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Abstract

To provide users with a uniform interface to access federated database systems, local database schemas must be integrated to form a global schema. Before the integration, objects to be integrated need to be defined. Only semantically similar objects are integrated. In our paper, we define semantic similarity via a method which considers the semantics of objects in a database application context. The context of database is treated rigorously. We propose a measurement of semantic similarity and provide a taxonomy of semantic similarity. The advantage of this approach is that it establishes a foundation for formulating methods to determine which object schemas are semantically similar and need to be integrated.

1 Introduction

With the advances in the computer network technology, applications to access multidatabase systems in a uniform way have emerged. Users want to share data stored on isolated databases. This need is especially urgent for large organizations and companies. But the requirement has been hampered by three dimensions of characteristics of multidatabase systems which are: heterogeneity, autonomy, and distribution [ÖV91].
While earlier research focused on the distribution aspect of databases, current work in the database community now emphasizes the heterogeneity aspect of databases [She91]. The function of database integration is to integrate multiple databases in order to reduce the heterogeneity among component databases and to provide a global view of the federated database for users [SL90].

Database integration consists of system integration, schema integration, and semantics integration. *System integration* operates to hide the system heterogeneity such as hardware, operating system, and transaction management heterogeneities among component databases. *Schema integration* functions to provide a global view of the databases by integrating local schemas if the objects are semantically similar. *Semantics integration* acts to resolve semantic conflicts among data stored on multiple databases and to maintain consistency among interdependent data.

To integrate databases, many commercial and prototype federated database systems [BOT86, ANRS92, LR82, TLW87, BCD+93] have been developed. Research on federated database systems has also made major advances. Regarding system integration, significant understanding of transaction management in multidatabase systems has been achieved [BGMS92, DE89]. In many papers, such as [KS91, DH84, BOT86], database heterogeneity has been investigated from the viewpoint of reducing schematic conflicts. Compared with literature on systemic and schematic issues [BLN86], much less progress has been achieved on semantic issues [She91]. Not enough research work on semantic heterogeneity has been done, although semantic integration is one of the oldest and most difficult problems in multidatabase systems [ACM90].

Before schema integration, objects to be integrated need to be defined. With the achievement in schema integration, as well as high interconnectivity and access to many information sources, the primary issue in the future will not be the efficiency of data processing but the relevancy of the data [She91]. We only integrate semantically similar objects. Three tasks are involved in finding semantically similar objects: 1) resolving schematic heterogeneity; 2) identifying semantic similarity; and 3) recognizing...
semantic discrepancy.

With consideration to both schematic and semantic aspects of multiple databases, a semantic equivalence theory was established in the papers [LNE89, ENS4, NSE84]. The theory concerns attribute equivalence, object equivalence, and class equivalence. In regards to our work, semantic equivalence is a special case of semantic similarity. [SM91] describes a rule-based approach to semantic specification that can be used to establish semantic agreement between a database and applications. [FKN91] investigated the similarity of classes which utilizes fuzzy and incomplete terminological knowledge as well as schematic knowledge. [GPN91] introduced a mathematically based distinction between the structural and semantic aspects of class specification.

Recently, [SK92] introduced the concept of semantic proximity to specify degrees of semantic similarities among objects based on their real world semantics and used such a concept to propose a taxonomy of semantic similarity and schematic conflicts. Semantic proximity considered database semantics with respect to database context. The context was described by enumeration of some examples with no precise definition given. Additional work is needed to further clarify the nature and structure of the context to which two objects can belong.

In comparison to previous works, the major contributions of our paper are: 1) We present a method to define the nature of context of database applications. An object-oriented data model is used for the presentation. Database semantics is defined with respect to context. 2) We define precisely semantic similarity based on database semantics within the database context. 3) We propose a way to measure semantic similarity between objects. 4) We give a taxonomy of semantic similarity according to our definitions. The treatment of these topics is formal and generic.

