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Computational study of the Seebeck coefficient of one-dimensional composite nano-structures

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The Seebeck coefficient (S) of composite nano-structures is theoretically explored within a self-consistent electro-thermal transport simulation framework using the non-equilibrium Green's function method and a heat diffusion equation. Seebeck coefficients are determined using numerical techniques that mimic experimental measurements. Simulation results show that, without energy relaxing scattering, the overall S of a composite structure is determined by the highest barrier within the device. For a diffusive, composite structure with energy relaxation due to electron-phonon scattering, however, the measured S is an average of the position-dependent values with the weighting factor being the lattice temperature gradient. The results stress the importance of self-consistent solutions of phonon heat transport and the resulting lattice temperature distribution in understanding the thermoelectric properties of a composite structure. It is also clarified that the measured S of a composite structure reflects its power generation performance rather than its cooling performance. The results suggest that the lattice thermal conductivity within the composite structure might be engineered to improve the power factor over the bulk by avoiding the conventional trade-off between S and the electrical conductivity. © 2011 American Institute of Physics. [doi:10.1063/1.3619855]

I. INTRODUCTION

When a temperature difference, ΔT , is applied across a material sample, an open-circuit voltage, V_{oc} , can be induced, generating an electric field that opposes the temperature gradient. This is called the Seebeck effect,¹ and the proportionality constant is the Seebeck coefficient (or thermopower) S , which gives $V_{oc} = -S\Delta T$. The Seebeck coefficient can be looked on as the entropy transport per charged particle,² and $S > 0$ for hole conduction and $S < 0$ for electron conduction. The Seebeck effect is central to thermoelectric (TE) operation, and S is a key parameter in the thermoelectric figure of merit $ZT = S^2\sigma T/\kappa$ that represents the efficiency of thermoelectric energy conversion,¹ where σ is the electrical conductivity, T is the absolute temperature, and κ is the thermal conductivity. For a homogeneous material, S can be calculated using the Boltzmann transport equation (BTE)^{3,4} or Landauer formalism^{5,6} in an integral form as

$$S = \frac{1}{qT} \frac{\int dE \Xi(E)(E - E_F)(-\partial f_0/\partial E)}{\int dE \Xi(E)(-\partial f_0/\partial E)}, \quad (1)$$

where q is the elementary charge ($q = -e$ for electrons and $q = e$ for holes), E is the energy, E_F is the Fermi level, and f_0 is the Fermi-Dirac distribution. The kernel $\Xi(E)$ is called the transport distribution function (in the BTE approach)^{3,4} or the transmission function (in the Landauer approach).⁵⁻⁷ It includes the band structure information and the effect of carrier scattering. If the band structure is simple (e.g., parabolic bands) and the scattering mechanism can be represented in a

simple way, such as the power-law form,⁸ then the S of a homogeneous material can be expressed in a simple analytical form.⁹⁻¹¹

For realistic devices, however, Eq. (1) may not be used because the device structure may be inhomogeneous. For example, nanowire (NW) devices usually have metal contacts at the ends,¹²⁻¹⁴ which introduce Schottky barriers. The potential barriers at the channel ends produce a non-uniform potential profile along the channel, which may affect the overall S of the NW device, making it different than that of a homogeneous NW calculated from Eq. (1). Understanding the Seebeck coefficient of a non-uniform, composite structure is becoming more relevant as the nano-engineered structures, such as superlattices¹⁵ and nano-composites,¹⁶ are attracting much attention as a promising way to further improve ZT .

In this paper, we explore the Seebeck coefficient of composite nano-structures within a self-consistent quantum transport simulation framework. The key questions to be addressed are: 1) What determines the overall S of a composite nano-structure? 2) What roles do the length scales (e.g., energy relaxation length λ_E , the grain size d , etc.) play? 3) How does the measured S relate to the cooling or power generation performance of a composite TE material? 4) Is there a way to use the composite structure to modify the S versus σ trade-off¹ and improve the power factor $S^2\sigma$? We use simple model structures and scattering mechanisms and restrict our attention to one-dimensional (1D) structures, but we expect that the general understanding established in this paper will be broadly applicable.

This paper is organized as follows: in Sec. II, we describe the simulation framework for the self-consistent electro-thermal transport in a 1D composite nano-structure. We also explain the techniques to numerically “measure” S

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in our simulation. In Sec. III, simulation results are presented for ballistic and diffusive transport, and the results are related to a simple electrical-thermal circuit model. The role of λ_E on the measured S is also clarified. In Sec. IV, we discuss the meaning of the measured S regarding the TE performance. Possibilities to modify the S versus σ trade-off and improve the power factor in a composite structure are also discussed. Conclusions follow in Sec. V.

II. APPROACH

Figure 1(a) shows the schematic of our model device. We assume a 1D NW with the doping densities varying along the transport (x) direction. In Fig. 1(a), L_w is the length of the well region, L_b is the barrier thickness, N_w is the doping density in the well, and N_b is the doping density in the barrier. The wire ends are connected to contact 1 and contact 2, which are ideal reservoirs maintained under equilibrium.⁷ To convert the three-dimensional (3D) doping densities to 1D and solve the Poisson equation, we assume a circular cross-section with a diameter D . In all following simulation results, we use $N_w = 3 \times 10^{19} \text{ cm}^{-3}$ (heavily doped), $N_b = 1 \times 10^{16} \text{ cm}^{-3}$ (essentially undoped), and $D = 3 \text{ nm}$. The model structure is intended to represent a potential barrier (grain boundary) between two doped regions (grains). In a realistic nano-composite material, the potential barrier comes from a charge at the grain boundary due to point defects, etc.¹⁷

