Effect of Value Based Software Engineering on Development Projects

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Abstract:

Previous models of software development projects have failed to represent people productivity accurately. In this paper, we present a model characterized by realistic productivity curves and flexibility in choosing resource factors in a software engineering project. A two-mode mathematical model similar to Putnam/Norden model is presented. The proposed model enhances the capability of engineering management users to make corrective actions when appropriate. It is extremely beneficial to detect problems and provide corrective actions since they are in many cases crucial to the successful project software engineering hiring and/or acquisition management planning to use the software product.
1 Introduction

Software development models provide techniques for estimating schedule, total cost, and total manpower or labor. The estimation should be as realistic as possible to real life situations. Productivity, although defined differently by software engineers, is considered an important attribute in a software development project. Norden[3] defines a development project as a finite sequence of purposeful, temporally ordered activities, operating on a homogenous set of problem elements, to meet a specified set of objectives representing an increment of a technological advance.” If we consider each new software system as a technological advance, then the people or team members play a major role in this advancement.

In a cost model proposed in [7], cost is directly proportional to productivity and project engineering software system. Productivity can be based on a number of factors such as the effectiveness of software development CASE tools, change in the stability of specification and the frequency of such change, design configuration stability, and quality requirements. Productivity, as defined in [7], can be improved by the software management team who can select factors to improve productivity. Productivity as defined in [9] can be viewed as a function of future concerns such as remaining tasks to be captured or the remaining project time.

In a study about predicting software productivity [10], it is indicated that companies measure software development by the line of code developed by programmers. The study suggests that coding is only a part of many activities that a software development engineer has to perform such as attending meetings, taking courses, and
calling out detailed planning. An experimental approach is instead proposed. Based on pre-existing productivity data recorded about a specific programmer or team, predictions can be made about the same programmer or team. It has been noted in [8] that during the life cycle of a project, the productivity of team members increases progressively. Such productivity can be the result of formal experience or increased learning capability. Human productivity as a result is the increasing capability to solve conformity and complexity problems. All these definitions of productivity can be transformed into the notion of quality, since all such factors effect the ultimate quality of the product.

There have been different practical and theoretical paradigms in developing software systems. To minimize delivery time, some companies use software analyzers during the coding phase. The purpose is to detect interface errors which contribute to about 75% of all errors in a system. These errors are found in the testing phase of traditional systems. Furthermore, in some software environments additional 10% errors are detected by test cases which are automatically generated by special software testing tools. By automatically detecting up to 85% of all the errors in a software system, delivery time can be reduced. In this regard, computer-aided software engineering (CASE) tools can help in increasing productivity and reducing errors as well and hence improving the quality. Theoretical estimation models, on the other hand, are categorized into two main categories: static and dynamic. Static models take a unique variable, such as size, as a starting point and uses that variable to calculate other variables such as the cost. In dynamic models, on the other hand, variables are inter-dependent; no basic variable is used. Two well-known models each fall into one of these two categories: The
COCOMO model, which is a static model, and Putnam/Norden, which is a dynamic model.

2 Background in Cost Estimation Models

An estimation model is defined as a scheme that predicts computer software data required by project planning steps using empirically derived formulae. Due to limited number of samples that provide empirical data, no estimation model can be used for all types of software and development environments. Therefore, estimation models must be used cautiously.

Static models can be further divided into two groups: single-variable and multivariable. Single-variable methods make use of a single basic variable to estimate other desired values. A typical equation that formulates this type of models is:

\[ C = aS^b \]

where \( C \) is the cost and \( S \) is the size of the code and \( a \) and \( b \) are constants.

Static, multivariable models are generally based on the same principle, except that the parameters depend on more than one variable such as methods used, user participation, memory constraints etc. Among the numerous models in the literature which fall into this category, COCOMO is the most widely accepted model which is elaborated in the next section.
The COCOMO model, abbreviated for the Constructive Cost Model (COCOMO), is a hierarchy of software estimation models [1]. This hierarchy consists of three sub-models, illustrated below:

Basic Sub-Model: This is a static single-valued model that relates the effort (cost) of the software development to the size of the code.

*Intermediate* Sub-Model: This sub-model uses a set of "cost drivers" in addition to program size to compute the cost of the projects.

