packet tokens are created and deposited in place \( PS \). \( X \) depends upon the actual message length, \( l \).
- **SEN** is a transition representing the sending of the next sequential packet to the output queue (place \( OUT \)).

We now focus our attention upon the places present in our variable-arc net and upon the attributes of each type of token allowed in any given place.

- **SQ** is a place containing tokens that represent messages, and have three attributes:
  - \( m \) : token subtype (message);
  - \( a \) : destination address;
  - \( l \) : message length.

- **PS** is a place containing tokens that represent packets. Such a token has four attributes:
  - \( p \) : token subtype (packet);
  - \( a \) : destination address (copied from the message);
  - \( l \) : packet length;
  - \( l_a \) : last packet in a message flag, used in reassembly.

A variable arc connects the transition \( FR \) to the place \( PS \). Consequently a variable number of packet tokens are deposited in place \( PS \) when the transition \( FR \) fires.

- **S** is a place containing tokens representing the sequence number counter, \( s \). Whenever the transition \( SEN \) fires, this counter is incremented modulo \( M_0 \).
- **FN** is a place containing the counter \( f_n \) of packets left in place \( PS \). When the transition \( FR \) fires, the value is set to \( X \), the number of packets created from the incoming message. Whenever the transition \( SEN \) fires, the value is decreased by one.

An equivalent model for the same mechanism is presented in Figure 1.(b) but a predicate-transition net is used instead of a variable-arc net. The complexity of this model is considerably increased. Instead of a single transition \( FR \) now we have the set of \( FR_i, i=1,2,3 \). The predicate associated with \( FR \) is the combination of all predicates associated with \( FR_i \).

Example (2). The Frame Reject Mechanism. In a data link layer protocol the receiver of a frame with sequence number \( i \), may inform the sender that it does not want
to accept the frame, by sending a reject command, \(<nak,i>\). A Go-back-N continuous
ARQ (Automatic Repeat Request) [42] technique for error control is used in our exam-
ple.

In our model, when a token representing a reject command is received, all tokens
representing frames in the sender's window and with a sequence number succeeding the
rejected frame are deleted from the time out queue, place TQ, in Figure 2. The possi-
bility that there is no token to be deleted, because retransmission has already been per-
formed (e.g. the time-out has occurred) is also taken into account in our model.

The places and the associated tokens have the following meaning:

- **S1**: is a place associated with a counter representing the sequence number of the frame.
  Its current value is denoted by \(s_1\).

- **PR**: is a place holding the reject token, associated with the receiving of a reject com-
  mand. Such a token has two attributes:
    - \(nak\) : token subtype;
    - \(i\) : the sequence number of the rejected frame.

- **TQ**: is a place holding tokens with two attributes:
    - \(x\) : the sequence number of the frame registered.
    - \(t\) : the time-out associated with frame \(x\) (omitted here).

- **RS**: is a place representing the retransmission control set which contains the sequence
  number of the frames that will be retransmitted.

The number of arcs from the place TQ to the transition TR is variable from zero to a
finite integer as shown in Figure 2.(a), depending upon the number of tokens contained
by the place TQ.

The equivalent model without the zero changeable arc is presented in Figure 2.(b).

The transition TR\(_2\) occurs for all frames with a sequence number \(x\) in the range \([i,s_1]\), and
as a result, the corresponding retransmission frame tokens are deleted from the place TQ.
The variable arcs from the place TQ to the transition TR\(_2\) and those from the transition
TR\(_2\) to the place RS both are changeable from one to a finite number. The arcs connect-
ing the place TQ and the transition TR\(_1\) represent the testing for place TQ, including possi-
ibly zero testing, i.e., testing whether there is any token in place TQ. The enabling con-
dition for the transition TR\(_1\) is the opposite condition as the one for the transition TR\(_2\),
and the firing of TR\(_1\) has no effect upon the the place RS, where tokens representing
frames waiting to be retransmitted are deposited.