Only with a strict, formal approach, can it be possible to establish an automatic or even a semi-automatic way to recognize semantic similarity between objects. A formal treatments serves several purposes:
• Facilitates in understanding of database and data semantics;
• Assists in federated database standardization;
• Supports federated database design;
• Aids in writing database integration tools;
• Accommodates the application verification and software reliability;
• Provides a model for database integration specification.

Formalization is not a panacea and should be used properly. Its major limitation is that real world applications are still difficult with the current technology [Mey90].

The paper is organized as follows: In section 2, we describe the notions and related concepts for defining database semantics with respect to the context. In section 3, we define semantic similarity according to the semantics defined in context and provide a taxonomy of semantic similarity. We also present a model to measure semantic similarity. In section 4, we delineate our conclusions and list some ideas for future work.

2 Database Semantics in Context

Basic significance of databases is to store and manipulate data by computers in an economical fashion. Data in databases is worthless if it does not mean anything or has no use. With respect to one database, data is manipulated according to certain semantic rules, and users usually interpret the data according to some implicit assumptions [Ken91]. When more than one database is considered, the rules and assumptions from different databases may conflict. Data stored in these databases can be interpreted in different ways by applications or by human users under different contexts. To capture the semantics of these data, context of database must be taken into account explicitly.
2.1 Modeling the Reality

Entities in the real world are modeled by data in computers to reflect the real world. Figure 1 shows steps to map from entities in the real world to the computer stored data. We regard the real world as one consisting of entities. An entity can be concrete, such as a book; or it can be abstract, such as 1, 2, \( \infty \), big, or happy. The first step is to map the real world to the abstract world. The abstract world mathematically consists of sets. Every real world entity can be modeled as a set. The modeling is an isomorphism. Therefore, we can use an entity to refer either to a real world entity or to a corresponding set in the abstract world.

![Figure 1: Graph of Worlds](image)

In the abstract world, functions are defined on sets. This is the behavior aspect of entities. A function \( f \) is related to an entity \( e \) if \( e \) is involved in the definition domain of \( f \) as:

\[
f : \ldots \times D \times \ldots \rightarrow R_1 \times R_2 \times \ldots
\]

or \( e \) is involved in the definition range of \( f \) as:

\[
f : D_1 \times D_2 \times \ldots \rightarrow \ldots \times D \times \ldots
\]

where entity \( e \in \) domain \( D \) and \( D_i, R_j \) are arbitrary sets.
In the second step, for convenient computer processing, we model the abstract world by a *model world*. There is more than one way to model the abstract world by a model world. In an object-oriented data model, the model world consists of abstract objects which can be represented in computers. Objects with the same behaviors can be grouped into classes.

We define the behavior of an object as follows: the behavior of an object \( O \) corresponds to a function \( f \) in the abstract world related to the entity \( e \) which is in correspondence to the object \( O \). Intuitively, behaviors are those activities or associations in which the object participates. A behavior can be a user application, called external behavior, or it can be a method or an attribute, etc. publically accessible to users, called internal behavior. The objects of the same class share the same behaviors. Therefore behaviors are usually defined with the class. The *environment* of an object \( O \) is the set of all behaviors of \( O \). The *context* of an object \( O \) is the subset of the environment consisting of behaviors which users are concerned with.

In the last step, the objects are represented as computer data in computers which form the *computer data world*. The representation mapping is also isomorphic. The model world and the computer data world become indistinguishable.

Therefore, from that point on, all our discussion is just on the model world and the abstract world. Database syntax is defined in the model world. The semantics is to define the mapping between the model world and the abstract world.

### 2.2 Database Context

Database context is the set of objects' behaviors which users are concerned with. We can divide behaviors of context into internal and external behaviors. Internal behaviors are defined by the system and are absolute for the outside world. They do not depend on any exterior elements. Publically accessible components, such as object attributes, methods, etc., all belong to the internal context. External behaviors
are applications defined by users and vary from user to user.

Without context but with the same syntax, an object can have several meanings or it can mean nothing. Context is a restriction of semantic mapping when an object has ambiguous semantics. When an object has no prior meaning, context can provide its semantics.

According to the location of the data being accessed, in multidatabases there are local and global application behaviors. Local behaviors are defined to a local database. Global behaviors are globally defined to more than one database.