The simulation framework for the self-consistent electro-thermal transport is summarized in Fig. 1(b). The “electron part” treating the carrier transport and electrostatics is solved self-consistently with the “phonon part” that describes the lattice heat conduction. Within the electron

part, the carrier transport is treated using the 1D non-equilibrium Green’s function (NEGF) method considering three transport models, i.e., ballistic transport, elastic scattering, and inelastic scattering. Most of the previous theoretical studies on nano-composite materials adopt the BTE approach,^{18,19} treating the effect of grain boundaries as another scattering mechanism with some relaxation time, τ . As the grain size gets smaller and approaches the electron wavelength,^{16,20} however, a quantum transport simulation framework, such as the NEGF,^{21,22} is required to better understand the electron transport in nano-composites. As shown in Fig. 1(b), the electrostatics are captured by solving the 1D Poisson equation, and the self-consistent solutions for the NEGF and the Poisson equation give the carrier density n and potential profile V along the x -direction. More details of the 1D NEGF and Poisson schemes are discussed in the Appendix.

The simulation framework for the electron part described so far is widely used for conventional electronic device simulations, assuming a constant lattice temperature T_L .²³ In this work, we add another branch, i.e., the phonon part, to treat the power dissipation P from the electron to the phonon bath^{21,22} and calculate T_L by solving a heat transport equation, which again affects the electron part, as shown in Fig. 1(b). In our simulation, we solve a 1D heat diffusion equation, assuming some lattice thermal conductivity, κ_L . More details are discussed in the Appendix. The self-consistent scheme between the electron and phonon parts is essential to treat the electro-thermal transport phenomena, such as thermoelectrics and self-heating of the device.^{24–26}

Next, we discuss how to determine the overall S . We first review the coupled current equation^{1,5}

$$I = G\Delta V + SG\Delta T, \quad I_q = -TSG\Delta V - K_0\Delta T, \quad (2)$$

where I is the electrical current, G is the electrical conductance, ΔV is the voltage difference, I_q is the heat current, and K_0 is the electronic thermal conductance for zero ΔV . Alternatively, Eq. (2) can be expressed as

$$\Delta V = I/G - S\Delta T, \quad I_q = \Pi I - K_e\Delta T, \quad (3)$$

where Π is the Peltier coefficient and K_e is the electronic thermal conductance for zero current. Note that the Kelvin relation gives $\Pi = TS$. Figure 2 shows the two possible configurations for the Seebeck coefficient measurement. First, S can be determined by measuring electrical currents, as shown in Fig. 2(a). From Eq. (2), $I = G\Delta V$ for a finite $\Delta V = V_2 - V_1$ and $\Delta T = T_2 - T_1 = 0$, where V_1 (V_2) and T_1 (T_2) are the voltage and temperature applied to contact 1 (contact 2), respectively. For $\Delta V = 0$ and a finite ΔT , we obtain $I = SG\Delta T$ and then the Seebeck coefficient can be calculated from the ratio of the two coefficients as $S = SG/G$. Another way to determine S is to measure the open circuit voltage ΔV for a ΔT , as shown in Fig. 2(b), and use the relation $S = -\Delta V/\Delta T$ from Eq. (3). Note that the approach in Fig. 2(b) is widely used for experimental devices.^{12–14} In Sec. III, we use the two approaches to numerically “measure” the Seebeck coefficient of a composite nano-structure and compare the results. For the approach in

FIG. 1. (Color online) (a) Schematic of the 1D NW model device. L_w is the length of the well region, L_b is the barrier thickness, N_w is the doping density in the well, N_b is the doping density in the barrier ($N_w > N_b$), D is the wire diameter, and x is the transport direction. The device is connected to ideal reservoirs: contact 1 and contact 2. (b) Simulation framework for the self-consistent electro-thermal transport. The “electron part” calculates the self-consistent carrier density n and electric potential V , and the “phonon part” is solved for the self-consistent solutions for the power dissipation P and the lattice temperature T_L .

FIG. 2. (Color online) Configurations for Seebeck coefficient measurement. (a) S from current measurements. $I = G\Delta V$ for a finite ΔV ($\Delta T = 0$) and $I = SG\Delta T$ for a finite ΔT ($\Delta V = 0$) and $S = SG/G$. (b) S from the voltage measurement. For an open circuit voltage ΔV for a ΔT , $S = -\Delta V / \Delta T$.

Fig. 2(a) (current measurement), we simply apply ΔV or ΔT and calculate the terminal electrical currents. For the approach in Fig. 2(b) (open-circuit voltage measurement), we first apply ΔT and then increase ΔV until there is no net electrical current flow. Under all ΔV and ΔT conditions, simulations are carried out self-consistently, as described in Fig. 1(b).