3. The Computer Network System Model

The Reference Model of Open Systems Interconnection (OSI) has seven layers.
The syntax, the semantics and the timing associated with the communication between peer
entities, located at the same layer, on different systems are collectively called protocols.
Each communication layer has a different function hence the protocols for different
layers are different. Nevertheless, some of the protocol primitive functions can be
identified in more than one layer. A non exhaustive list of such functions contains frag-
mentation and reassembly, encapsulation, connection control, flow control, error control,
synchronization, sequencing, etc.
This paper is focused upon the first three layers of the OSI Model, the Network Layer, the Data Link Layer and the Physical Layer. The methods developed can be extended to cover the protocols for other layers. In the network model shown in Figure 3, the concept of using non-prime transition for modeling of the functions related to different network layers is illustrated. This shows that the modeling technique based upon modified predicate transition nets, presented in this paper, is capable to take advantage of hierarchical modeling concepts and a top-down modeling approach is possible.

The communication between two transport layer entities, each with multiple data link connections is illustrated in our example. Since processes within layers operate asynchronously, queues at layer interfaces are a necessary part of the network model. Each layer protocol entity has associated with it four queues: a send and a receive queue to (from) the upper layer, and a corresponding pair connecting to the next lower layer. A protocol entity is represented as a non-prime transition, e.g. the network layer entity is represented by the Fragmentation, Reassembly, Routing, Buffering, Congestion non-prime transition which will be examined in more detail in the next section. A queue is represented as a place, e.g. $SQ_i, RQ_i, FQ_i, EQ_i, LQ_i, IQ_i$. It is assumed that the transport entities generate messages according to a Poisson distribution $T(\lambda)$ with mean arrival rate $\lambda$. The distribution of the message length is reflected in the length attribute of the message token. The transitions $US_i, UR_i$ represent the sending and the receiving of messages to and from the transport entity.

In our model, the communication between the protocol entities, (peer-to-peer), may be full-duplex. Only the data transition phases are investigated, modeling of connection set-up and of connection termination process have been investigated elsewhere [3,6,7] and will be omitted here. Nevertheless their effect on the performance of the system will be taken into account by considering the firing time of the corresponding transitions.

3.1. Layer 3: Network Layer

In Figure 4. we describe the network layer model using non-prime transitions. Each non-prime transition represents a mechanism of the protocol and it can be extended as a subnet.

3.1.1. Fragmentation and Reassembly

The Fragmentation and its corresponding Reassembly model are presented in Figure 4. The Fragmentation model has been discussed earlier, in Example 1, and we focus our attention on the Reassembly model, namely how several packets are put together into a message to be delivered to the upper layer. In case of Reassembly, transition REC corresponds to the receiving of a packet, and it fires whenever a token is placed in the input place IN and the receiver counter value $r$ equal to $s$, the sequence number of the packet received. This keeps the receiving packets in sending order.

The following places are presented in our model:

- $R$ is a place related to the sequence number of the next packet expected. The current value of this counter is denoted by $r$. Whenever the transition REC fires, the value $r$ is incremented modulo $M_0$.
- $PR$ is a place containing tokens which represent packets. It is the correspondent of the place $PS$ in the fragmentation model. It contains tokens with four attributes.
which have been described in Example (1). When the last packet arrives, i.e., when a token with $l_a = 1$ arrives at the place PR, then the transition RE fires. After firing, all tokens are removed from the place PR and a token of subtype message is put in the place RQ.

RQ is a place containing tokens which represent received messages, hence it is associated with the received message queue. It is the correspondent of the place SQ, the sent message queue, from Example (1) and contains tokens with identical attributes.

3.1.2. Routing

Routing is an important function of the network layer of any packet switched network. Different routing strategies ranging from fixed to adaptive routing are used in existing communication networks. In case of adaptive routing the updates can be periodic, or they can be triggered by major load or topology changes in the network. The selection of a route is based upon a certain performance criterion as delay, cost, throughput. The routing decision can be made using local information only, information from adjacent nodes, or from all nodes of the network. The routing decision can be made for each packet individually in case of a datagram type of service or it can be made only once, when a virtual circuit is established. The routing decision can be made by each node (distributed routing), by a central node (centralized routing), or by the originating node (source routing).

A distributed adaptive routing mechanism with updated triggered by major changes, for a packet switched network operating internally as a datagram is embedded in the network model presented in Figure 4. The routing table RB is represented by a place and it is updated at random time intervals, $\nu$, associated with firing of the transition RDU. The routing table has $N$ entries, one for each node of the network. Each entry consists of two items, the destination node id and the the output line or the next node to which the packet is to be delivered. Update vectors are received periodically by each node from its neighbors. Each update vector contains entries with the same format. The places RB and NRB contain tokens with two attributes: $x$ and $y$ as described above. The arc label N indicates that there are $N$ arcs. Functions $f_1$ and $f_2$ represent the updates for an entry in the routing table.