A behavior which can create values of an object is called a producer of the object. A behavior which retrieves values of an object is called a consumer of the object. Usually, the producer of an object defines the semantics of the object. Consumers of the object interpret the object with the semantics defined by the producer. If there is no communication barrier between the producers and the consumers, semantic problems will not exist at all. For multidatabases, usually the consumers can not grasp the meaning defined by the producers easily.

Very often, context plays its role in a guise of other terms, such as places, databases, etc.. But contexts are still collections of behaviors.

Example 2.1 Location can determine semantics. For instance, in some databases, a value of an attribute money is 150. In the context of London, when we consider applications for London, it means 150 British pounds. In the context of New York, it means 150 U.S. dollars. The activities in which 150 is involved imply its meaning as either British pounds or U.S. dollars. To be more specific, the producers of the data value 150 determine the semantics. In London, for instance, the producer of 150 assumes that it is 150 pounds and all consumers should interpret it as 150 pounds. In computers, sometimes it is very convenient to store some rules or additional attribute items for this purpose. The rules or attributes can imply (or restrict) the meaning of some syntax structure [SM91].
Example 2.2 Database names can determine semantics. In a database $DB_1$, education degrees Ph.D, Master, Bachelor and High School diploma are represented as 1, 2, 3, 4, respectively. But in another database $DB_2$, they are represented as 4, 3, 2, 1, respectively. In the context of these different databases, the values represent different degrees. Although the context in this case is in the guise of the database names, again the semantics of the data are defined by the producer of the data. The context is actually the application behaviors.

In paper [SK92], many other instances of contexts are discussed. They all fit our definition of the context if viewed from the perspective of object behaviors.

2.3 Database Syntax and Semantics

In this section we discuss the concepts of syntax and semantics of databases formally and generically. Based on this discussion, we define semantic similarity in the next section.

1. Syntax

Syntax is the symbols and the structures in which the symbols are put together to form the model world objects in representations of entities in the real world. Computers process these symbols according to some rules and human beings interpret the meaning of the results. In database systems, schemas are used to describe the syntax of databases.

Objects with common properties and behaviors are grouped into classes. Therefore objects of the same class can be defined by their class description.

Definition 2.1 Syntax of class C is defined as

$$S_C = \{\text{Class Identifier, Properties, Internal Behavior Description}\},$$

where Internal Behavior Description includes all the behaviors, such as attributes and methods of the class defined by the system, publicly accessible to the outside
world. The external behavior of a class is the applications using the class defined outside the definition of the class.

An object is an instance of a class. Syntax of an object can be defined by the object identifier, the class it belongs to, and the instance state which retains the effect of the behaviors.

**Definition 2.2** Syntax of an object \(O\) is defined as

\[ SO = \{\text{Object Identifier, Class Identifier, State}\}, \]

**Example 2.3** A class with class identifier Employee has properties \{name, photo, birth_date, salary\} and behaviors \{IncreaseSalary, ShowPhoto\}. An object of class Employee can have object identifier E and state \{Mark Twain, photo_image, 08/04/45, 90\}. From this syntax, the semantics of 90 of Mark's salary is not so obvious here. It can be 90 thousand dollars per year, or 90 dollars per week.

### 2. Semantics

Semantics is the scientific study of the relations between syntax and what it denotes\[\text{Wo085}\]. In our model introduced in the early part of this paper, semantics is the mapping between the conceptual world and the abstract world. For one database, data is manipulated according to some rules and users interpret the data according to some implicit assumptions. These rules and implicit assumptions are consistent within one database. When more than one database is considered, these rules and assumptions may conflict. The semantics of data has to be defined with respect to context explicitly.

