

# Virtual Eye: a spatio-temporal bottom-up eye sensitivity model

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**Introduction.** Video quality and compression models use the spatial contrast sensitivity function (CSF) [5], which is solved based on a linear system approximation. This function measures the eye’s sensitivity to sinusoid gratings, ignoring the subtle connectivity and inhomogeneity of cell density across the visual field. Non-linear aspects of the eye, such as the change in frequency sensitivity with changing illumination, are not captured by this simple approximation. We propose Virtual Eye, a bottom-up approach that models the spatio-temporal dynamics of the eye across the visual field. Each functional retinal cell layer in the eye is modeled using non-uniform spatial cell responses, which can be easily extended to incorporate complex retinal nonlinearities. Given any grayscale signal input, Virtual Eye produces a dense output that describes the total retinal energy transmitted to the brain for each point in the visual field.

**Model.** The  $T$  frame,  $M \cdot N$  resolution signal  $V$  is first treated with a lens distortion function to form the retinal projection,  $V_R$ . This projection is then processed by a continuous inhomogeneous ‘field’ of photoreceptors  $R_{cones}$ , which transmit pointwise information along center and surround pathways. Lastly, midget and parasol cell fields difference these paths over time to produce dense spatio-temporal outputs  $R_{midget}$  and  $R_{parasol}$ .

Each cell layer is computed using a spatially continuous Gaussian cell approximation. The local width of Gaussian per pixel coordinate is computed using physiological cell density measurements [2], display distance, and display resolution to ensure output spatial units of cells per pixel. The spatial connectivity and receptive fields of cones, midgets, and parasols are all captured by Virtual Eye.

After computing  $R_{midget}$ , the responses are normalized for sensitivity analysis using

$$\frac{1}{TMN} \sum_{(t,m,n)} |R_{midget}(t,m,n) + \tau_m|^\alpha D_{midget}^2(m,n) \quad (1)$$

where  $t$ ,  $m$ , and  $n$  index the temporal axis, the vertical spatial axis, and the horizontal axis respectively. The parameters  $\tau_m$  and  $\alpha$  model cell firing rate and output non-linearity.  $D_{midget}^2(m,n)$  refers to the squared density of the midget cells. Dividing by  $TMN$  normalizes for resolution and frame rate. Finally, sensitivity can be directly predicted by adding (1) to the complementary computation involving  $R_{parasol}$ .

**Validation.** We calibrated Virtual Eye simultaneously to multiple datasets. Each dataset was chosen to cover different aspects of retinal sensitivity. Figure 1 depicts the spatiotemporal fit for flickering sinusoids presented at the fovea [3]. Figure 2 depicts sensitivity falloff matching across the visual field for select spatial frequencies [4]. We also calibrated with

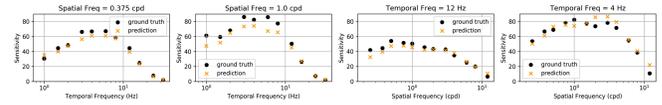
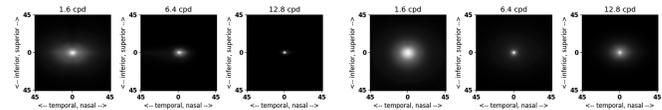


Fig. 1: Virtual Eye fits to spatio-temporal data.



(a) Measurements

(b) Virtual Eye

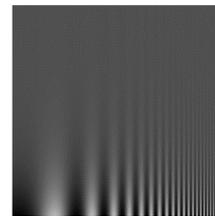
Fig. 2: Sensitivity vs spatial frequency and eccentricity.

the Modelfest dataset [1]. For each dataset, we observing Spearman’s correlation greater than 0.95. For visualizing the calibrated system response, we plot the resulting Virtual Eye midget cell output energy field given the image of a spatial CSF stimuli in Figure 3, demonstrating the emergent property of the csf from the retinal cell populations.

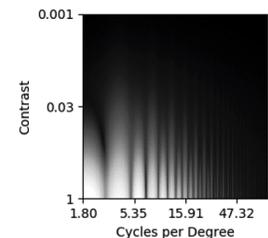
**Conclusion.** We consider this early validation of an exciting new approach, which has the power to model traditionally more challenging phenomena such as eye movement, cortical magnification, and luminance adaptation through emergent properties of cell populations.

## REFERENCES

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(a) Spatial CSF input



(b) Virtual Eye midget energies

Fig. 3: Sensitivity of local foveal midget cells to CSF.