The routing table is used for every packet to decide which is the optimal route, and then the token associated with the packet is passed to the proper Buffering and Congestion control mechanism.

3.1.3. Store and Forward Buffering and Congestion Control

Long haul computer communication networks, and the interconnection networks, the catanets, are multi-hop networks, operating in a store and forward manner. The intermediate nodes buffer messages, route them, and then free the buffers only when the acknowledgements for the buffered messages are received. Clearly, the buffer space is a critical resource of an intermediate node whether this is an IMP (Intermediate Message Processor) or a gateway processor. Whenever such a node runs out of buffer space it starts discharging incoming packets and this may trigger a chain reaction affecting an entire region of the network. The problem of buffer management is closely related to the
mechanisms for traffic control in a packet switched network. The traffic control problem has multiple aspects namely the flow control, the congestion control and the avoidance of deadlocks. The flow control is used to regulate the traffic between two different points. The congestion control has the objective to maintain the number of packets within the network or within a region of the network below some critical values.

A rather simple congestion control mechanism is modeled in the graph presented in Figure 5. An intermediate node maintains a low water mark, \( M_l \) and a high water mark, \( M_h \). Whenever the amount of used buffers reaches \( M_l \), the node informs its neighbors that it will no longer accept any messages by sending a \(<\text{ref}>\), REFUSE control packet. When the amount of used buffer space decreases below \( M_l \), then the node becomes friendly again, sends to its neighbors a \(<\text{res}>\), RESUME control packet and starts accepting messages.

We focus our attention upon the congestion control mechanism sketched above. In order to simplify the graph (Figure 5), we consider only one host and one neighbor node connected to the node under examination. Some attributes of the tokens representing packets are omitted in the graph, for example the attributes \( l_1, l_a, s \), are not represented though the tokens contain them.

The flow of the tokens representing packets is as follows: tokens are deposited by the data link entity in the place \( \text{EQ} \). Depending upon the type of the packet, different transitions take place. For example the arrival of data packets triggers the transition \( T_{12} \) and depending upon the destination address, the tokens representing packets for the local host trigger transition \( T_{13} \) and end up in place \( \text{IN} \) while the tokens for the other hosts trigger transition \( T_{14} \), are transmitted to the place \( \text{OUT} \) and go through the routing mechanism previously described.

The places and attributes of the tokens they contain are:

\( S_1 \) is a place representing a counter, namely the sequence number of the next packet to be sent on the outgoing link. Its current value is denoted by \( s_1 \). Note that there is no need to represent the place \( S \), the end-to-end packet sequence number.

\( \text{BUF} \) is a place representing the store and forward buffer. It contains tokens of subtype packet, with six attributes. In addition to \( s_1 \) the remaining five attributes are \( p, a, l_1, l_a \) and \( s \) are as in the case of tokens in Place \( \text{OUT} \) of Example (1).

\( \text{BC} \) is a counter of the number of buffers in use, it reflects the occupancy of \( \text{BUF} \). Its current value is \( b_c \). It is incremented when a new packet arrives and buffer space is allocated to it and it is decremented when the buffer space is released. It has a maximum capacity, \( M \).

\( P_6 \) is a place where tokens representing data packets are deposited.

The transitions shown in Figure 5 are described in the followings:

\( T_2 \) occurs when an explicit acknowledgment for packet \( i \), \(<\text{ack},i>\) is received. Then the buffer holding packet \( i \) is released and a token is removed from the place \( \text{BUF} \).

\( T_3 \) occurs when a negative acknowledgment for packet \( j \), \(<\text{nak},j>\) is received. Then the proper token is first removed, then put back in the place \( \text{BUF} \) through the self-loop arc. In addition, when \( T_3 \) fires a token is put in the place \( P_3 \) which
contains tokens representing packets to be retransmitted.

T4 occurs when the high water mark, $M_h$ is reached and the current node sends a <ref>, REFUSE control packet to its neighbors.