**Definition 2.3** Semantics of a class \(C\) in external context \(C^e\) is:

\[ \text{Sem}_{C^e} : S_C \mapsto (D_C, C^e, C^i) \]

Where \(S_C\) is the syntax of class \(C\). \(C^i\) is the internal context consisting of functions corresponding to the internal behaviors of class \(C\). The context of class \(C\) is \(C^e + C^i\). \(D_C\) is the semantic domain of class \(C\).
Definition 2.4 Semantics of an object $O$ in external context $C^e$ is:

$\text{Sem}_{C^e} : S_O \rightarrow (\text{value}, D_O, C^e, C^i)$

Where $S_O$ is the syntax of $O$, $D_O$ is the semantic domain of $O$ and $\text{value} \in D_O$. $C^i$ is the same as that in the definition of class semantics.

The definition shows that the semantics of an object is related with the domain, the corresponding value in the domain, as well as external and internal behaviors. Example 2.1, Example 2.2, and the following example show how behaviors determine semantics in different situations.

Example 2.4 The number 2 may be an integer or a floating number. $2/3.0$ implies 2 is the floating number 2.0. But $\text{list}[2]$ implies that 2 is an integer. Operations $/$ and $[\ ]$ determine the semantics of 2. Without these behaviors, we can not have the exact semantics of the object 2.

3  Semantic Similarity

In this section, we define semantic similarity between objects using database semantics in application context defined in the previous section. When two objects represent the same real world entity, they will have the same semantics. When they represent different types of real world entities, they often do not share every property. Therefore, when two objects share some common property in a context, we say that they are similar, and we can integrate them according to their common behaviors.

3.1 Semantic Equivalence and Semantic Similarity

When two objects represent the same real world entity, their behaviors will be the same although the entity was modeled in different ways. In this case, the two objects are semantically equivalent. The theory of attribute equivalence, object equivalence, and class equivalence [LNE89, EN84, NSE84] is compatible with our semantic equivalence concept.
When two objects represent different types of real world entities, they can still share common attributes. Under some context, we want to integrate similar objects although they do not represent the same entity in the real world. For example, Car and Truck are two different kinds of objects. But they share some common attributes. In this case, we say they are semantically similar. We can generalize the classes of the objects and integrate them.

Some objects do not have any common attribute to share in a context. But in some extended context, they can have some properties in common. For example, if we consider Car and Book both as items we spend money on, they can be integrated as (item name, price). In this case, the object similarity is very obviously context related.

3.2 Measurement of the Semantic Similarity

To know the strength of semantic similarity, we define a measurement of semantic similarity. The measurement of degrees of semantic similarity can help the decision of database integration and the optimization of global queries.

We measured semantic similarity according to the amount of the common semantic behaviors in all behaviors of the two objects. The weight function in which the frequencies are taken into account make the measurement more precise. Semantics which are often used take more weight in the measurement.

Definition 3.1 For two objects $O_1$ and $O_2$ in context $C$, we define the strength of semantic similarity between them as the shared behaviors in all behaviors of $O_1$ and $O_2$ with respect to some weight function $w(x)$ which reflects the frequency of the usage of behaviors:

$$sim_C(O_1, O_2) = \frac{|w(Sem_c(O_1) \cap f(Sem_c(O_2)))|}{|w(Sem_c(O_1))| + |w(Sem_c(O_2))|}$$

where $w(x)$ can be obtained by statistical data or in advance by the user's estimation. $f$ is the mapping from semantic domain of object $O_1$ to semantic domain of object $O_2$. 
When \( \text{sim}_C(O_1, O_2) > 0 \), we say object \( O_1 \) and \( O_2 \) are \textit{semantically similar} in context \( C \).

Since we consider the frequency of behaviors being used, the measurement is more accurate than those described in [SK92]. The strength of semantic similarity is useful for optimization of data storage. For highly similar objects, the global view can be materialized for fast access.

Example 3.1 If objects \( O_1 \) and \( O_2 \) are semantically equivalent, all their behaviors are the same, i.e. \( \text{sim}(O_1, O_2) = 1 \). In this situation, the objects can be totally integrated. We will give the strict definition of semantic equivalence in the next section.

Example 3.2 If there is no common behavior among objects or their common behaviors are never used, then the similarity between them is 0. Then there is no need to integrate the objects.