III. RESULTS

In this section, we present simulation results for ballistic transport, elastic scattering, and inelastic scattering and explore how carrier scattering affects the measured S of a composite nano-structure. Figure 3(a) shows the ballistic transport simulation results for the energy- and position-resolved electrical current $I(E, x)$ for $L_b = 10$ nm, $L_w = 10$ nm, $\Delta V = 1$ mV, $T_1 = T_2 = 300$ K, and $\kappa_L = 150$ W/m-K, which is the bulk Si value.¹² The Fermi level of contact 1 (E_{F1}) lies at 0 eV; $E_{F1} = E_F = 0$ eV. There is no carrier scattering within the device, so $I(E, x)$ is uniform along the x -direction, and the average energy of the current flow $\langle E \rangle$ is constant. We numerically measure S using the two approaches described in Fig. 2, and the results are $S = -346$ $\mu\text{V/K}$ for the current measurement approach and $S = -348$ $\mu\text{V/K}$ for the voltage measurement approach. The two results are consistent and can be verified in the following way. From the constant $\langle E \rangle$ in Fig. 3(a), we can calculate the Peltier coefficient of the device as $\Pi = \langle E - E_F \rangle / q = -0.103$ V, and the Kelvin relation gives $S = \Pi / T = -344$ $\mu\text{V/K}$, which is consistent with the numerical measurement results. Also note that, for a 1D ballistic conductor, S can be calculated analytically as⁵

$$S_{1D} = \frac{k_B}{q} \left(\frac{\mathcal{F}_0(\eta_F)}{\mathcal{F}_{-1}(\eta_F)} - \eta_F \right), \quad (4)$$

where $\mathcal{F}_j(\eta_F)$ is the Fermi-Dirac integral of order j ,²⁷ $\eta_F = (E_F - E_C) / k_B T$, k_B is the Boltzmann constant, and E_C is the conduction bandedge. For $\eta_F = -3.04$, which is extracted from the simulation result at the top of the barrier

FIG. 3. (Color online) (a) Ballistic transport simulation results for $I(E, x)$ for $L_b = L_w = 10$ nm, $\Delta V = 1$ mV, and $T_1 = T_2 = 300$ K. $I(E, x)$ and the average E of the current flow $\langle E \rangle$ are uniform along the x -direction. Using the approaches in Fig. 2, S is determined to be -346 $\mu\text{V/K}$ (from current measurements) and -348 $\mu\text{V/K}$ (from the voltage measurement). The Kelvin relation gives $S = \Pi / T = \langle E - E_F \rangle / qT = -344$ $\mu\text{V/K}$, which is consistent with the numerical measurement results. (b) Simulation results for $I(E, x)$ for elastic scattering with $D_0 = 0.01$ eV². $I(E, x)$ and $\langle E \rangle$ are still uniform. The two approaches in Fig. 2 give consistent results of $S = -317$ $\mu\text{V/K}$. The Kelvin relation gives $S = \Pi / T = \langle E - E_F \rangle / qT = -315$ $\mu\text{V/K}$, which is consistent with the numerical measurements.

in Fig. 3(a), we obtain $S = -351$ $\mu\text{V/K}$, which is again consistent with the numerically measured S values.

Figure 3(b) shows the simulation results for $I(E, x)$ for elastic scattering with a deformation potential of $D_0 = 0.01$ eV². (The meaning of D_0 within the NEGF framework⁷ and its relation to the conventional expressions in the BTE approach²⁸ are discussed in the Appendix.) All other parameters in Fig. 3(b) are the same as those of Fig. 3(a). Still, the two approaches in Fig. 2 give consistent results as $S = -317$ $\mu\text{V/K}$. Note that carrier scattering broadens energy levels,⁷ which results in a smaller $\langle E \rangle$ than that of the ballistic case in Fig. 3(a). Although elastic scattering relaxes momentum and reduces G , it does not relax energy so that $I(E, x)$ and $\langle E \rangle$ are still uniform along the x -direction. Therefore, we can calculate the overall Π of the device as $\Pi = \langle E - E_F \rangle / q = -0.0945$ V, and the Kelvin relation gives $S = -315$ $\mu\text{V/K}$, which is consistent with the numerical measurement results.

As discussed so far, when there is no energy relaxation within the device, S is determined by the potential barrier. Phase or momentum breaking scattering broadens the levels, effectively lowering the barrier height, as shown in Fig. 3(b),⁷ but still the overall S is determined by the barrier region unless there is energy relaxing scattering. In these cases, Π is uniform along the device, so we can define an overall Π of the device, and the S obtained from the Kelvin relation is consistent with the numerically measured S .

Next, we introduce energy relaxing scattering and see how the results change. Figure 4(a) shows the simulation result for $I(E, x)$ with $\Delta V = 1$ mV and $T_1 = T_2 = 300$ K for optical phonon scattering with $D_0 = 0.01$ eV² and $\hbar\omega_o = 20$ meV, where $\hbar$ is the reduced Planck constant and ω_o is the frequency of the optical phonon. All other parameters are the same as those in Fig. 3. Unlike the results in Fig. 3 without energy relaxation, $I(E, x)$ and $\langle E \rangle$ are non-uniform along the x -direction and we cannot define a constant Π for the overall device. For example, the Peltier coefficient near contact 1 is $\Pi_1 = -0.0702$ V while it is higher in magnitude in the barrier region, where $\Pi_b = -0.0893$ V in Fig. 4(a). The two approaches to measure S (recall Fig. 2) give consistent results as $S = -245$ $\mu\text{V/K}$. Note that the measured S is neither $\Pi_1/T = -234$ $\mu\text{V/K}$ nor $\Pi_b/T = -298$ $\mu\text{V/K}$, but a value somewhere in-between.