T5 occurs when the low water mark, $M_l$ is reached and the current node sends a <res>, RESUME control packet.

T6 if the final destination of a packet is a host connected to the immediate neighbor of the current node, the buffering of the packet is not under the control of the congestion mechanism and the transition is T6 enabled. The predicate (D2=a) is true when the immediate neighbor condition is satisfied.

T7 the enabling condition of this transition is the opposite of the enabling condition for transition T6.

T8 occurs when the current node receives a <ref>, REFUSE control packet from its neighbors. It shows the action of congestion control. In this case the transition T7 cannot fire until T9 fires (a <res> control packet is received).

T9 occurs when a <res>, RESUME control packet is received from its neighbor.

T11 occurs whenever a packet is sent on the output line. The predicate associated with this transition represents its firing condition, where LINE is related to the Buffering and Congestion address on the output line determined after checking the routing table.

3.2. Layer 2: Data Link Layer

A model of the Data Link Layer is presented in Figure 6. A sliding window flow control mechanism coupled with a GO-Back-N, continuous ARQ, error control mechanism are embedded into our model. The set of the frame sequence numbers has a size $M_2$.

The sender’s window is denoted by $W_s$ and the receiver’s window by $W_r$. Acknowledgments are sent in separate frames and an <ack,i> means that frame i and all frames preceding it are acknowledged. <nak,j> requires that frame j and all succeeding frames in the sender’s window be retransmitted.

As the tokens travel across layers boundaries new attributes are added (deleted) to (from) them. This process corresponds to the encapsulation (decapsulation) when data units cross from one protocol layer to another. Header information is added when the data units flow from higher to lower layers and it is removed and interpreted for the opposite direction of the flow.

In our model all tokens contained by the place FQ represent packets and they will be converted into tokens of subtype frame. In addition to the original attributes, two new attributes are added to each token in the place FQ: subtype attribute f and the data link sequence number s2. This is performed by the transition T21 in Figure 6. In order to simplify the arcs labelling the token attributes not used by the current layer are omitted in the graph.

In the graph represented in Figure 6 the following places can be recognized:

S2 is a place representing the data link sequence number of the next packet to be sent. Its the current value is s2.
R is a place representing a counter associated with the lower limit of the sender's window. Its value is updated every time an acknowledgment is received. Current value is denoted by r.

RS is a place which contains the set of the sequence numbers of the packets to be retransmitted. The element variable is denoted by l and the set variable by rs.

RC is a place containing the data link sequence number of the next packet to be received, the current value is denoted by rc. After receiving the packet which it is awaiting, this lower limit of the receiver's window is updated.

PC the set of the frames which are within the receiver's window, the frame sequence number is in the range, (rc, rc ⊕ W_r), excluding the duplicate elements.

RTQ is a place associated with the frame retransmission queue. When sending a frame (including retransmission), a token of subtype frame is put in this place; when an acknowledgement is received, the proper tokens are removed from this place.

TQ is a place associated with the time out queue. It contains tokens with two attributes:

- x--the frame sequence number;
- t_v-- the time out associated with frame x.

The transitions present in our graph are:

T21 it represents sending frames. When a token from the higher layer arrives at the place FQ and the predicate is satisfied, since s2 is in the sender's window, (s2 ∈ [r,r ⊕ W_s]), and there is no retransmission occurrence (rs=∅), then transition T21 can fire. After firing, the token representing a frame is delivered to the lower layer and to the retransmission queue RTQ. In the same time a token of time out subtype is put in time out queue TQ and then s2 is incremented (s2=s2 ⊕ 1 (modulo M_2)).

T22 it represents frame retransmission. When there is requirement for retransmission, i.e., rs=∅, the transition T22 can fire. After firing, the action is similar with the transition T21. The difference is that the value s2 is not changed and the proper sequence number is removed from the place RS.

T23 After receiving an acknowledgement token <ack,i>, this transition can fire. The proper elements of the queue RTQ and TQ and the set RS are canceled if the sequence numbers of these elements are → i (including i), and the value of r is modified, r=i ⊕ 1 (modulo M_2).

T24 After occurrence of a time out, all elements of the queue TQ are removed and the tokens are put in the place RS.

T25 After receiving a <nak,j> token, this transition can fire. The action is like that of the transition T24.