Example 3.3 A car \( C \) and a truck \( T \) have common attributes \{plate.num, maker, year\}. Car \( C \) has a distinct attribute style, and truck \( T \) has a distinct attribute tonnage. The applications accessing the common behaviors and attributes are, say, 60% in all accesses to the behaviors and attributes of the objects. Then \( \text{sim}(C, T) = 0.60 \).

Assumption: For simplicity in our presentation, we assume that all behaviors of an object are used by local and global users. Otherwise, if a behavior is not used by any user, it can be treated as nonexistent. If a behavior is not used by global users, it is equivalent to not being exported to global users.
3.3 A Taxonomy of Semantics Similarity

Figure 2 summarizes the taxonomy of semantic similarity which we will discuss in this section. Our work is based on [SK92]. Since our definition of semantic similarity is based on the behavior aspects of objects within the same context, the taxonomy is therefore different from that presented in [SK92] where semantic similarity was classified according to abstraction mappings and context cases.

![A Taxonomy of Semantic Similarity](image)

When two objects are unrelated, they have semantic incompatibility. Otherwise they have semantic relativity if common behaviors exist in an extended database context. Two objects have semantic likeness if common behaviors exist in an extant database context. If the behaviors of one object is a subset of those of another, the semantic similarity is more specific as semantic specialization or semantic general-
When two objects represent the same entity in the real world sharing the same behaviors, they have semantic equivalence.

1. Semantic Equivalence

Two objects have state semantic equivalence in a database context if they represent the same entity in the real world. Therefore, their behaviors and instance states are exactly the same. Two objects have class semantic equivalence if they represent entities of the same class in the real world, i.e. their behaviors are the same but the instance states may be different. By (object) semantic equivalence, we mean either state semantic equivalence or class semantic equivalence. Object semantic equivalence is also called object semantic isomorphism. A formal definition of state semantic equivalence is the following:

Definition 3.2 Object $O_1$ and $O_2$ have state semantic equivalence if and only if there exists a bijective mapping $f$ between the definitions of $O_1$ and $O_2$ such that $f(O_1) = O_2$, and there exists a bijective mapping $\tilde{f} : Sem_1 \rightarrow Sem_2$ where $Sem_j$ is the semantics of $O_j$ ($j=1,2$) such that for context $C^e$

$$Sem_{C^e}(O_2) = Sem_{C^e}(f(O_1)) = \tilde{f}(Sem_{C^e}(O_1)).$$

When object $O_1$ and $O_2$ have state semantic equivalence, we denote it as $O_1 \equiv_{C^e} O_2$. When the external context $C^e$ is obvious, it can be omitted. In the definition, $f$ is the mapping between equivalent objects. $\tilde{f}$ is the mapping between semantics. Equation (1) means that the corresponding objects have the equivalent semantic behaviors. Therefore all database constraints, security control, etc. are the same for the two objects.

When $f$ is the identity mapping in Definition 3.2, there is no schema heterogeneity between $O_1$ and $O_2$. $O_1$ and $O_2$ are identical for all contexts.

Object state semantic equivalence only exists when the objects in different databases represent exactly the same entities in the real world. If there is any inconsistency be-
tween equivalent objects, either the objects should be updated to the most recent value with consistency, or some relaxed correctness criteria should be adapted.

In reality, different objects of the same class are usually stored in different databases. In this case, we want to integrate the database schema since they represent the same class although different objects are stored in different databases. We define class semantic equivalence below.

**Definition 3.3** Object $O_1$ and object $O_2$ have *class semantic equivalence* if $O_1$ is an instance of $C_1$ and $O_2$ is an instance of $C_2$, where it is possible that, $\exists O_3$ which is an instance of $C_2$ (or $C_1$), such that $O_1$ (or $O_2$) is state semantic equivalent to $O_3$.

We denote class semantic equivalence of object $O_1$ and $O_2$ as $O_1 \equiv O_2$. For classes $C_1$ and $C_2$, where $O_1$ is an instance of $C_1$ and $O_2$ is an instance of $C_2$ and $O_1 \equiv O_2$, then $C_1$ and $C_2$ have the same structure and behaviors. So we can integrate them by one schema.