Advanced Sub-Model: This sub-model takes the effect of cost drivers on each development step of the development process into account.

The basic COCOMO model is used for quick and efficient estimation in most of the small- to medium-sized software projects. Three modes of software development are considered in this model, namely: the organic mode, the embedded mode, and the semi-detached mode. The organic mode deals with simple projects in which a team of experienced programmers work in small groups. In embedded mode, a project is assumed to have tight hardware, software, and operational constraints. The semi-detached mode is an intermediate mode between the organic mode and embedded mode. The mathematical models for determining the manpower, cost, and the development time for the organic, semi-detached and embedded modes, respectively, are as follows:
These models provide an estimate for the approximate development time in terms of the cost and the projected program size. We use the relationship between the completion time and cost to determine the performance profile of projects for different cost levels. The same is done for varying manpower levels (team sizes), using a dynamic estimation model which is discussed next.

3 The Putnam/Norden Model

The objective of this model is to progressively reduce the number of problems (tasks) or faults in a project at a constant rate and hence model productivity as a linear learning curve [4]. The following assumptions are made in this model:

1. The number of problems to be solved is unknown a prior but finite.
2. The problem-solving effort does make an impact on the unsolved problem set.
3. A decision removes one unsolved problem from the set.
4. The staff size is proportional to the number of problems seeking solution.

The above assumptions lead to a Rayleigh distribution of manpower over the course of project development. This is due to the assumption that the number of problems to be solved is unknown and finite, and the total manpower effort, $K$, is an indicator of the number of problems. The rate of variation for the cumulative manpower cost, $\frac{dC}{dt}$, signifies the number of people involved in the project, $m(t)$. The cumulative cost $C(t)$ can then be expressed as:

$$C(t) = \int_0^t m(\tau) d\tau \quad (1)$$

According to the fourth assumption given above, the number of people involved is proportional to the effort remaining to be employed. Therefore,

$$\frac{dC(t)}{dt} = p(t)[K - C(t)]$$

where $K$ is the total manpower effort and $p(t)$ is a proportionality factor, which is a function of time and it takes the effect of learning/productivity into account. By integrating this equation, one obtains:

$$C(t) = K[1 - \exp\left(-\int_0^t p(\tau) d\tau\right)] \quad (2)$$

Another assumption that is made in this model is that the most representative learning curve is linear. This linearity is expressed as:

$$p(t) = 2at$$
where $a$ is a positive constant number. By carrying out the integration in Equation 2, one obtains the expression of the cumulative manpower cost as:

$$C(t) = K[1 - \exp(-at^2)]$$  \hspace{1cm} (3)

The manning of the project can easily be obtained by differentiating the above equation:

$$m(t) = 2K at \exp(-at^2)$$  \hspace{1cm} (4)

which represents a Rayleigh distribution. $m(t)$ is zero at the beginning of the project, has a single peak at a time value which is a function of the constant $a$ and then asymptotically decreases towards zero. By deriving the function $m(t)$ and finding its zero point, i.e., the peak time, we can find the so called, development time, which is given below:

$$t_d^2 = \frac{1}{2a}$$  \hspace{1cm} (5)

By substituting the values of $t_d$ into the cumulative cost equation (3), the cost at $t$, can be found in terms of the total effort spent, $K$:

$$C(t_d) = K(1 - \frac{1}{\sqrt{e}}) = 0.39K$$  \hspace{1cm} (6)

This representation, which has frequently been verified in industry on large-scale project developments involving high technology has an important implication. It allows us to carry out the scalability of the software development profile, which according to Putnam/Norden model, states that the completion of intermediate software problems must be proportional to the completion of the entire project. For example, if the project is to be completed in half the time, all steps have to be done so. This is due to the fact that the time variable $t$ appears in the cost equation in a simple form and can be easily proven.
The COCOMO model has its limitations as it does not allow factors to be introduced other than those given in the model. This model considers variations other than those caused by the specified factors of this model to be errors [7]. An extension to the COCOMO model has been proposed in [7]. The extension allows users to select factors according to actual data. A data set of software metrics collected from 71 software development projects has been used to derive the cost model. Statistical techniques such as regression analysis and principal component analysis is the basis of this extension. The fact that users can select factors is advantageous, although the representation means of these factors are limited. Team ability, for example, is represented as a set of four values (-2, -1, +1, and +2) where -2 represents the lowest ability level while +2 is for the highest level.