To understand the measured S of the composite nanostructure with energy relaxing scattering, we re-visit the coupled current equations in Eq. (2). Note that the T in Eq. (2) actually means the electron temperature T_e as

$$I = G\Delta V + SG\Delta T_e, \quad I_q = -T_e SG\Delta V - K_0\Delta T_e. \quad (5)$$

In the contacts, electrons are in equilibrium with the phonon bath, so $T_{e1} = T_{L1} = T_1$ and $T_{e2} = T_{L2} = T_2$, where T_{e1} (T_{e2}) and T_{L1} (T_{L2}) are the electron and lattices temperatures for contact 1 (contact 2), respectively. When there is no energy relaxation (e.g., ballistic transport), T_e is not well-defined within the device,⁸ but the transport properties, such as S , are well-defined across the terminals. In Fig. 3, for example, carriers injected from the contacts with $T_{e1} = T_1$ and $T_{e2} = T_2$ only see the highest potential barrier and that determines the

FIG. 4. (Color online) (a) Simulation results for $I(E, x)$ ($\Delta V = 1$ mV, $T_1 = T_2 = 300$ K) for optical phonon scattering with $D_0 = 0.01$ eV² and $\hbar\omega_o = 20$ meV. $I(E, x)$ and $\langle E \rangle$ are non-uniform along the x -direction. The two approaches in Fig. 2 give consistent results as $S = -245$ $\mu\text{V/K}$. Simulation results for (b) $S(x) = \langle E \rangle / qT$ ($\Delta V = 1$ mV, $T_1 = T_2 = 300$ K) and (c) $T_L(x)$ ($\Delta T = 1$ K, $\Delta V = 0$). From Eq. (7), we obtain $S = -243$ $\mu\text{V/K}$, which is consistent with the numerical measurement result.

overall S of the device, regardless of the potential profile in the well region. When the carrier energy is relaxed by electron-phonon (e-ph) scattering, however, T_e follows T_L .⁸ As discussed in more detail in the Appendix, the lattice heat transport model gives $T_L(x)$, which determines the carrier energy relaxation rate due to e-ph interaction along the x -direction. This results in the carrier distribution with $T_e(x) \sim T_L(x)$, and $T_e(x)$ governs the coupled current equations in Eq. (5) within the device.

To understand the measured S of a diffusive composite structure in a simple way, we consider a model composite structure in Fig. 5. Two dissimilar regions with different S and G (S_1 and G_1 for region 1, S_2 and G_2 for region 2) are connected in series, and we measure the overall S using the two approaches in Fig. 2. Using a simple electrical-thermal circuit model (see Appendix for details) for the two configurations in Fig. 5, we obtain the same expression for the overall S as

$$S = \frac{S_1\Delta T_{L1} + S_2\Delta T_{L2}}{\Delta T}, \quad (6)$$

where ΔT_{L1} (ΔT_{L2}) is the lattice temperature difference across region 1 (region 2) and $\Delta T_{L1} + \Delta T_{L2} = \Delta T$. Equation (6) shows that the overall S of a diffusive composite structure is a weighted average of its component S values, and the weighting factor is the temperature difference across each component.^{29,30} More generally, Eq. (6) can be expressed in an integration form as

$$S = \frac{\int dx S(x) dT_L(x)/dx}{\Delta T}, \quad (7)$$

where $S(x)$ is the x -dependent Seebeck coefficient. In Figs. 4(b)–4(c), we show simulation results for $S(x) = \langle E \rangle / qT$ ($\Delta V = 1$ mV, $T_1 = T_2 = 300$ K) and $T_L(x)$ ($\Delta T = 1$ K, $\Delta V = 0$) for the model device in Fig. 4(a). From Eq. (7) we obtain $S = -243$ $\mu\text{V/K}$, which is consistent with the numerical measurement result, -245 $\mu\text{V/K}$.

FIG. 5. (Color online) Seebeck coefficient measurement of a composite structure with region 1 (S_1 and G_1) and region 2 (S_2 and G_2). The device is assumed to be diffusive with energy relaxation due to e-ph scattering. (a) Open-circuit voltage measurement. (b) Current measurements. A simple electrical-thermal circuit analysis gives $S = (S_1\Delta T_{L1} + S_2\Delta T_{L2}) / \Delta T$ for both cases, where ΔT_{L1} and ΔT_{L2} are the ΔT_L values applied across region 1 and region 2 and $\Delta T_{L1} + \Delta T_{L2} = \Delta T$.

To derive Eq. (6) or Eq. (7), we assumed that $T_e = T_L$, which holds in the strong scattering limit. In general, however, it may be hard to define $T_e(x)$ in the device, because electron energy may not be fully relaxed by e-ph scattering, so that electrons and phonons are not fully in equilibrium.⁸ Our results above, however, show that the assumption works quite well when analyzing the simulation results, where we numerically “measure” S across the terminals and do not define or assume any $T_e(x)$ within the device.

As demonstrated in Fig. 4(c), for a constant κ_L , the heat diffusion equation gives a linear $T_L(x)$ for a finite ΔT . In such cases, Eq. (7) can be simplified as

$$S \sim \int dx S(x)/L, \quad (8)$$

where L is the total length of the device. Equation (8) implies that, for a uniform κ_L , the overall S of a composite structure is dominated by the region with a longer length. Figure 6(a) shows the simulation results for $\langle E \rangle$ versus x for our model device with optical phonon scattering ($D_0 = 0.01$ eV², $\hbar\omega_o = 20$ meV) for various L_w values with $L_b = 10$ nm ($\Delta V = 10$ mV, $T_1 = T_2 = 300$ K). The maximum $\langle E \rangle$ in the barrier region remains the same, but $\langle E \rangle$ in the well region decays more as L_w increases. The energy relaxation length

FIG. 6. (Color online) (a) Simulation results for $\langle E \rangle$ vs x with optical phonon scattering ($D_0 = 0.01$ eV², $\hbar\omega_o = 20$ meV) for various L_w values, with $L_b = 10$ nm and $\kappa_L = 150$ W/m-K ($\Delta V = 10$ mV, $T_1 = T_2 = 300$ K). The maximum $\langle E \rangle$ in the barrier region remains the same, but $\langle E \rangle$ in the well region decays more as L_w increases. (b) Simulation results for the overall S vs L_w for the composite structure and bulk wire with no potential barriers. Two approaches in Fig. 2 still give consistent results (solid lines: open-circuit voltage measurements; dashed lines: current measurements). As L_w increases, the overall S is more dominated by L_w , and approaches the value of a wire with a uniform doping density.