Tt It represents time out. Every t_v units of time this transition can fire if there is any token < x, t_v > in the queue TQ.

T26 When receiving a frame in error, a <nak, a> is sent if the frame sequence number is rc=a.
When receiving an error-free frame with the sequence number \( rc = b \), an acknowledgement token \(<\text{ack}, b>\) is sent. Then \( rc \) is increased (\( rc = h \oplus 1 \) (modulo \( M \))) and the tokens representing frames with sequence numbers in the range \([b, h]\) are removed from the place PC, if any. After this transition fires, the transition T30 is enabled.

It represents the receiving of error-free frames which are in the range of receiver’s window, but which are duplicated frames. After firing, this transition puts the frame token into the place P8 and the sequence number into the place PC.

It represents the discard of other frames including the duplicated ones.

It delivers the frames to the higher layer in sending order. After firing, it puts the frame in the place EQ, i.e., it removes the two attributes of the token, which were added when this token entered the data link layer at the sender’s site.

3.3. Layer 1 : Physical Layer

The physical layer of a computer communication architecture is concerned with the transmission of streams of raw data bits over a communication channel. We model a time division multiplexing scheme with \( n \) slots so that \( n \) streams of data can be exchanged through the same channel. All slots are of the same length (expressed in number of bits). The fact that the slots may not be fully occupied is reflected into the time function of the timed transition which represents the physical propagation of data.

We assume a full duplex communication and we use two queues to model the two propagation directions on the medium. Each is a FIFO queue with \( n \) slots and it can be described by Petri nets as in Figure 7. This subnet is replaced by the places LQ and IQ at a higher level as shown in Figures 3 and 6 respectively. Such a subnet is fully described in reference [7].

The places and tokens which are allowed to visit them have the following meaning:

- **Pf**: It contains tokens which represent occupied (full) slots. Such tokens have two attributes: the first one is the subtype of stream contained by the slot and the second one is the slot number.

- **Pe**: It contains tokens which represent empty slots. These tokens have only one attribute, the slot number.

The place Pq and Pr contain separately the receiving and sending streams.

The transition Ts and Tr constitute the interface of the queue. Ts can fire, if the first slot is empty, i.e., Pe contains the token 1 and a stream presents in Pq. After this transition fires, the first slot is removed from Pe and is put in Pf with attributes \(<m, 1>\). Conversely, Tr can fire, if the last(nth) slot is contained by Pf. After it fires, the last slot is removed from Pf and is put in Pe with one attribute \( n \).

The transition Tp stands for the progression of stream from one slot to the following one. Whenever place Pe contains a token \( p \), i.e., the slot \( p \) is empty, and the place Pf contains a token of stream subtype \( c \) which slot number is \( p-1 \), the transition is enabled and waiting a random time \( b*p \), it can fire. Then the stream of subtype \( c \) is put in the slot \( p \), and the slot \( p-1 \) becomes empty, i.e., the token \( p-1 \) is put in Pe. The random time \( b*p(l: \text{the stream length}) \) denotes the the delaying time of a slot transmission.
The transition $T_d$ stands for stream loss during transmission. Every random time $w$ period the transition can fire if the transmission medium is not idle. When it fires, it simply discards a stream of subtype $i$ and puts the slot occupied by the stream into the place $P_e$.

The transition $T_e$ stands for corruption of stream during transmission. Every a random time $u$ period, a token of subtype $e(error)$ may substitute for a stream of subtype $x$ in the slot $y$.

4. Translation of Protocol Models into Simulation Programs

The models of the communication protocols developed in the previous section can be translated into simulation programs. The target language can be any programming language which supports concurrent processing. We have selected ASPOL since it is a process oriented simulation language which in addition to concurrent processing provides an adequate support for simulation constructs.

The mapping of Petri nets and of extended Petri nets into programming structures has been investigated in the literature [35-37]. In case of Petri nets a process can be associated with a connected subnet in which every transition has at most one input arc and one output arc from (to) any input (output) place. Other methods have been proposed recently, [38-40]. However the method used in this paper is conceptually different, and easier to use. It partitions the set of all places into two disjoint classes and associates with one class synchronization primitives and with the second one processes. We recognize different types of tokens and we associate with each of them a different type of process.