In order to provide a more comprehensive model we need a representation that is time changing or temporal. The reason is that in reality, changing team sizes, mobility of developers, and changing CASE technology have significant impact on the development of a software product and the time-changing parameter must be captured in a succinct manner. Although the Putnam/Norden model deals with a time varying productivity or learning capability, its modeling of human productivity doesn't represent real life situations. For example according to this model during the life cycle of a project, team members acquire more and more knowledge about the problems of the project. Productivity or capability to solve problems continues to increase indefinitely. There are two reasons that invalidate the linear productivity rate:

The learning process of human beings about a specific problem tend to saturate.
Problems in a development software project are finite.

The level of full-time-equivalent software personnel active on a project tends to follow a continuous curve where the instantaneous full-time commitment of a large number of people is an unlikely event [6]. As mentioned above, the model suggested in [6] indicates that the labor or manpower distribution for a number of software projects can be approximated by the Rayleigh distribution. From this distribution various important parameters can be obtained including the development time of a project, the peak manpower required, and the project finishing time. The development time, as mentioned in [7], is the time at which peak manpower occurs. It is the delivery time before which effort is spent on specification, design, coding, testing, and qualification [6]. Manpower requirements drop after the delivery time since the most of effort from that point on is spent on maintenance and modifications. At the delivery time, the product is considered operational [4,5]. It has frequently been verified in industry on large-scale project developments involving high technology that 39 percent of a software development project cost is consumed by the delivery time.

In this report we propose a model that combines the flexibility of model proposed in [7] and a more realistic time changing productivity model. In our model we consider two cases about the learning or productivity in a software development project. These includes:

- a rapid learning/productivity model
- an average learning/productivity model

The objective of our new models is not only to accurately analyze the man power and cost entities but also help us in improving the decision making process by providing
corrective alternatives. In order to facilitate this process we need to develop a powerful estimation mechanism that is as realistic as possible for the life cycle of a project, accurately predicts the maximum manpower required, and the time at which the maximum manpower occur. By proposing such a technique, we can find answers to some critical management issues such as:

- How to meet the completion deadline by choosing appropriate team members.
- Whether or not the current team satisfies the desired time requirements or not at any time in the project life.
- How to make corrective actions at any point of the project due to changes in time requirements or quality of the project.
- How to predict the cost and quality based on the present and the past data.

Corrective actions may imply replacing old team by a more advanced/skilled personnel, or bringing few expert software developers into the process. The proposed model is not limited to the productivity aspects of the development team. To some extent, it can also be used to study the effect of evolving CASE technology on the development process of the software project. It also implies changing cost assignments to control the quality of the project.

We apply our analysis to three major software metrics, namely, design stability, fault profiles, and requirement stability data and discuss our result at the end of the report.

4 The Proposed Models for Metric-Based Decision/Quality Tradeoffs
As mentioned earlier, we propose two new models for estimating the impact of team productivity and, in general, the impact of software environment such as the use of CASE technology on the cost and quality of project. Specifically, we illustrate the effects of varying team size and costs on the progress of software projects. We use the following three software metrics for the measurement of the progress. The following metrics identify the quality of project:

- Design Stability.
- Fault Profiles
- Requirement Stability

### 4.1 The Rapid Learning Model:

In the rapid learning model, productivity is assumed to grow exponentially. In other words, the model emphasizes the fact that during the life cycle of a project, team members' capability to solve problems increase exponentially until a final saturation level. When this final level is reached, team's productivity is maintained. Following are the reasons for choosing such model:

1. The saturation of the learning process indicates that the team cannot continue to acquire knowledge about the project indefinitely.
2. Since productivity represents the ability of solving problems, and because problems are resolved with the passage of time and thus decrease in number; productivity also decreases with time.
3. When team members have an extensive experience in software development, they may require a small duration to learn about the project. In other words, they start with a high impact on the productivity during the development process. This impact decreases as the project phase approaches towards completion. A similar impact on software development process can be extended to argument about the use of CASE technology.