λ_E is estimated to be about 30 nm in our model device, and we expect that, as L_w becomes much longer than λ_E , $\langle E \rangle$ deep in the well region will approach the value of a wire with a uniform doping density of N_w . We numerically measure the overall S using the approaches in Fig. 2, and the results are shown in Fig. 6(b). Note that the results from the two approaches are still consistent. For $L_w < \sim \lambda_E$, the carrier energy is not fully relaxed in the well region, so that the overall S is more dominated by the barrier, resulting in a higher $|S|$. As L_w increases, however, carrier energy is relaxed more in the well region, as shown in Fig. 6(a), and the overall S is more dominated by L_w and approaches the measured S of a wire with a uniform, high doping density N_w (no potential barrier). Note that the values of S for bulk wires in Fig. 6(b) are consistent with experimental results reported for heavily doped NWs.^{13,14}

In summary, for a composite structure with no energy relaxation or $L \ll \lambda_E$, the overall S is determined by the highest barrier within the device. For a diffusive composite structure with energy relaxation, however, the overall S is an average of its constituent S values, with the weighting factor being the lattice temperature drop across each region. For a simple case of a constant κ_L , $T_L(x)$ is linear for a finite ΔT , and the overall S is the average of $S(x)$ over the device length. In Sec. IV, we discuss the meaning of the measured S of a composite structure in the context of TE performance, explore the effect of a x -dependent κ_L , and suggest possible ways to improve the TE performance by using the composite nano-structures.

IV. DISCUSSION

A. Measured S and TE performance

As shown in the previous section, the two approaches to measure S in Fig. 2 give consistent results. Note that this measured S directly reflects the power generation performance of a TE device.^{29,30} In Fig. 2(a), the measured S is related to the open circuit voltage generated by a temperature difference as $\Delta V = -S\Delta T$ or, equivalently in Fig. 2(b), it represents the device's ability to drive an electrical current for a given temperature difference as $I = SG\Delta T$. For a homogeneous structure with a uniform S , the same S also determines the cooling performance. The cooling performance is determined by the heat current I_q taken away from contact 1, i.e., $I_q(x=0)$ for $\Delta V > 0$ in Fig. 1(a), and this is related to the Π near the contact as $I_q(x=0) = \Pi(x=0)I$, where I is uniform along the device. For a composite structure without energy relaxation, $\Pi(x)$ is uniform, as shown in Fig. 3, and the uniform Seebeck coefficient from $S = \Pi/T$ determines both the cooling and power generation performances. For a composite structure with energy relaxing scattering, however, $\Pi(x)$ is non-uniform, as shown in Figs. 4 and 6, and cooling and power generation performances are represented by different S values. The measured overall S , which is related to the power generation performance, is an average of the non-uniform $S(x) = \Pi(x)/T$, and the weighting factor is the temperature gradient, as discussed in Sec. III. In the case of a constant κ_L (a uniform temperature gradient), the measured S can be related to the average Peltier coefficient

(Π_{avg}) as $S = \Pi_{avg}/T$, where $\Pi_{avg} = \int dx \Pi(x)/L$. The cooling performance, however, is more related to the local value at the contact end, $S(x=0) = \Pi(x=0)/T$.

B. Effects of a non-uniform κ_L

In Sec. III, we discussed simulation results for a constant κ_L , which gives a linear $T_L(x)$ for a finite ΔT . For a composite structure, κ_L may vary within the device, which alters $T_L(x)$ and may affect the measured S . Figure 7(a) shows the simulation results for $T_L(x)$ ($\Delta T = 1$ K, $\Delta V = 0$) for the two model devices, where one of them has a constant κ_L of 150 W/m-K (device 1) and the other one has a much lower κ_L of 1.5 W/m-K in the barrier region (device 2). Both devices are assumed to be diffusive with optical phonon scattering ($D_0 = 0.01$ eV², $\hbar\omega_o = 20$ meV). For a constant κ_L (device 1), $T_L(x)$ is linear, as already shown in Sec. III. When $\kappa_L(x)$ is non-uniform (device 2), however, a large portion of ΔT is applied across the barrier region, which has a smaller κ_L . Figure 7(b) shows simulation results for G versus L_w for the two model devices ($\Delta V = 1$ mV, $T_1 = T_2 = 300$ K). Note that all the parameters are the same for devices 1 and 2 except for κ_L , so they give similar G values. In Fig. 7(c), however, we see a significant difference for the measured S . As shown in Eq. (7), the temperature gradient $dT_L(x)/dx$ is the weighting factor in calculating the average of $S(x)$. This means that the region with a larger ΔT dominates in determining the overall S . As shown in Fig. 7(a), for device 2 (a lower κ_L in the barrier region), most of ΔT is applied across the barrier,