Two types of places can be distinguished in our previous models which are based upon modified predicate transition nets:

a. **Type e places.** They may contain Type 1 or Type 2 tokens which are associated with predicates that decide upon the opportunity of firing a transaction. The correspondent of such places in our simulation structures are primitives to control the synchronization between the processes executing concurrently in the simulation programs.

b. **Type m places.** They may contain only Type 3 tokens which are associated with the transmission units exchanged by the corresponding protocols. For example, in the data link protocol, the basic transmission units are data frames, acknowledgment, negative acknowledgment frames. In our model they are represented by different subtypes of Type 3 tokens. In the network layer there are: data packets and different types of control packets. In this section, unless it is explicitly stated otherwise, all tokens are assumed to be Type 3 tokens. Each different token subtype will be associated with a process type. The number of concurrent processes of a given type equals the number of tokens of the corresponding subtype. A process will in fact describe the the migration of that particular token through all the places it visits in the system.

Each entity at a given network layer can be conceived as consisting of two basic agents, the sender and the receiver, and in some cases of additional auxiliary components. Each component will be mapped into a different process. The activities of the two primary agents consists of: interfacing with the immediate upper neighboring layer, the specific processing associated with the current layer and interfacing with the immediate lower
layer. Both handle the same type of transmission units (frames, packets, etc.) but they are concerned with the flow of transmission units in different directions. For example in case of the network layer we recognize a packet sending and a packet receiving process and in addition a packet retransmission process and a routing table update process which for the sake of simplicity will be omitted in our discussion.

To illustrate the translation technique from the modified predicate transition net model to the simulation program, we present in Figure 8, the basic types of processes, the packet sending, packet receiving and packet retransmission. Each structure identifies the range of the corresponding process activities and the path followed by the respective token type. A *type m place* is associated with a sequential code in the corresponding process. When a process (remember that a process is associated with a Type 3 token) visits such a place the program counter is position to execute the next sequence of instructions. The firing of a transition determines the execution of the next sequential code section. Whether the transition can fire or not, this depends upon the predicate associated with the transition, if any. If a predicate is associated with the transition then it should be checked according to the label variables of the input arcs associated with the transition. Then the sequential code is executed. Usually it will compute some environment variables and modify some attributes of tokens. These operations are shown by the labels of the output arcs associated with that transition.

In ASPOL, a process description specifies the behavior of a type of processes and defines variables and events unique to each process of that type. Each process is a particular and independent instance of a execution of a process description.

In Appendix, we give three process descriptions of packet type, which were written in ASPOL. The *sendp* (send packet) process executes first the operations associated with transition T11 from Fig.5. These operations are: routing table lookup to determine the output line and checking the availability of that line, by evaluating the predicate associated with T11. If the predicate which is related to buffer occupancy on the selected output line is not satisfied, the process waits until the predicate becomes true. If the predicate is true, then the transition fires and it triggers the execution of subsequent operations: computation of the sequence number and the buffer counter, addition of the packet sequence number into token attribute record, creation of a *retrap* (retransmit packet) process, and decision whether to create a *sref* (sending refuse) process. The place P3 is a decision place because it has multiple output arcs. The program branches at this place according to the attribute value of the destination address. If the predicate associated with the transition T7 is satisfied and the variable P4 is held, i.e., the refuse command is not received, the only operation associated the transition T7 (including T6) is to hold the process for a random time interval. If P4 is empty, i.e., the refuse command has been received, the process waits until the receiving resume process wakes it up. Finally, the process arrives at the place FQ, it is substituted for a sending frame process, *sendf*. The *retrap* process and the *recep* (receive packet) process are simpler and their description will be left as an exercise for the reader. The creation, termination and synchronization of processes will be discussed later.

The *Type m places* are in turn classified into three groups:

a) Places which accept as input tokens of two or more different subtypes. In the graph, such places are nodes with two or more input arcs labelled with token variables of different subtypes. For example places P3 and FQ in Figure 5 belong to this group.
Tokens of two different subtypes are also in place P3 since a retransmitted packet is specially identified. Place FQ contains different types of tokens corresponding to, ref, res, ack, nack control packets and the data packet, p. This indicates that different type of processes may execute the same operations in steps to follow. At these places, we may combine such processes into a new process, since they execute the same sequence of operations and this reduces the complexity of our simulation programs.

b) Places which allow as output two or more different subtypes of tokens. In the graph, there are two or more output arcs emerging from such a node, labelled with token variables of different subtype. The places EQ in Figure 5 and IQ in Figure 6 are examples. These places are decision nodes of the programs. The tokens of different subtypes contained by the place can cause that the different transitions are executed. At these places, it is possible to substitute several types of process for the original one.

c) Places where no transformation of the process type can occur.