A feasible curve that describes such an environment of productivity, would be an exponential curve, $p(t)$, defined as:

$$p(t) = a - b \exp(-ct) \quad (7)$$

where $a$, $b$, and $c$ are positive constant numbers. It can be noticed that in this case we have three parameters to deal with in contrast to the linear learning curve case where only one parameter controls the goal function, namely the cumulative manpower costs with respect to time. The parameters $a$ and $b$ in our model can be set to be equal to each other in case if we need to model the situation when we assume that the team at the beginning of the project has no knowledge about the work to be accomplished. Parameter $c$ indicates the productivity characteristics of the team. The larger the value of $c$ is, the faster the learning curve is.

For the proposed productivity characteristic model of the team, using the same line of procedure as adopted in the Putnam/Norden model, we can find cost, manpower, and development time. The four assumptions made in the Putnam/Norden model still hold. The representation of cumulative manpower cost, $C(t)$ expressed in man years, in terms of manpower and the learning rate is given in equation (1).
It is worthwhile to mention that the cumulative manpower cost effort, $C(t)$, is null at the beginning of the project and grows towards the total effort, $K$. Using the new model (equation 7) with equation (1) and carrying out the integration we find the cumulative manpower cost as follows:

$$C(t) = K \left[ 1 - \exp \left( -at - \frac{a}{c} \exp(-ct) + \frac{a}{c} \right) \right]$$

(8)

In this case the manning of the project would be:

$$m(t) = Ka \left( 1 - \exp(-ct) \right) \times \exp \left( -at - \frac{a}{c} \exp(-ct) + \frac{a}{c} \right)$$

(9)

As mentioned earlier, $m(t)$ is zero at the beginning of the project (when $t = 0$), and it has a single peak at the time, whose value depends on the constants $a$ and $c$. $m(t)$ then asymptotically decreases towards zero. Deriving $m(t)$ and finding its zero point, we get a quadratic equation of the form:

$$a^2 \exp(-2ct) - (2a^2 + ac) \times \exp(-ct) + a^2 = 0$$

The solutions to this equation, each representing the peak time which is referred to as the development time, are obtained as:

$$t_d = \left( \frac{1}{c} \right) \times \ln \left( \frac{2a}{2a + c \pm \sqrt{c^2 + 4ac}} \right)$$

(10)

By substituting these values of $t_d$ into equation (8), the cumulative cost in terms of the total effort spent, $K$, can be given as:
We need to set $C(t_d) = 0.39K$, in order to rationalize the industrially verified fact that for large-scale project developments, 39% of the cost occur at the development time. In other words we must validate our cumulative manpower cost for whole, we can use iterative numerical analysis. The analysis is aimed at finding the list of all possible combinations of $a$ and $c$ that satisfy the equation (11). In other words;

$$K \left[ 1 - \exp \left( -\frac{a}{c} \right) \times \ln \left( \frac{2a}{2a + c \pm \sqrt{c^2 + 4ac}} \right) - \left( \frac{2a + c \pm \sqrt{c^2 + 4ac}}{2c} \right) + \frac{a}{c} \right] = 0.39K \quad (12)$$

The result of the numerical analysis provides a list of possible solution sets for parameter $a$ and $c$. Figure (1) shows plots of manpower with respect to time as parameter $c$ increases. It is important to remember
Figure (1) Rayleigh Distribution on manpower

that the total manpower effort, $K$, is assumed to be constant. It can be observed from this figure that $c$ affects the overall distribution of manpower over time. It affects the development time as well as the peak manpower at development time. For example, for $c=0.1 \ (a=b=5)$ the development time is as high as 1.5 years while the maximum required team size is 4 persons. For the other extreme case, among the ones showed in the figure, when $c=1.9 \ (a=b=5)$ the development time is as low as 0.3 years while the maximum manpower required is 15 persons. Notice that the assumption that $K$ is constant justifies the reason that the peak manpower increases with an increase in the learning rate $c$. This might not seem intuitive, because we can think that the same peak team size, i.e., constant peak manpower, can reduce the development time when the team members are
more productive resulting in a large volume of \( c \). The assumption that \( K \) is constant requires a constant area under each manpower curve, which when changing \( c \) changes both the peak manpower and the development time. Figure (2) shows that changing \( a \), while keeping \( c \) constant, has little impact on the development time and has a more obvious impact on the maximum manpower required.