FIG. 7. (Color online) (a) Simulation results for T_L vs x ($\Delta T = 1$ K, $\Delta V = 0$) for the two model devices ($L_w = 50$ nm, $L_b = 10$ nm), where “device 1” has a constant κ_L of 150 W/m-K and “device 2” has a lower κ_L of 1.5 W/m-K in the barrier region. Both devices are diffusive with optical phonon scattering ($D_0 = 0.01$ eV², $\hbar\omega_o = 20$ meV). For device 1, $T_L(x)$ is linear, and for device 2, a large portion of ΔT is applied across the barrier region. (b) Simulation results for G vs L_w for the two model devices ($\Delta V = 1$ mV, $T_1 = T_2 = 300$ K). They give similar G values, because all the parameters are the same except for κ_L . (c) Simulation results for the measured S vs L_w (from open-circuit voltage measurements). The measured S is significantly higher for device 2 and stays high even for $L_w > \lambda_E$, because it is dominated by the barrier region with a large ΔT , as shown in Fig. 7(a), and the barrier has a high $|S(x)|$, as shown in Fig. 6(a).

which has a high $|S(x)|$, as shown in Fig. 6(a). Therefore, as shown in Fig. 7(c), the overall $|S|$ is dominated by the barrier region and remains high even for $L_w > \lambda_E$ for device 2. For device 1 (a uniform κ_L), however, the overall S is more dominated by the well region as L_w increases, as discussed in Eq. (8), so $|S|$ decreases and approaches the value of a uniform wire with a high doping density N_w , as shown in Figs. 6(c) and 7(c). These results suggest that, for a properly designed composite structure, it may be possible to alter the S versus G characteristic from its value in the bulk.

C. Improving the power factor

The effect of non-uniform κ_L on the measured S may open up new possibilities to improve the thermoelectric power factor $S^2\sigma$. It has been suggested that the power factor can be improved by using composite nano-structures composed of grains and grain boundaries,^{17,31,32} where the grain is a doped crystalline region and grain boundaries are thought of as potential barriers that can result in the so-called “energy filtering” effect.³³ The basic idea is the following: first, if the grain size d is much longer than the momentum relaxation length λ_p , then introducing grain boundaries within the device may not decrease σ much, because the device is already in the diffusive limit. Note that the potential barriers at the grain boundaries filter out low energy carriers. If d is shorter or comparable to the energy relaxation length λ_E , then the carrier energy is not fully relaxed within the grain, so $|S|$ increases, as also shown in our simulation results in Fig. 6. Note that λ_E is usually significantly longer than λ_p ,⁸ so, by engineering d as $\lambda_p < d < \lambda_E$, S may improve, while not hurting σ much, which may result in a net improvement in $S^2\sigma$ over a bulk material. If d is very large, as $d \gg \lambda_E$, then one may expect that the composite structure will behave similarly to the bulk material. If the κ_L is non-uniform and specifically low in the barrier region, however, $|S|$ may remain high even for $d \gg \lambda_E$, due to the non-uniform T_L -distribution, as shown in Fig. 7. This suggests that the use of polycrystalline materials may enhance S and the power factor, even for large grain sizes, if the grain boundaries highly impede phonon transport.^{34,35} A detailed quantitative study of the power factor enhancement in composite nano-structure is beyond the scope of this paper, but our results show that it is essential to treat the electron transport and phonon heat transport self-consistently to clearly understand the TE properties of composite structures and explore possible ways to improve the power factor performance.

V. CONCLUSIONS

In this work, we computationally explored the Seebeck coefficient of composite nano-structure within a self-consistent electro-thermal transport simulation framework. Quantum transport of electrons was treated using the non-equilibrium Green’s function method coupled with the Poisson equation, and electron transport was solved self-consistently with the lattice heat diffusion equation. We numerically “measured” Seebeck coefficients using the techniques that mimic experimental methods and explored the effects of energy relaxing

scattering and coupling with phonon heat transport. Simulation results show that, without energy relaxing scattering, the overall S of a composite structure is determined by the highest barrier within the device. For a diffusive composite structure with energy relaxation due to e-ph interaction, however, Peltier and Seebeck coefficients are position-dependent. The measured overall S is an average of the position-dependent values, and the weighting factor is the carrier temperature gradient, which follows the lattice temperature gradient due to e-ph interaction. Therefore, self-consistent simulations of the phonon heat transport and the resulting lattice temperature distributions are very important to understand the TE properties of a diffusive composite structure.

We also clarified the meaning of the measured S regarding the TE performance. For a diffusive composite structure, the measured S directly reflects the electrical power generation performance, but it is less related to the cooling performance. Our simulations also suggest that κ_L -distribution within the composite structure may be engineered to modify the S versus σ trade-off and improve the power factor. For example, by making κ_L smaller in the region with a high local Seebeck coefficient (e.g., grain boundaries), we can apply a larger temperature gradient across that region and improve the overall S while not decreasing σ . Note that this idea may work even for a large grain size of $d > \lambda_E$.

In this work, we used a simple 1D model and a classical heat diffusion model to treat the lattice heat transport, but we believe that the general understanding established in this paper should be useful in exploring nano-composite structure as a promising TE material. For future work, a more advanced phonon transport model^{34,35} may be required to better treat non-equilibrium phonon transport in nanoscale devices and explore its effect on electron transport. While we assumed potential barriers with smooth interfaces where lateral momentum is conserved,³⁶ interface roughness scattering³⁷ may result in different thermoelectric properties. It will be also important to understand carrier transport in the network of 3D grains to address issues in realistic, bulk nano-composite materials.