The transitions associated with process creation and termination are of special concern for the generation of simulation programs from modified predicate transition nets models. The following types of transitions can be recognized:

Fork The transitions for which the number of output arcs (labelled by token variables of type 3, the following is the same denotation) is larger than that of input ones correspond to a fork operation. For example, referring to Figure 5., the transition T11 corresponds to a fork operation. When this transition fires, some new processes are created. The number of the new processes created is the difference between the number of output and input arcs. The transition T3 is another example. Whenever T3 is executed, the packet process is created while the original one still exists.

Join The transitions with more input arcs than output arcs correspond to a join operation. When such a transition fires, some processes terminate their execution. The number of terminating processes is the difference between the number of input and output arcs. For instance, whenever the transition T2 is executed, the receiving ack process and the certain retransmitting frame process are terminated.

Synchronization among processes is represented by transitions to or from places of Type e. If a transition is associated with a predicate concerning with the attributes of tokens of type 2 contained by its input places or if a input place of a transition can contain a token of type 1, generally we can identify a synchronization topology. For example referring to Figure 5, the input place P4 of transition T7 can contain a Type 1 token. This is not true for transition T6 since the predicate associated with it contains only Type 3 tokens. For transition T11 the predicate is concerned in the value of token bc contained by the place BC. When a process executes such a transition, it should decide whether it waits or not. If the predicate is not satisfied the process waits, else it continues.

If a transition is associated with updating Type 1 or Type 2 token variables then one may identify a synchronization topology. In Figure 6, the place R connects the transition T21 and T23. When a process executes the transition T23, the process would like to update the token variable r contained by the place R. It is possible this process wakes-up
other processes which wait to execute transition T21. In Figure 5, the place P4 connects the transitions T7 and T8. There is synchronization between the sending packet process and the receiving packet process, because the receiving ref process would like to remove the token contained by the place P4.

Most of the synchronization problems can be treated in the framework of Petri nets or modified Petri nets. As two examples in last paragraph, the former is a classical producer-consumer synchronization, the latter is a mutual exclusion problem.

5. Conclusion

A significant part of the performance analysis of a computer communication architecture is related to the modeling of communication protocols supported by the architecture. The communication architecture investigated in this paper is based upon the OSI Reference Model. Queuing models and analytical methods [41] have been used for this purpose.

In this paper we take a different approach. We define modified predicate transition nets and use them to model the mechanisms built into different protocols. While Petri nets have been used in the past to prove the correctness of protocols, by introducing the time concept and the variable arc concept, we are able to use modified predicate transition nets for the performance analysis of communication protocols. A two step approach is presented, first we built the graphs which model the protocol behavior and then we translate these graphs into simulation programs.

Since our models can include non-prime transitions we are capable to represent intricate communication mechanisms using simpler ones as building blocks. Using this hierarchical modeling approach we model first mechanisms like frame rejection, data link flow control, fragmentation and reassembly, etc., then we model the function of an entire layer, for example the network and the data link layers.

We believe that the modified predicate transition nets can be successfully used as a framework for the study of communication protocols and that they can be applied to the performance evaluation, specification, validation and implementation phases.

Reference


[37]. R. Janicki, "Nets, Sequential Components and Concurrency Relations" Theoretical Comp. Sci. 29, PP. 87-121, 1984
Appendix: Examples of Program Structures

```
sim net;  
  
  def (nod=5); comment number of the node;  
def (line=4); comment maximum line number with a node;  
def (m1=16); comment modulo of packet sequence number;  
def (m=10); comment buffer maximum capacity;  
def (mh=8); comment buffer high water mark;  
event out(line); comment event set of output queue;  
event con(line); comment congestion semaphore;  
event rq(m1); comment event set of retransmission queue;  
macro cm; comment defining a referencing block's;  
  block com; comment defining a storage space shared;  
    integer rb(nod,nod,2); comment routing table, each row contains  
      destination and line number;  
    integer s1(line); comment counter of packet sequence number;  
    integer bc(line); comment buffer capacity counter;  
    integer p1(line); comment sending ref control flag;  
    integer p2(line); comment sending res control flag;  
    integer p4(line); comment receiving ref control flag;  
    integer ad(nod,line); comment post neighbor table;  
    integer rtq(line,m1); comment retransmission state variable;  
  end block;  
end macro;  

end sim;
```

Comment the meaning of the following arguments in processes
a: destination address, sou: source address,
s: sequence number of packet(end-to-end),
s1(j) or ss1: sequence number of packet(point-to-point),
j: the number of output line;

Comment send packet process description;

```
process sendp(a,s,sou);
  integer i,j,a,s,sou,f1;
  cm; comment introducing the common data space;
  comment checking the routing table to decide output line;
  i=0;
  while(i.lt.nod)do
    begin
      if(rb(sou,i,1).eq.a)then
        goto g;
      i=i+1;
    end;
  g: j=rb(sou,i,2);
```
begin

comment deciding whether or not buffer is full;
if(bc(j).ge.m)then
  queue(out(j));

comment computing the counters;
s1(j)=mod(m1,s1(j)+1);
bc(j)=bc(j)+1;

comment deciding whether to create sref process;
if(bc(j).eq.mh)then
  if(plG).eq.l)then
    begin
      plG)=O; p2(j)=1;
      initiate sref(sou,j);
    end;

comment creating retrap process;
initiate retrap(a,s,s1(j),sou,j);

comment deciding congestion;
if(a .ne.ad(sou,j))then
  if(p4(j).ne.1)then
    queue(con(j));

comment delaying time of interface and connection;
hold(random(1.,5.)*.001);

comment substituting send frame process for this one;
t1=1;

comment setting frame type;
initiate send(t1,a,s,s1(j),sou,j);

end process;

comment retransmit packet process description;

process retrap(a,s,s1,j); integer a,s,s1,j,t1;

comment introducing the common data space;

comment waiting for being woke;
queue(rq(s1+1));

comment deciding whether ack or nak has been received;
if(rtq(j,s1).eq.1)then goto v;

comment creating retransmit packet process;
initiate retrap(a,s,s1,j);

comment the following is same with that of sendp process;
if(a.ne.ad(sou,j))then
  if(p4(j).ne.1)then
    queue(con(j));

hold(random(1.,5.)*.001);
t1=1;

initiate sendp(t1,a,s,s1,j);

v: rtq(j,s1)=0; comment reset the ack flag;

end process;
comment receive packet process;

process recep(a,s,ssl,sou,j,me);
  integer a,s,ssl,sou,j,me;
comment introducing the common data space;

comment creating sending ack process;
  initiate sack(ssl,sou,j);
  hold(random(0.,3.)*.001);

comment deciding whether the packet is mine;
  if(a.ne.me)then
    initiate sendf(a,s,sou); comment delivering it;
  else initiate recem(s,sou); comment receiving it;

end process;
X=\text{INT}(I/128)

where \text{INT} is a function of truncation to nearest integer not smaller than the argument

1.(a) Fragmentation modeling using a variable arc net

The following predicates associate with the transition \( FR_i \) \((i=1,2,3)\):

- \( FR_1 \): \((fn=0) \land (0<1\leq348)\)
- \( FR_2 \): \((fn=0) \land (128<1\leq256)\)
- \( FR_3 \): \((fn=0) \land (256<1\leq384)\)

1.(b) Fragmentation modeling using a predicate-transition net

\begin{figure}
\centering
\includegraphics[width=\textwidth]{fragmentation_modeling.png}
\caption{Modeling of the fragmentation mechanism}
\end{figure}
(a) The model using variable arcs with zero changing

(b) The model using variable arcs without zero changing

Figure 2. Modeling of the frame reject mechanism
Figure 3. A model of computer network using non-prime transition
Figure 4. The network layer model with non-prime transition
Figure 5. Store and forward buffering and congestion control model
Figure 6. The data link layer model
Figure 7. The model of the transmission medium
Figure 8. The primitive processes involved in packet handling