The above discussion suggests that \( c \) is the dominating factor for controlling two important project parameters; development time and peak manpower. The cumulative manpower cost function then should be determined in terms of \( c \). So far in our analysis, the new parameter, \( K \), the total effort cost in man years, has been assumed to be a constant. In the following discussion we consider a more realistic representation of the total effort \( K \). The total cost, as defined in [7] and is henceword called NEC cost model expression, can depend on various factors such as program size etc. In [7], it has been analyzed that the new parameter \( Y \), in man-hour, can be given as

\[
Y = C \times \prod_{i=1}^{n} 10^{\beta_i x_i} \times X^{\beta_i} \quad (13), \text{ where}
\]

\( x_i \): Value of factor \( i \)

\( X \): Program size in kilo lines (KL)

\( C, \beta_i, \beta_i \): Constants.
Figure (2) Manpower Distribution Over Time When Changing Parameter

For a set of 71 software development projects, the following cost in terms of the program size $X$ has been reported as:

$$y = 10^{2.418} \times 10^{0.123_x} \times 10^{0.025c^2} \times X^{0.58} \text{ MH}$$

(14)

The dominant factors in the above mentioned set of 71 projects include the development tools and development techniques/methodologies [7]. If we substitute the total effort $K$ by $Y$, we can then introduce a new dimension to our cost model. When replacing $K$ which is measured in man years with $Y$ which is measured in man hours, we need to convert the unit of $K$ from MH to MY. Man month consists of 152 hours of
working time[6] which means that a man year is 1824 man hours. For the rapid learning model the extended cost expression is thus defined as:

\[ C(t) = \frac{390}{1824} \times X^{0.958} \left[ 1 - \exp \left( -at - \frac{b}{c} \exp(-ct) + \frac{b}{c} \right) \right] \text{ MY} \]

(15)

As discussed before we set \( a = b \), and

\[ C(t) = \frac{390}{1824} \times X^{0.958} \left[ 1 - \exp \left( -at - \frac{a}{c} \exp(-ct) + \frac{a}{c} \right) \right] \text{ MY}, \]

(16)

\[ m(t) = a \times \left[ \frac{390}{1824} \times X^{0.958} \right] \left[ 1 - \exp(-ct) \right] \exp \left[ -at - \frac{a}{c} \exp(-ct) + \frac{a}{c} \right] \]

(17)

It is important to indicate that the development time is not changed, and remains as:

\[ t_d = \frac{1}{c} \ln \left( \frac{2a}{2a + c + \sqrt{c^2 + 4ac}} \right) \]

(18)

The expression (16) and (17) provide analytical estimations for the cost and the manpower required, both as a function of program size and the effectiveness of software tool and team over a period of time.

4.2 The Effect of Rapid Productivity on the Quality

One of our research objectives is to determine how the change in various parameters such as cost, time, and productivity (team/CASE technique) can affect the quality of an ongoing development of a software product. For such purpose, we can use the four software metrics mentioned above, namely; requirement stability, fault profile,
design stability, and reliability. As we collect metric data, we can use this data for evaluation the quality of the project under development.

In this section we illustrate our approach using data from the NASA project. The sub-metrics used in our stability is the percentage of requirement met as we progress through the various development phase of the project. This sub-metrics can directly determine the quality of the product, as argued in the previous report. Using this data from the design stability metrics, we have found the following relationship between design stability and cost:

\[
Q = 2.4093C^3 - 3.4591C^2 + 2.241C - 0.1192 \quad (18)
\]

where \( C \) is the cost that ranges between 0 and 1 of the final cost \( K \) and \( Q \) is the design stability that ranges between 0 to 1 of the desired design requirement, \( S \). For the cost function in equation (18) we assume that \( c \) has a value of 1.3. Figure (3) shows the above relationship. If we consider the development time in this case \( t = 1 \) year, we find that the cost, from the cost function, is 0.85594\( K \), and the quality, from the metric \( Q \) (equation 18), is 0.85135. If we wish to achieve better quality, 0.9, to occur at the same time \( t = 1 \) year, we need to allow larger cost consumption rate prior to that time. This implies changes in cost assignments and thus a new set of changes toward improved use of CASE technology and deployment of more expert personnel for the task. From the above equation, we can find \( C (=0.94K) \). Since, cost is a function of time and \( c \) and time is known (= 1 year) in this case, thus \( c \) could be found (=1.95). This result is intuitively expected; if we want to achieve better quality, we must improve our CASE technology and team personnel.