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APPENDIX: DEVICE MODELS

1.1D Poisson

The 1D Poisson equation along the x -direction is solved as

$$A \frac{V_j - V_{j+1}}{a} - A \frac{V_{j-1} - V_j}{a} = \frac{q(-n_{1D} + AN_{3D})a}{\epsilon_S \epsilon_0}, \quad 2 < j < N - 1, \quad (\text{A1a})$$

$$V_1 = V_2, \quad V_{N-1} = V_N, \quad (\text{A1b})$$

where A is the cross-sectional area of the wire, V_j is the electric potential at the j th grid point, a is the grid size, N is the total number of grid points, ϵ_S is the dielectric constant ($\epsilon_S = 10$ for our model device), ϵ_0 is the vacuum permittivity, N_{3D} is the 3D doping density (N_w or N_b), and n_{1D} is the 1D carrier density, which is obtained from the 1D NEGF, as discussed in Subsection Appendix B. For numerical stability, we adopt the non-linear Poisson technique³⁸ when solving Eq. (A1a). Equation (A1b) represents the boundary conditions at the device ends.

2.1D NEGF

The general model for dissipative quantum transport is⁷

$$G(E) = [EI - H - U - \Sigma(E)]^{-1}, \quad (\text{A2a})$$

$$G^n(E) = G(E)\Sigma^n(E)G^+(E), \quad (\text{A2b})$$

$$A(E) = i[G(E) - G^+(E)], \quad \Gamma(E) = i[\Sigma(E) - \Sigma^+(E)], \quad (\text{A2c})$$

where $G(E)$ is the retarded Green's function, I is the identity matrix, H is the device Hamiltonian, and $U = -eV$ is the self-consistent potential energy obtained from the Poisson scheme in Eq. (A1). In Eq. (A2), $\Sigma(E)$ is the self-energy, $G^n(E)$ is the electron correlation function, $\Sigma^{in}(E)$ is the in-scattering, $A(E)$ is the spectral function, and $\Gamma(E)$ is the broadening, which are all $N \times N$ matrices. For our model device, H is constructed using the effective mass approach⁷ with $m^* = 0.25m_0$ and $a = 0.25$ nm, where m_0 is the free electron mass. The matrices, Σ and Σ^{in} , describe the effects of contacts and carrier scattering as $\Sigma = \Sigma_1 + \Sigma_2 + \Sigma_s$ and $\Sigma^{in} = \Sigma_1^{in} + \Sigma_2^{in} + \Sigma_s^{in}$, where the subscripts 1, 2, and s represent contact 1, contact 2, and scattering, respectively.

In this work, we consider three transport models, i.e., ballistic transport, elastic scattering, and inelastic scattering. For ballistic transport, Σ_s and Σ_s^{in} are all zero in Eq. (A2). Elastic scattering can be treated as⁷

$$\Gamma_s(E) = D_0 A(E), \quad \Sigma_s^{in}(E) = D_0 G^n(E), \quad (\text{A3})$$

where $\Sigma_s(E) = -i\Gamma_s(E)/2$ and D_0 is the deformation potential. For acoustic phonon scattering with elastic approximation, D_0 in Eq. (A3) can be related to the acoustic phonon deformation potential D_A as²⁸

$$D_0 = D_A^2 k_B T F / (\rho v_s^2 a^3), \quad (\text{A4})$$

where F is the wavefunction overlap,⁸ ρ is the mass density, and v_s is the sound velocity. In Eq. (A4), D_A is given in eV and frequently appears in the conventional BTE approach.⁸ For Si bulk parameters,³⁹ Eq. (A4) gives $D_0 \sim 0.002$ eV² for a cylindrical NW with $D = 3$ nm and intraband transition within the ground state ($F \simeq 2.66a^2/D^2$). In Sec. III, we use $D_0 = 0.01$ eV² for elastic scattering, which gives $\lambda_p \sim 6.5$ nm for our model device.

For inelastic scattering, we consider optical phonon with a single frequency ω_o as⁷

$$\Gamma_s(E) = D_0(N_{\omega_o} + 1)[G^p(E - \hbar\omega_o) + G^n(E + \hbar\omega_o)] + D_0N_{\omega_o}[G^n(E - \hbar\omega_o) + G^p(E + \hbar\omega_o)], \quad (\text{A5a})$$

$$\Sigma_s^{in}(E) = D_0(N_{\omega_o} + 1)G^n(E + \hbar\omega_o) + D_0N_{\omega_o}G^n(E - \hbar\omega_o), \quad (\text{A5b})$$

$$N_{\omega_o} = 1/(\exp(\hbar\omega_o/k_B T_L) - 1), \quad (\text{A5c})$$

where N_{ω_o} is the Bose-Einstein factor and $G^p(E)$ is the hole correlation function, which gives $A(E) = G^n(E) + G^p(E)$. Note that, in Eq. (A5c), we assume an equilibrium occupation factor for phonons, but T_L is position-dependent. We can also relate D_0 in Eq. (A5) to the optical phonon deformation potential D_o as²⁸

$$D_0 = \hbar D_o^2 F / (2\rho\omega_o a^3), \quad (\text{A6})$$

where D_o is given in eV/cm. For a cylindrical NW with $D = 3$ nm and Si bulk parameters (LO mode),³⁹ we obtain $D_0 \sim 0.01$ eV². In Sec. III, we use this typical value of $D_0 = 0.01$ eV² for optical phonon scattering, which gives $\lambda_p \sim 4.5$ nm and $\lambda_E \sim 30$ nm for our model device.