**Example 3.4** Two synonym objects are semantically equivalent. For instance, we have

\[
\text{STUDENT} : (\text{Sno}, \text{Sname}, \text{Age}) \\
\text{STU.REC} : (\text{Sid}, \text{Sn}, \text{S.age}).
\]

Then we can say, an object $(36, \text{John}, 20)$ in STUDENT is *class semantic equivalent* to $(21, \text{Mary}, 18)$ in STU.REC, and $(36, \text{John}, 20)$ in STUDENT is *state semantic equivalent* to $(36, \text{John}, 20)$ in STU.REC since they represent the same person. State semantic equivalence maps the objects that represent the exact same real world entity to each other.

We can see from the example that semantically equivalent objects have the same inner structure and behaviors. They belong to the same class in an object-oriented data model or have the same relation schema in a relational data model. State equivalent objects are exactly the same objects which have been stored over several databases.
Theorem 3.1 Object semantic equivalence is a symmetric, transitive relation.

1. Symmetric: $A_1$ is equivalent to $A_2$, if and only if $A_2$ is equivalent to $A_1$. i.e. $A_1 \cong (or \equiv) A_2 \iff A_2 \cong (or \equiv) A_1$

2. Transitive: If $A_1$ is equivalent to $A_2$ and $A_2$ is equivalent to $A_3$, then $A_1$ is equivalent to $A_3$. i.e. $A_1 \cong (or \equiv) A_2$ and $A_2 \cong (or \equiv) A_3 \implies A_1 \cong (or \equiv) A_3$

The proofs are trivial from the Definition 3.2 and Definition 3.3.

By the theorem, if we have semantically equivalent classes, we can use one schema to represent all of the classes by integration since they are semantically equivalent to each other.

2. Semantic Likeness

When two objects represent different entities, they might share some common properties, therefore object semantic similarity can be defined. If the behaviors of an object are a subset of those of another object, then we say that the latter is the specialization of the former.

Definition 3.4 Object $O_1$ is a state semantic specialization of object $O_2$ if and only if $\exists$ a mapping $f$ between the definitions of $O_1$ and $O_2$ such that $f(O_1) = O_2$, and $\exists$ a mapping $\tilde{f}$: $\text{Sem}_1 \rightarrow \text{Sem}_2$ where $\text{Sem}_j$ is the semantics of $O_j$ ($j=1,2$) such that for external context $C^e$

$$\text{Sem}_{C^e}(O_2) = \text{Sem}_{C^e}(f(O_1)) \subseteq \tilde{f}(\text{Sem}_{C^e}(O_1))$$ (2)

where $f$ need not to be a bijection. It can be many-to-one and partial. Equation(2) shows that semantic behaviors of one object is a subset of the other's behaviors.
We denote state semantic specialization of object \( O_1 \) and \( O_2 \) as \( O_1 \prec_s O_2 \). We can also define class semantic specialization.

**Definition 3.5** Object \( O_1 \) is a class semantic specialization of object \( O_2 \) if and only if for \( O_1 \) as an instance of class \( C_1 \) and \( O_2 \) as an instance of class \( C_2 \), \( \exists O_3 \) in \( C_2 \) (or \( O_3 \) in \( C_1 \)), such that \( O_1 \) (or \( O_2 \)) is a state semantic specialization of \( O_3 \). We denote class semantic equivalence as \( O_1 \prec C O_2 \).

The anti-relation of semantic specialization is semantic generalization. The definition follows.

**Definition 3.6** Object \( O_1 \) is a (state) semantic generalization of object \( O_2 \) if and only if \( O_2 \) is a (state) semantic specialization of \( O_1 \). We denote (state) semantic generalization as \( (O_1 \succ_s O_2) \) or \( O_1 \succ O_2 \).

**Example 3.5** An object of Vehicle : (Plate#, Owner) is a semantic generalization of an object of Car : (Plate#, Owner, Maxspeed). Vehicle is a generalization of Car and Car is a specialization of Vehicle.

Like semantic equivalence, semantic generalization and specialization are transitive by their definitions.