Similarly, we can predict quality using sub-metrics for the other two matrices:

requirements stability, the degree to which changes in the software requirements affect the
development effort; and fault profile, the number of known faults fixed. Using the NASA data, we have found the following relation between the requirements stability ($R$), and fault profile ($F$) in terms the cost, $C$.

$$R = 1000(4.5529C^3 - 6.1759C^2 + 2.6081C - 0.0305)$$  \hspace{1cm} (19)$$

$$F = 1000(2.2699C^3 - 3.1848C^2 + 1.4565C - 0.0401)$$  \hspace{1cm} (20)$$

Figure (3) Quality as a Function of Cost

These relations have been plotted in Figure 4 and 5.
Figure (4) Requirement Stability as a Function of Cost
4.3 Average Productivity Model

In this section we introduce the second model to represent an environment that represents the average effectiveness of CASE technology and performance of personnel. In this model, the productivity is assumed to be considerably slow in the beginning of the development process. After a slow start-up, the team members become more productive and their effectiveness starts following the rapid productivity curve discussed in the previous section. Such a model is quite common because it represents the following two phases in the performance of a software development team:
1. During the first phase, team members try to get familiar with the overall requirements and try to achieve proficiency in using CASE tools. However, the progress of the overall process can be slow. In other words, once a software engineer is given the definition of the overall project, he/she has to understand all the aspects of the given project and gradually solve the problems associated with the project.

2. In the second phase, the team members become more effective in solving the problems and using CASE tools.

The following function can be chosen to represent such phenomenon mathematically,

\[ p(t) = a - \frac{b}{\exp(ct) + \exp(-ct)} \]  \hspace{1cm} (21)

where \( a, b, \) and \( c \) are positive constant numbers. This function can approximate both the two phases mentioned above. As mentioned earlier, the team size at the beginning of the project should be zero. This requires:

\[ p(0) = 0 \Rightarrow b = 2a \] which reduces equation (21) to:

\[ p(t) = a - \frac{2a}{\exp(ct) + \exp(-ct)} \]

where \( a \) is the final productivity level that an individual might attain. This parameter is used to represent the concept of saturation in effectiveness. \( c \) represents how slow the team members are in the beginning of the project and how they become more effectiveness later in the process of development. Larger values of \( c \) represent short duration for slow phase of productivity and quality shifting the productivity at a faster
pace. Figure (6) shows different plots for $p(t)$ as $c$ increase.

![Figure (6) Average Productivity Model Curves](image)

Following the same analysis as is given in the previous section, we obtain the following expression for $C(t)$ and $m(t)$:

\[ C(t) = K \left[ 1 - \exp(-at + \frac{2a}{c}(\tan^{-1}(\exp(ct)) - 0.7854) \right] \quad (22) \]

\[ m(t) = -K \left( -a + 2a \times \frac{\exp(ct)}{1 + \exp(2ct)} \right) \times \exp\left( -at + \frac{2a}{c}(\tan^{-1}(\exp(ct)) - 0.7854) \right) \quad (23) \]

Finding the derivative of $m(t)$ and setting it to zero in order to find the development time, we have the following equation:

\[ a^2 \exp(4ct) + (-2ac - 4a^2) \exp(3ct) + (6a^2) \exp(2ct) + (2ac - 4a^2) \exp(ct) + a^2 = 0 \]

\[ (24) \]

It is obvious from equation (24) that it is quite difficult to find the development time in terms of $a$ and $c$ analytically. We also have to keep in mind that the condition
\[ C(t_d) = 0.39K \] must be satisfied. Having these two purposes in mind, we need to find a relationship between parameters \( a \) and \( c \) to simplify the above polynomial. Random choosing a value for \( a \) in the above polynomial, we found that for \( a = 1.8c \),

\[ C(t_d) = 0.3755K \] which can be considered to be acceptable. Accordingly, the solution to the polynomial is as follows:

\[
\exp(¢t_d) = 3.6707 \Rightarrow t_d = \left( \frac{1}{c} \right) \ln(3.6707)
\]