Once the solutions for $G(E)$ and $G^n(E)$ are obtained, physical quantities at the j th grid point can be calculated as^{7,23}

$$n_{1Dj} = \int dE G_{j,j}^n(E) / (\pi a), \quad (\text{A7a})$$

$$I_{j \rightarrow j+1} = \frac{e}{\pi \hbar} \int dE \left(-\text{Im} \left[H_{j,j+1} G_{j+1,j}^n(E) - H_{j+1,j} G_{j,j+1}^n(E) \right] \right), \quad (\text{A7b})$$

where $I_{j \rightarrow j+1}$ is the electrical current flow from the j th to the $(j+1)$ th grid points. Note that the spin degeneracy of 2 is included in Eq. (A7). The n_{1D} in Eq. (A7a) is again an input to the Poisson scheme in Eq. (A1), and the process is repeated until the self-consistent solutions for n_{1D} and V are obtained.

3. Lattice heat transport

To treat the heat conduction due to phonons, we solve a 1D heat diffusion equation as^{21,25}

$$\frac{d}{dx} \left(-\kappa_L \frac{dT_L}{dx} \right) = P, \quad P = -dI_E/dx, \quad (\text{A8a})$$

$$T_L(x=0) = T_1, \quad T_L(x=L) = T_2, \quad (\text{A8b})$$

where I_E is the energy current by electrons, which is calculated from Eq. (A7b) with e substituted by E . As shown in Eq. (A8b), we use fixed boundary conditions at the device ends. As described in Fig. 1(b), T_L is calculated by solving Eq. (A8) for a given P from the electron part, and the updated T_L again affects the electron part by changing the phonon scattering rates in Eq. (A5). The process is repeated until we obtain converged results for T_L .

4. Diffusive composite structure: Electrical-thermal circuit model

Under the open-circuit condition in Fig. 5(a), Eq. (5) gives

$$I_1 = G_1 \Delta V_1 + S_1 G_1 \Delta T_{e1} = 0, \quad (\text{A9a})$$

$$I_2 = G_2 \Delta V_2 + S_2 G_2 \Delta T_{e2} = 0, \quad (\text{A9b})$$

$$\Delta T = \Delta T_{e1} + \Delta T_{e2}, \quad (\text{A9c})$$

$$T_e = T_L, \quad (\text{A9d})$$

where I_1 (I_2) is the electrical current along the region 1 (region 2), ΔV_1 (ΔV_2) is the voltage across the region 1 (region 2), and ΔT_{e1} (ΔT_{e2}) is the electron temperature difference across the region 1 (region 2). As discussed in Sec. III, Eq. (A9d) comes from the carrier energy relaxation due to e-ph scattering, and T_L is given from the lattice heat conduction model in Eq. (A8). Equation (A9) gives the solutions for the four variables, i.e., ΔV_1 , ΔV_2 , ΔT_{e1} , and ΔT_{e2} , and then the overall S becomes

$$S = -\frac{\Delta V}{\Delta T} = -\frac{\Delta V_1 + \Delta V_2}{\Delta T} = \frac{S_1 \Delta T_{L1} + S_2 \Delta T_{L2}}{\Delta T}. \quad (\text{A10})$$

Equation (A10) means that the overall S of a diffusive composite structure is the average of the S values of its constituent materials weighted by the temperature difference applied in each region.^{29,30} For the current measurement configuration in Fig. 5(b), we first apply a finite ΔV and then Eq. (5) and the current continuity condition give

$$I = G_1 \Delta V_1 = G_2 \Delta V_2, \quad (\text{A11a})$$

$$\Delta V = \Delta V_1 + \Delta V_2. \quad (\text{A11b})$$

And then, by defining $I \equiv G \Delta V$, we obtain the overall G as

$$G = G_1 G_2 / (G_1 + G_2), \quad (\text{A12})$$

which implies that the region with a smaller G dominates.³⁶ Next, we apply a finite ΔT and $\Delta V = 0$. Here, we should be careful not to use the current continuity condition, as $I = S_1 G_1 \Delta T_{e1} = S_2 G_2 \Delta T_{e2}$. For a diffusive device with energy relaxation due to e-ph interaction, T_e follows T_L , not being determined by the current continuity condition. The correct equations to be solved are

$$I = S_1 G_1 \Delta T_{e1} + G_1 \Delta V_1 = S_2 G_2 \Delta T_{e2} + G_2 \Delta V_2, \quad (\text{A13a})$$

$$\Delta T = \Delta T_{e1} + \Delta T_{e2}, \quad (\text{A13b})$$

$$\Delta V_1 + \Delta V_2 = 0, \quad (\text{A13c})$$

$$T_e = T_L. \quad (\text{A13d})$$

Note the additional $G_j \Delta V_j$ terms ($j = 1, 2$) in Eq. (A13a) and the condition for $\Delta V = 0$ in Eq. (A13c). And then, by defining $I \equiv SG \Delta T$, we obtain the overall SG as

$$SG = \frac{G_1 G_2 (S_1 \Delta T_{L1} + S_2 \Delta T_{L2})}{(G_1 + G_2) \Delta T}, \quad (\text{A14})$$

and the overall S is calculated from Eqs. (A12) and (A14) as

$$S = \frac{SG}{G} = \frac{S_1 \Delta T_{L1} + S_2 \Delta T_{L2}}{\Delta T}. \quad (\text{A15})$$

Note that Eq. (A15) is the same as Eq. (A10), which means that the two approaches to measure S in Fig. 2 give consistent results for composite structures, as has been demonstrated in simulation results in Sec. III.

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