In general, the behaviors of two objects do not have inclusive relations. They only have some behaviors in common. Then we can define the concept of semantic likeness.

**Definition 3.7** Object \( O_1 \) and object \( O_2 \) have semantic likeness if and only if \( \exists \) object \( O_3 \), such that \( O_3 \) is a semantic generalization of both \( O_1 \) and \( O_2 \). We denote it as \( O_1 \sim O_2 \).

**Example 3.6** An object of Truck : (Plate#, Owner, Tonnage) has semantic likeness to an object of Car : (Plate#, Owner, Maxspeed) since we can have an object in Vehicle : (Plate#, Owner) being a semantic generalization of both a truck and a car.
Theorem 3.2 Semantic likeness is symmetric and semi-transitive.

1. Symmetric: \( O_1 \sim O_2 \iff O_2 \sim O_1 \)

2. Semi-Transitive: \( O_1 \sim O_2, \text{ and } O_2 \equiv O_3 \implies O_1 \sim O_3 \)

Example 3.7 The semantic likeness relation is not a transitive relation. For example, let us consider pens. Pen A and Pen B both are blue in color. Pen B and Pen C both are large in size. Pen A and Pen B are similar in color. Pen B and Pen C are similar in size. But Pen A is small and blue, while Pen C is large and red, so they are not similar in the context. See Figure 3.

![Figure 3: A ~ B, B ~ C, but A \not\sim C](image)

3. Semantic Discrepancy

Semantic discrepancy [She91] means there is inconsistency in the database environment. Then, either the consistency of the database should be enforced, or some weak consistency condition should be defined and maintained.

Definition 3.8 If object \( O_1 \) and object \( O_2 \) have semantic likeness, but some consistency conditions for \( O_1 \) and \( O_2 \) are violated, then the objects have semantic discrepancy.

Example 3.8 Two databases store employee information. For an employee, the birthday should be the same in both databases. If a birthday is not the same in the two databases, semantic discrepancy exists. This must be resolved for database integration.
4. Semantic Relativity

Sometimes, in the existing context there are no common behaviors between two objects. But when the context is extended, common behaviors may appear.

**Definition 3.9** Object $O_1$ and object $O_2$ have *semantic relativity* for giving context $C$ if and only if there is a new context $C'$ where $C \subseteq C'$, and $O_1$ and $O_2$ have semantic likeness in $C'$.

**Example 3.9** Classes Car and Book are unrelated in an environment. When we extend the context, there is an application to access prices of a car or a book. Then Car behaves the same as Book. They are relative in the new context. We can create a new schema

\[ \text{Goods: (item name, price).} \]

for the new application and context.

5. Semantic Incompatibility

It is impossible to integrate two semantically incompatible objects. Moreover, there is no need to integrate them. They do not share any similar properties in the applications users are concerned with.

**Definition 3.10** Two objects $O_1, O_2$ have *semantic incompatibility* if they are not semantically relative, i.e., there is no context which users are concerned with in which the two objects have a semantic relativity.

**Example 3.10** Classes Person and Steel have no common behavior in the context. No applications would instill them with common properties, i.e. no applications require extension of the database context. Then these objects are semantically incompatible.
4 Conclusions and Future Work

In this paper, we precisely give a very general definition of database context and semantics in respect to context of database applications. We present a way to define and classify object semantic similarity.

Our work is an extension of work by Sheth et al [SK92]. In comparison, our main contributions are:

1. We investigate the nature of database context which was mentioned in [SK92] as an open problem. We define it as object's behaviors which we are concerned with. This definition encloses all the context cases mentioned in [SK92].

2. Based on the context concept, we define semantic similarity. Semantic equivalence is a special case of semantic similarity.

3. We proposed a measurement of semantic similarity. It is more accurate since the frequency of behavior usage is taken into account.

4. We present a taxonomy of the semantic similarity. For each case, we describe the integration to be made.

Future problems remaining to be solved are: 1) To represent semantics and semantic similarity as rules or additional attributes in databases. 2) To build an expert system to aid the evaluation of semantic similarity.

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References