Thus, \( C(t) = K \left[ 1 - \exp(-1.8ct + 3.6\tan^{-1}(\exp(ct)) - 0.7854) \right] \), \( t \)

\[
m(t) = -K \left[ -1.8c + 3.8c \times \frac{\exp(ct)}{1 + \exp(2ct)} \right] \times \exp\left( -1.8c + 3.6\tan^{-1}(\exp(ct)) - 0.7854 \right)
\]

(26)

The average rate of software team build up is defined as:

\[
SBU = \frac{m_0}{t_d} = 1.077 \times K \times c^2 \times \exp(-1.8c + 1.87) \quad (27)
\]

where \( m_0 \) is the peak manpower at delivery time and \( t_d \) is the development time.

Figure (7) shows the Rayleigh distribution of manpower with respect to time. The total effort \( K \), as before, is assumed to be constant. Higher values of \( c \), which correspond to high productivity rate, result in a smaller development time

Incorporating the NEC cost model, the cost and manpower expressions when using the NEC cost model are given as follows:

\[
C(t) = \frac{390}{1824} \times 0.958 \left[ 1 - \exp(-1.8ct + 3.6 \tan^{-1}(\exp(ct)) - 0.7854) \right], \quad (28)
\]
\[ m(t) = \frac{390}{1824} X^{0.958} \left( -1.8c + 3.6c \frac{\exp(ct)}{1 + \exp(2ct)} \right) \times \exp(-1.8c + 3.6(\tan^{-1}(\exp(ct)) - 0.7854)) \]

(29)

Figure (7) Rayleigh Distribution of Manpower based on the Average Productivity Model

Table 1 shows how factor c affects the finishing time (FT), the development time (DT), and the slow productivity time (ST) which is the period of time during which the team's productivity rate is slower. The percentage columns, following DT and ST
columns, represent the percentage of development time and slow time with respect to finishing time, respectively.

We notice from Table 1 that percentage DT first increases and then decrease. A slightly different increase followed by some decrease in percentage ST can be noticed as well. For $c = 1.7$ notice that DT is 21% and ST is 13.3%. We consider this as the best representation of the average productivity model.

4.4 The Effect of Average Productivity Environment on The Quality

We now find the relationship between the metrics mentioned earlier and cost. For the design stability metric, we find the following relationship between the design stability ($Q$) and cost ($C$):

$$Q = 2.4428C^3 - 3.8706C^2 + 2.7698C + 0.0706 \quad (30)$$

<table>
<thead>
<tr>
<th>$C$</th>
<th>$FT$ (yrs)</th>
<th>$DT$ (yrs)</th>
<th>%DT</th>
<th>$ST$ (yrs)</th>
<th>%ST</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.5</td>
<td>9</td>
<td>2.6</td>
<td>28</td>
<td>1.7</td>
<td>18.9</td>
</tr>
<tr>
<td>0.7</td>
<td>6.5</td>
<td>1.857</td>
<td>28</td>
<td>1.5</td>
<td>23</td>
</tr>
<tr>
<td>0.9</td>
<td>5</td>
<td>1.445</td>
<td>29</td>
<td>1.25</td>
<td>25</td>
</tr>
<tr>
<td>1.1</td>
<td>4.2</td>
<td>1.18</td>
<td>28</td>
<td>0.7</td>
<td>16.67</td>
</tr>
<tr>
<td>1.3</td>
<td>4</td>
<td>1</td>
<td>25</td>
<td>0.5</td>
<td>12.5</td>
</tr>
<tr>
<td>1.5</td>
<td>3.5</td>
<td>0.8669</td>
<td>24</td>
<td>0.45</td>
<td>12.8</td>
</tr>
<tr>
<td>1.7</td>
<td>3</td>
<td>0.7649</td>
<td>21</td>
<td>0.4</td>
<td>13.3</td>
</tr>
<tr>
<td>1.9</td>
<td>2.5</td>
<td>0.6844</td>
<td>27</td>
<td>0.35</td>
<td>14</td>
</tr>
<tr>
<td><strong>2.1</strong></td>
<td><strong>0.06192</strong></td>
<td><strong>27</strong></td>
<td><strong>0.3</strong></td>
<td><strong>13.4</strong></td>
<td></td>
</tr>
</tbody>
</table>

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Table 1: A profile of the average productivity curve:

Equation (30) represents the relationship between cost and design stability when cost ranges between 0 and 1 of the final cost K, and Q ranges between 0 and 1 of the desired design requirement. Figure (8) shows the above relationship between quality and cost. This cost function assumes a value of 1.7 for c. If we consider the development time in the latter case to be $t = 9$ months, we find that the cost is $0.3614K$, and the quality, from the metric, is 0.6317. If we wish to achieve a better quality, 0.8, at the same time $t = 9$ months, we need to allow larger cost consumption rate prior to that time. This indirectly implies a new team with high productive personnel. From the above equation, we can find $C (=0.555K)$. Since cost is a function of time and $c$ and in this case time is known ($=9$ months), $c$ can be found to be equal to 2.15. This result is intuitively expected; if we want to achieve better qualities, we have to hire a more productive team or use a more effective CASE tool environment.
Figure (8) Quality as a Function of Cost

Similar predictions for the other two matrices namely: requirements stability and fault profile can be made. As a case study, we use the NASA data and find the equations for R, requirements stability, and F, fault profile in terms the cost, C, as:

\[ R = 1000(2.2065C^3 - 3.1434C^2 + 1.4738C + 0.0484) \]  \hspace{1cm} (31)

\[ F = 1000(3.112C^3 - 4.1855C^2 + 2.039 + 0.1284) \]  \hspace{1cm} (32)

These equations have been plotted in Figure 9 and 10, and show the same trend as of design
stability metric.

Figure (9) Requirement Stability as a Function of Cost
5 Summary

It is important to compare our two newly proposed models with the Putnam/Norden model. Figure (11) shows the rapid learning/productivity model with productivity rate $c=1.3$ and two linear models with productivity rates $a=5$ and $a=1.5$. 
Figure (11) Rapid Learning/Productivity Curve in Comparison to Two Linear Learning/Productivity Curves

Figure (12) provides a similar comparison between the average learning/productivity model with rate $c=1.7$ and two linear learning/productivity models with same rates as mentioned above. The corresponding manpower distributions are given in Figures (13) and (14). It is known that the coding activity phase typically contributes to 42% of the overall project activities and maintenance activities including rewriting parts of the code contribute to 48% of the project activities [8].
Figure (12) Average Learning Curve in Comparison to Two Linear Learning Curves

Figure (13) Manpower Distribution of Rapid Model in Comparison to Two Linear model
Figure (14) Manpower Distribution of Average model in Comparison to Two Linear models.

In other words, the development time should typically be at about 42% of the finishing time of the project which is observed in the rapid learning model. For a high linear productivity rate $a=5$, the manpower distribution tends to be symmetric with respect to development time which is not quite realistic for the reason given above. Additionally, peak manpower is significantly high which is not desirable due to communication and interactive problems among large team members. In Figure (14), on the other hand, we can see that the development and finishing times of the average model and the linear model with low productivity rate are close. For software development projects having project duration in the range of one to two years, the rapid productivity model represents a realistic representation of a highly qualified/productive team and an effective use of the CASE environment. For larger software development projects, the
average productivity model is expected to behave better than the linear productivity model with low learning rates due to the fact that average team personnel improve their performance later in the project.

5 Conclusion

In summary, our main goal in this report was to represent accurately the human productivity factor in the development of software projects. In previous sections this factor historically was considered to be either indefinitely growing or was always constant. Our proposed models introduce a time changing human productivity that grows for some time and then saturates. It should also be noted that the final cost of a software development project can be given in terms of program size derived from the NEC model. Software development engineers using these proposed models can change quality requirements as needed. The price is extra cost for paying more experienced labor. In this latter case new cost distribution and schedule can be determined a priori. The rapid productivity model, as discussed above, is a more realistic representation of manpower distribution than the linear model with high learning rate; whereas the average learning model is comparable to the linear model with low learning rate in representing the manpower distribution.
References:


